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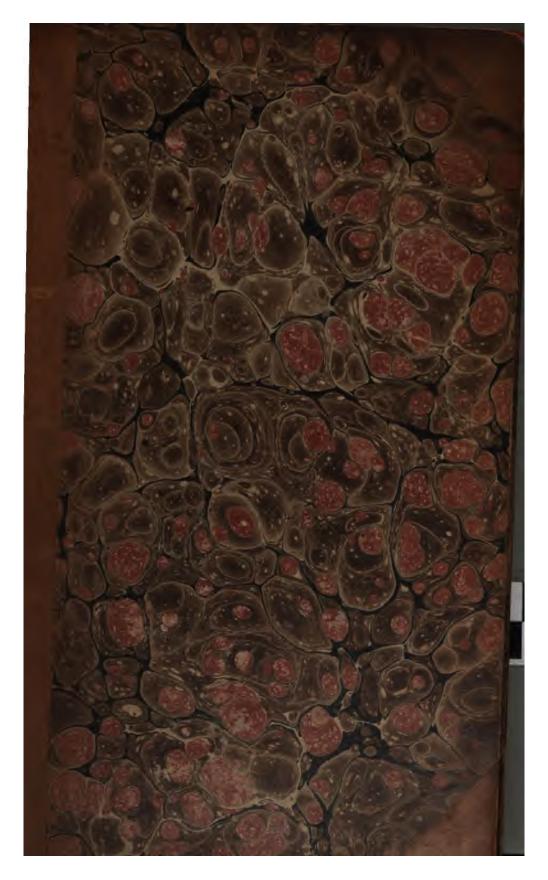
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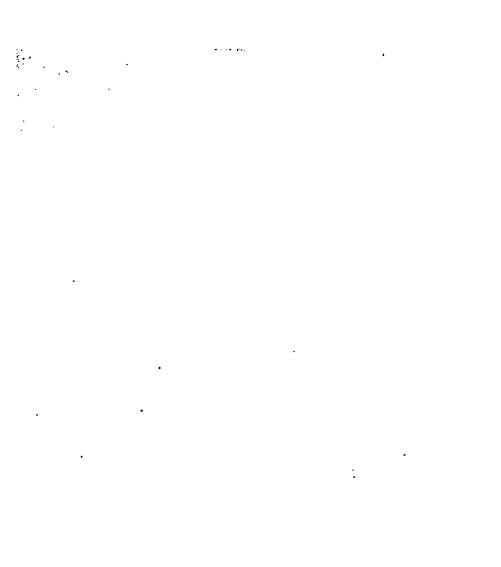


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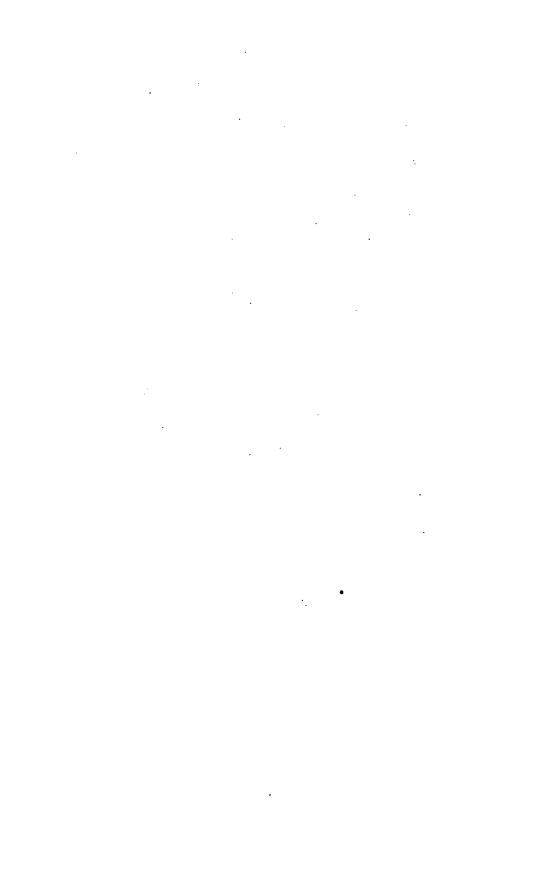


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MATHEMATICAL

AND

ASTRONOMICAL TABLES,

FOR THE USE OF

STUDENTS OF MATHEMATICS,

PRACTICAL ASTRONOMERS, SURVEYORS, ENGINEERS,
AND NAVIGATORS;

WITH

AN INTRODUCTION,

CONTAINING

THE EXPLANATION AND USE OF THE TABLES,

ILLUSTRATED BY

NUMEROUS PROBLEMS AND EXAMPLES.

BY WILLIAM GALBRAITH, M. A.,

TEACHER OF MATHEMATICS IN EDINBURGH.

EDINBURGH:

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LIVER * BOYD, PRINTERS.

SIR GEORGE CLERK, OF PENNYCUICK,

BART., M.P., F.R.S.,

ONE OF THE LORDS COMMISSIONERS OF THE ADMIRALTY, &c., &c.

SIR,

THE following Work, which you have allowed me the honour of inscribing to you, is intended to promote the purposes of useful instruction, and the advancement of practical science; and it is therefore confined to subjects having a direct utility in the business of life.

THOUGH I am aware that no patronage can materially influence the success of a Work of this nature, which must depend upon its merits alone; yet I have been solicitous to inscribe it to you, in the hope, that practical men, in search of useful knowledge, may be induced to consult a Book sanctioned by a name intimately connected with many recent scientific improvements; and I confidently trust, that a reference to the volume itself will prove that your obliging permission has not been undeservedly bestowed.

I have the honour to be,

SIE,

With the utmost respect,

Your most obedient servant,

WILLIAM GALBRAITH.

EDINBURGH, Nov., 1826.

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PREFACE.

THE application of the mathematical sciences to practical purposes has of late made great advances in accuracy and precision. The perfection also which astronomical and geodetical operations have reached, and the extreme delicacy of construction to which instruments have been carried, require correspondent improvements in the methods of computation and reduction; and, therefore, convenient tables of moderate expense must be of great value to those engaged either in the details of practice, or the husiness of instruction.

There are two classes of tables chiefly in use; one either large and expensive, or attached to expensive works, and which therefore can with difficulty be procured by the generality of purchasers; the other so limited and defective as to be totally unfit for constant reference. It has been my study to hold a middle course between these two extremes. By making such additions to the usual tables as to render their application more easy, without greatly increasing their bulk; by selecting the most useful from larger collections; by supplying some new tables, and simplifying the practical rules, several very laborious processes have been rendered more simple and precise, while the requisite accuracy for the nicest purposes has been strictly preserved.

In most of our initiatory works for popular instruction, the processes and examples are unfortunately conducted in such a manner as to be comparatively of little advantage in actual practice, and, consequently, what has been learned in youth, must, in a great degree, be forgotten in manhood, while new methods are then to be acquired.

To remedy this inconvenience, I have selected some of the most approved modes of treating the problems frequently required by Astronomers, Navigators, and Engineers, from the works of persons celebrated for their successful application of the exact sciences to the niceties of modern practice.

I have therefore taken many of the Astronomical Rules and Examples from the works of Maskelyne, Pond, and Brinkley; and such as relate to other topics from those of Captains Kater, Hall, Sabine, and Parry. To Captain Hall I am under great obligations, not only for access to his original papers, but also for his friendly advice relative to the application of these methods to practice.

To Mr Ivory I am indebted for his very accurate Table of Astronomical Refractions, which I have endeavoured to improve by expanding and adding proportional parts to the subsidiary tables, thereby facilitating its practical application.

Besides labouring to improve many of the ordinary Tables, I have added several which are new, chiefly for the purpose of simplifying some operations and rendering others more accurate.

The explanations will, it is hoped, be found full and explicit, especially towards the beginning. The explanation of some tables which follow others, analogous in structure or arguments, is sometimes less full, as it is presumed those previously given are well understood. For example, the note to Table XXV., at the bottom of page 91, can hardly be intelligible to a mere practical man who has little mathematical knowledge; but as the method of taking out the quantities from Table V., in whatever quadrant of the circle, or division of 24 hours, they are situated, is so fully explained before, it was thought unnecessary to repeat the same minutiæ a second time. Still, however, there may be some parts which require to be expanded, in order to be more readily understood, as well as others which might, perhaps with propriety, be abridged.

The Introduction is divided into three parts, followed by a copious explanation of the general tables, which may be called a fourth.

In the first I have shortly described the nature, and investigated the more simple series for the computation of Logarithms. I have generally, however, only given the more important rules in words at length, without investigation, so as to be readily comprehended by persons who have acquired a knowledge of the elementary principles of mathematics. In fact, the demonstrations can only be understood by those who have obtained a tolerable knowledge of the elements of geometry and algebra, and, since the generality of books containing these comprehend also the usual investigations in trigonometry, it was thought advisable to omit them. If, for example, a student should purchase Legendre's Elements of Geometry in order to study that science, he will find it to contain also very elegant investigations of almost all the useful properties in Plane and Spherical Trigonometry. On this account, I have only given the demonstrations of those propositions less commonly inserted in the usual treatises.

On the Barometric Measurement of Altitudes, I have given four different methods. The third is in a great degree new, and by the original subsidiary tables, calculated expressly for this purpose, it will be found easy and accurate.

The second part contains Spherical Trigonometry, with a great variety of its most useful applications. As the rules and examples are either new or selected from the best writers on the subject, it is hoped this section will prove interesting to students of Astronomy and Navigation, since it contains a number of the usual methods and examples practised by the most distinguished men of science of the day.

The third part contains a variety of Rules and Formulæ for the use of Surveyors, Engineers, Navigators, and practical Astronomers. Those for geodetical purposes are selected chiefly for their general utility, and comprehend a sufficient number for usual practice,—an idea which was suggested to me by some of my more advanced pupils who have been employed in government surveys. They were first collected in the form of notes and transcribed into their albums, to be used when they were engaged in geodetical, accurate military or marine surveying; and as they may prove generally useful to that class of Students, I have arranged them in as natural an order as possible.

The ingenuity and skill of Captain Kater having devised the most beautiful simplifications of the problem of determining the figure of the earth by means of the pendulum, and brought the experiment within the reach of our more active and intelligent military and naval officers, I have added the necessary rules and formulæ for that purpose, in order to initiate, as far as possible,

our Cadets and Midshipmen in these interesting researches; as such higher objects of pursuit, not only invigorate their faculties, but inspire them with enthusiasm for the attainment of professional renown.

The fourth part contains the necessary Explanation of the Tables.

I have thus endeavoured to collect, into as small a space as possible, the greatest quantity of useful matter naturally connected with the subjects treated in the work; but with what success I must allow the public to determine.

WILLIAM GALBRAITH.

EDINBURGH, November, 1826.

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INTRODUCTION.

PART I.

OF LOGARITHMIC AND TRIGONOMETRICAL TABLES.

SECTION I.

Of the Properties of Logarithms.

1. Logarithms are a series of numbers, originally invented by Baron Napier, for the purpose of facilitating arithmetical calculations. This end is attained by their enabling us to perform the operations of multiplication by addition, of division by subtraction, of involution by multiplication, and of the extraction of roots by division.

2. It is evident that any two series of numbers, the one being in arithmetical and the other in geometrical progression, possess these properties, thus, for example, let the

Ar. series be 0 1 2 3 4 5 &c. Geo. series 1 10 100 1000 10,000 100,000 &c.

Now, if we add any two numbers in the arithmetical series, such as 2 and 3, which are equal to 5, and multiply the corresponding numbers under them, 100 and 1000, we have 100,000, the number immediately under 5, which was obtained by the addition of 2 to 3. Hence, then, it is clear that, if tables of this kind, sufficiently extensive, were formed, by a reference to them, the operation of multiplication could be performed by means of addition.

In like manner, we perform division by subtraction, for, if from 5 we take 3, the remainder is 2, under which we get 100, that is 100,000, the number under 5, divided by 1000, that under 3, gives

100 as a quotient.

Roots are readily determined in a similar way; thus, 4, in the arithmetical series divided by 2 gives 2, under which, in the geometrical series, is 100, that is, the second, or square root of 10,000 the number under 4, is 100, the number under 2, and so on.

Napier called the first series the logarithms of the corresponding

numbers in the second.

3. Since the two series may be assumed at pleasure, we may have

as many different systems of logarithms as we choose.

4. The series in art. 2 being adapted to the common denary scale of arithmetic, is, on the whole, the most convenient for general purposes, though other systems have, in particular cases, their peculiar advantages.

On considering these series, it appears that the logarithm of 1 is

[•] The identity of this process with that performed upon the exponents of quantities in the corresponding operations of algebra, will be obvious to those who have acquired the rudiments of that branch of mathematics.

0, and that of 10 is 1, and hence the logarithms of all numbers between 1 and 10 are greater than 0 and less than 1, that is, they are fractions. In the same manner, between 10 and 100 they are greater than 1 and less than 2, that is, they are 1 with some fraction annexed, and so on. The whole numbers or integers in the logarithmic series are hence easily obtained, being always a unit less than the number of figures in the integral part of the corresponding natural number. On this account it is customary, in the common printed tables, to put down only the fractional part in the form of a decimal, the computer supplying the whole number or integer under the name of index.

5. In order to generalize, let us assume the two following series:

 r^x , r^y , $r^{x''}$, $r^{x''}$, &c. . . . (1) y, y', y'', &c. . . (2) in which r is some given number greater or less than unity, and x, x', x", &c. any variable quantities chosen in such a manner that $r^{x}=y$, $r^{x'}=y'$, $r^{x''}=y''$, $r^{x''}=y'''$, &c., then the several exponents, x, x'. x", x", &c. of the series (1) are called the logarithms of the corresponding terms in the series (2).

Thus if y, y', y'', y''', &c. be a series of numbers such that $r^x = y$, $r^x = y'$, $r^x'' = y''$, $r^x''' = y'''$, &c., then $x = \log y$, $x' = \log y'$, $x'' = \log y''$,

x'''=log. y''', &c.

6. For the purpose of adapting the series (1) to the series of natural numbers 1, 2, 3, &c. the given number r must be greater than unity, the first index x must be equal to 0, and the several indices x', x", x", &c. must continually increase. For, since by the principles of algebra, $x^{\circ}=1$, whatever r may be, this series will increase from 1 to infinity; and by properly adjusting the values of x', x'', x", &c. it is evident that the several quantities rx, rx", rx", &c. may be made to coincide with the numbers 2, 3, 4, &c. For example, let r=10; then, since 10°=1, find 101=10, the indices of 10, which would give 10", 10", 10", &c. equal to the numbers 2, 3, 4, &c., must be fractions between 0 and 1. If we take the number 3 we have 10^{12} = 3.16 nearly, from which we infer that a fraction (x')somewhat less than $\frac{1}{2}$ or 0.5, being made the index of (r) 10, would give 10"=3. This fraction is found by calculation to be 47712; hence $10^{47719}=3$; therefore, when r=10, the logarithm of 3 is .47712.

In like manner, if we assume the number 5, whose logarithm is to be found in place of that of 3, we have 10\(^1=4.64\) whence a fraction, $x^{(n)'}$ somewhat greater than $\frac{2}{5}$, or .666 being made the index or exponent of 10, would give $10^{x^{(n)'}} = 5$. This fraction more accurately computed is found to be .69897, that is, when r=10 the loga-

rithm of 5 is .69897.

7. From this it appears, that the value of the logarithm of any given number depends upon the value of the number r, and that by assuming it equal to different numbers, as many different systems of

logarithms may be formed as we please.

In every system, however, since $r^{\circ}=1$, the logarithm of 1 must be 0. This constant quantity r from the powers of which the natural numbers are formed, is called the radix or base of the system to which it belongs.

8. In the general equation $r^x = y$, (art. 5.), let us make x vary

and observe the correspondent variations of y.

If r is greater than 1, on making x=0, we have y=1; when x=1 then y=r or the logarithm of the base is=1; in proportion as x increases from 0 to infinity, y will increase from 1 towards r, and afterwards to infinity, so that if we suppose x to pass through all the intermediate values, in following the law of continuity, y will increase also in the same manner, though much more rapidly.

If we put for x, negative values, we shall have $y=r^{-x}$, or $y=\frac{1}{r^x}$. Here we see, in like manner, that the more x increases the

more y or $\frac{1}{r^2}$ decreases, so that in proportion as x augments, negatively y takes all possible values less than 1 as far as 0, in which case x becomes infinite. This was the proposition which Napier made to Briggs on their celebrated meeting at Edinburgh, when conversing on the propriety of changing the logarithmic scale.

If r is less than 1 we shall make $r=\frac{1}{b}$, b being greater than 1 and

we have $y = \frac{1}{b^x}$ or $y = b^x$, according as x is positive or negative. We fall here upon the same case, with this difference, that x is positive when y is less than 1, and negative when y is greater than 1. This proposal Briggs made to Napier, but immediatly abandoned it on Napier suggesting that mentioned above, which was finally adopted.

If r=1, we have y=1 whatever x may be.

We may then say generally, that provided r is not unity, there can always be found a value for x, which renders r^* equal to any given number y. The constant use that is made of the properties of the equation $y = r^*$ requires the denominations of its parts to be fixed in order to avoid circumlocution. Hence as before remarked, x is called the logarithm of the number y, the invariable number r is called the base and, finally, the logarithm of a number, the power to which the base must be raised in order to produce that number.

With regard to the base r it is arbitrary, and when we write $x=\log y$ to show that x is the logarithm of the number y or that $y=r^x$, the base r is alway understood, because when once chosen it is supposed to remain fixed. If it should be changed the new base

ought to be indicated.

9. From these principles are derived several properties.

1°. In every system of logarithms, the logarithm of 1 is 0 and that of the base r is 1.

2°. If the base r is greater than 1, the logarithms of numbers greater than 1 are positive, the others are negative. The contrary

takes place if r is less than 1.

3°. The composition of a table of logarithms consists in determining all the values of x when y is made successively equal to 1, 2, 3, &c. in the equation $y=r^x$.

The ratios are the arbitrary numbers e and μ . We may, therefore, regard the systems of values of x and y which satisfy the equation

 $y=r^s$, as classed in these two progressions, which coincides with what has been already said in art. (2.)

10. We shall now demonstrate algebraically the various properties

of logarithms.

Let N and n be any two numbers belonging to the series (1); and for example, let $N=r^x$ and $n=r^x'$, then $N = r^x \times r^y = r^{x+x'}$, but, by art. 5, the logarithm of $r^{x+x'}$ is $x+x'=\log r^x+\log r^y = \log r^x+\log r^y$.

In like manner, if n, n', n'' be any set of numbers in the series (1) it might be shown that the logarithm of $n \times n' \times n''$, &c.=log. $n+\log n'+\log n''$, &c., from which we infer that the logarithm of the product of any number of factors is equal to the sum of their logarithms.

11. Again $\frac{N}{n} = \frac{r^x}{r^{x'}}$; but the logarithm of $r^{x-x'} = x - x'$; therefore,

the logarithm of $\frac{N}{r}$ =x-x'=log. r^x -log. r^x =log. N-log. n; hence it appears, that the logarithm of the quotient of any two numbers is equal to the difference of their logarithms; and that the logarithm of a fraction $\left(\frac{N}{n}\right)$ is equal to the logarithm of its numerator minus, the logarithm of its denominator.

If N be less than n, then log. N—log. n is negative; therefore,

the logarithms of all proper fractions are negative.

12. Let $N=r^x$ be raised to the m^{th} power, then $N^m=r^{mx}$; but the logarithm of r^{mx} is=mx, hence the logarithm of $N^m=mx=m$ log. r^x =m log. N; for the same reason, since $\sqrt{N=N_m^1=r_m^x}$, the logarithm

of $\sqrt[m]{N = \frac{x}{m} = \frac{\log N}{m}}$; from which we infer, that the logarithm of the m^{th} power of any number is found by multiplying its logarithm by m, and that of the m^{th} root of any number, by dividing its logarithm by m.

SECTION II.

Of the Construction of Tables of Logarithms.

13. Let r^x express generally any term of the series, (1), and let N be the corresponding number, then r^x =N. Hence to find the logarithm of N is merely to solve the equation r^x =N where x is the unknown quantity. In order to accomplish this purpose let r=1+b and N=1+n, then extract the y^{th} root of each side of this equation,

and we obtain $(1+b)\frac{x}{y} = (1+n)\frac{1}{y}$, which by expansion gives

$$1 + \frac{x}{y}(b) + \frac{x}{y} \left(\frac{x}{y} - 1\right) \left(\frac{b^2}{2}\right) + \frac{x}{y} \left(\frac{x}{y} - 1\right) \left(\frac{x}{y} - 2\right) \left(\frac{b^3}{2.3}\right) + \&c. = 1 + \frac{1}{y}(n) + \frac{1}{y} \left(\frac{1}{y} - 1\right) \left(\frac{n^2}{2}\right) + \frac{1}{y} \left(\frac{1}{y} - 1\right) \left(\frac{1}{y} - 2\right) \left(\frac{n^3}{2.3}\right) + \&c.$$
Now suppose y to be indefinitely great with respect to x and 1 ,

Now suppose y to be indefinitely great with respect to x and I, then will $\frac{x}{y}$ and $\frac{1}{y}$ vanish in reference to -1, -2, &c., so that $\frac{x}{y}-1$ and $\frac{1}{y}-1$ will each become equal to -1; $\frac{x}{y}-2$, $\frac{1}{y}-2$, each

equal to -2, &c. &c., hence rejecting 1 from each side of the equa-

$$\frac{x}{y} (b - \frac{1}{3} b^2 + \frac{1}{3} b^5 - \frac{1}{4} b^4 + &c.) = \frac{1}{y} (n - \frac{1}{3} n^2 + \frac{1}{3} n^3 - \frac{1}{4} n^4 + &c.)$$
hence x , the log. $(1+n) = \frac{n - \frac{1}{3} n^2 + \frac{1}{3} n^3 - \frac{1}{4} n^4 + &c.$
but $n = N - 1$ and $b = r - 1$, therefore, by substitution, the above ex-

pression becomes

$$\begin{array}{l}
\bullet \ \, \frac{(N-1) - \frac{1}{2} (N-1)^2 + \frac{1}{5} (N-1)^5 - \frac{1}{4} (N-1)^4 + &c.}{(r-1) - \frac{1}{2} (r-1)^2 + \frac{1}{5} (r-1)^3 - \frac{1}{4} (r-1)^4 + &c.}
\end{array}$$

14. Let
$$\frac{1}{(r-1)^{-\frac{1}{2}}(r-\frac{1}{2}(r-1)^2+\frac{1}{3}(r-1)^3-\frac{1}{4}(r-1)^4+&c.=}$$
 $\frac{1}{D}=M$.

This quantity M, which evidently depends upon the base r, is called the modulus of the particular system of logarithms to which it belongs. As it is obvious the series $n = \frac{1}{2}n^2 + \frac{1}{3}n^3 = \frac{1}{2}n^4 + \frac{1}{3}n^5 = \frac{1}{3}n^4 + \frac{1}{3}n^4 + \frac{1}{3}n^4 = \frac{1}{3}n^4 + \frac{1}{3}n^4 + \frac{1}{3}n^4 = \frac$ &c. will not converge when n is any whole number greater than unity, before proceeding to the calculation of the logarithms of any particular system, it will be proper to show the manner in which the value of x in the last article may be expressed in a converging series. This may be effected by means of the following process in which M is substituted for the quantity

By means of this formula the logarithm of a quantity exceeding unity by a very small fraction may be readily found.

Since the log. of 1=0, this last series which converges very rapidly, will give the logarithms of all the natural numbers, with facility in succession. To these theorems might have been added others still more convenient, but they are sufficient for ordinary

15. Before proceeding to compute a table of logarithms, some value must be assigned to M. Since the value of r is arbitrary, let

it be so assumed that $(r-1)-\frac{1}{2}(n-1)^2+\frac{1}{3}(r-1)^3-&c$. or M shall be equal to 1, that adopted by Napier. Taking series (8) we have since

Log.
$$1 = 0$$
 (art. 6.)
 $2 = 2\left(\frac{1}{3} + \frac{1}{3^4} + \frac{1}{5 \cdot 3^5} + &c. \text{ to } 8 \text{ terms}\right)$. $= 0.6931472$
 $3 = 2\left(\frac{1}{5} + \frac{1}{3 \cdot 5^5} + \frac{1}{5^6} + &c.\right) + \log 2$. $= 1.0986123$
 $4 = 2 \log 2 \text{ (art. } 12)$. $= 1.3862944$
 $5 = 2\left(\frac{1}{9} + \frac{1}{3 \cdot 9^5} + \frac{1}{5 \cdot 9^5} + &c.\right) + \log 4$. $= 1.6094379$
 $6 = \log 2 + \log 3 \text{ (art. } 10)$. $= 1.7917595$
 $7 = 2\left(\frac{1}{13} + \frac{1}{3 \cdot (13)^5} + \frac{1}{5 \cdot (13)^5} + &c. + \log .6$. $= 1.9459101$
 $8 = 3 \log 2 \text{ (art. } 12)$. $= 2.0794415$
 $9 = 2 \log 3 \text{ (art. } 12)$. $= 2.0794415$
 $9 = 2 \log 3 \text{ (art. } 12)$. $= 2.1972246$
 $10 = \log 2 + \log 3 \text{ (art. } 10)$. $= 2.3025851$

In this manner the Napierean logarithms of all the natural numbers may be found. As their accuracy, however, depends upon those immediately preceding, being derived successively from each other, it would be necessary to check the computations in the actual construction of a table of logarithms by some independent formula, such as (6), though this in large numbers would be rather inconve-

nient from its slow convergency.

16. To find the value of r, the base, in this system recourse must be had to the series (3) art. (14). If log. (1-n) or log. N be put =l and M=1, we have $l=n-\frac{1}{2}n+\frac{1}{3}n^3-\frac{1}{4}n^4+$, &c.; reverting this series, and 1+n, or N= $1+l+\frac{1}{2}l^2+\frac{1}{2\cdot 3}l^5+\frac{1}{2\cdot 3\cdot 4}l^4$, &c. Now let l=1, then the number whose logarithm is 1, that is, the base $r=1+1+\frac{1}{2}+\frac{1}{2.3}+\frac{1}{2.3.4}+$, &c. =2.7182818. To prevent confusion, however, we shall always designate the base or radix of this system by R, retaining r for that of the common logarithms. Hence R=2.718,281,82846.

These are also called hyperbolic logarithms from their application to the quadrature of the hyperbola; but this designation is improper,

as any system may be similarly employed.

17. When we have the logarithm of a number N for any particular value of r, the base, we can readily obtain the logarithm of the same number in every other system. Since, art. (5), when the base is t we have $r^x=N$, we shall likewise have $R^x=N$ when the base is R, in which x is different from X, therefore, $R^X = r^x$.

=0.3010000

1.0000000

Now taking the logarithms relatively to the system whose base is r, then

but l.r = x by hypothesis, and l.R = X l.R, art. (12), whence X l.R = x, or $X = \frac{x}{\sqrt{R}}$. But if R is the base, X will be the logarithm of N in the system having that base, and designating this by L.N to distinguish it from the other, we shall have L.N= $\frac{l.N}{l.R}$ (12)

consequently we obtain the logarithm of N in the second system, by dividing its logarithm taken in the first system by the logarithm of the base of the second system. Again from formula (12) we get

 $L.N \times l.R = l, N$ Hence in every system the logarithm of any number is the product of its Napierean logarithm by the logarithm of R, called the modulus.

Also since $\frac{l. N}{L.N} = l. R$, there exists between l. N and L.N a constant ratio represented by I.R

Since we have by formula (12) L.N= $\frac{l.N}{l.R}$, as N=10, then art (15)

 $2.3025851 = \frac{1}{M}$, or $M = \frac{1}{2.3025851} = 0.4342944819$, and $2 M = \frac{1}{2.3025851} = 0.4342944819$

18. It is now easy to construct a table of common logarithms whose base r=10, for by formula (13) we have $l.N=l.R\times L.N$, but l.R = M = 0.4342944849; consequently $l.N = 0.4342974819 \times L.N.$ It therefore only is necessary to substitute this value for M in any of the series formerly give for the computation of the Napierean logarithms to obtain the common; thus, if in series (8) for 2 M we substitute its value 0.86858896 we shall have

log. $(N+1)=0.86858896\left(\frac{1}{2N+1}+\frac{1}{3(2N+1)^3}+\frac{1}{5(2N+1)^5}+&c.\right)$ + log. N, and making N successively 1, 2, 3, &c. Log. 1 =0.0000000 $2 = 86858896 \left(\frac{1}{3} + \frac{1}{3^4} + \frac{1}{5 \cdot 3^5} + , &c. \right)$

$$3 = 86858896 \left(\frac{1}{5} + \frac{1}{3 \cdot 5^3} + \frac{1}{5^6} + , &c. \right) + \log 2 = 0.4771213$$

$$4 = 2 \log 2. \qquad = 0.6020600$$

$$4 = 2 \log_2 2$$
. $= 0.6020600$

$$5 = 86858896 \left(\frac{1}{9} + \frac{1}{3.9^3} + \frac{1}{5.9^3} + , &c.\right) + \log. 4 = 0.6989700$$

$$6 = \log. 2 + \log. 3 = 0.7781513$$

6 = log. 2+log. 3 = 0.7781513
7 = 86858896
$$\left(\frac{1}{13} + \frac{1}{3(18)^3} + \frac{1}{5(13)^5} + &c.\right) + log. 6 = 0.8450980$$

$$8 = 3 \log_2 2$$
 =0.9030900
 $9 = 2 \log_2 3$. . . =0.9542425
 $10 = 10000000$

19. After Lord Napier had computed his first tables of logarithms it occurred to him that it would be proper to change the radix R=2.7182818 to r=10, at the same time making the logarithms of integers positive, and those of fractions negative, (art. 8.), as more conformable to the denary scale notation, and more convenient in practice. It appears that Mr Henry Briggs had also conceived the idea of changing the radix, and had computed logarithms on a plan somewhat less commodious, by making the logarithms of integers negative, and those of fractions positive, which, upon a personal communication with Lord Napier, he rejected, and finally adopted his lordship's views. He soon afterwards published the first thousand logarithms of this kind under the title of Logarithmorum Chilias Prima.

SECTION III.

Of the Trigonometrical Lines, called Sines, Tangents, &c.

20. THE Egyptians and Chaldeans began to study astronomy at a very early period. As the determination of the relations and distances of the heavenly bodies involve the mensuration of lines and angles, it was necessary to invent some method of ascertaining the value of these quantities, at least in an approximate manner, before any useful results could be obtained. Some of the more elementary propositions in geometry must have been discovered in the most remote antiquity, and the inventive genius of the Greeks filled up the general outline. The properties of geometrical figures thus acquired, would, without doubt, be applied to the mensuration of several magnitudes, and the distances of various points in space. About six hundred years before the Christian era, Thales measured the heights of the pyramids in Egypt by means of their shadows; a method which depends upon the proportionality of the sides of similar triangles. This simple property forms the basis of modern trigonometry. If, for example, a pole or gnomon be set perpendicular to the horizontal plane, it will, in a clear day, when the sun is not vertical, cast a shadow to a given distance, while any other high object, such as a steeple near, it will do the same. If straight lines be conceived to be drawn from the top of these objects to the extremity of each of their shadows, it is evident that, unless they are very distant, by this means triangles nearly similar will be formed, whose sides are proportional; that is, as the shadow of the gnomon is to its height so is the shadow of the object to its height. Now, suppose the length of the shadow of the gnomon to be made the radius with which an arc of a circle is described commencing at the bottom of the gnomon, and, as will be afterwards explained, measuring the angle between the horizontal line and the line from the extremity of the shadow to the top of the gnomon, that gnomon will, by the principles of geometry be a tangent to the circle. Whence the former proportion becomes as the radius is to the tangent of the angle of elevation, so is the length of the shadow of the object to its height. It would thus require the length of the shadow of the pole or gnomon to be measured each time any height was determined. This, however, might be avoided by having the measure of a set of triangles whose sides, to an assumed radius, and a corresponding series of angles, are previously determined by computation. By this means, in such cases, it is only necessary to measure the angle of elevation of the object, at a given point, and its distance from it, and comparing it with one of those computed triangles equiangular to it, to determine, in a manner similar to the former, the height of the object. It is obvious that the same principles may be applied to objects situated in any plane, whether vertical, horizontal, or oblique.

Several series of triangles of the kind now mentioned have been

actually computed and arranged in tables under the designation of

trigonometrical tables.

These were not accomplished at once, but were the improvements of successive ages. Hipparchus, about 150 years before the Christian era, supposed similar triangles to be inscribed in circles, and employed in his computation the chords subtending the arcs measuring them in sexagesimal parts of the radius. Nearly 300 years afterwards, Ptolomy, in his Mayaka Eurraks, recomputed the chords, but in his Analemma employs the half chords instead of the chords approaching very nearly to the use of sizes, afterwards introduced

by the Arabians.

Some notions of the tangents, secants, and versed sines, were, towards the beginning of the tenth century, entertained by the more learned Arabians. About the beginning of the fifteenth century the sciences began to be cultivated in Europe, where the greatest progress has been made. At that period Müller invented the tangents, and shortly after Maurolycus produced his table of secants. These were all in natural numbers to a given radius now generally taken at unity, and, therefore, their application was in many cases trouble-some. To remove this inconvenience as far as possible, Napier invented his logarithms, which have brought them perhaps to the last degree of perfection.

Hipparchus, who has been followed by most of the moderns, em-

Hipparchus, who has been followed by most of the moderns, employed the circle to measure angles. He supposed the whole circumference to be divided into 360 equal parts each called a degree. The degree was divided into 60 equal parts called minutes, and the minute into 60 equal parts called seconds, and the sexagesimal division was continued, though now the fractions of seconds are more commonly expressed in decimals, which are more convenient for calcula-

tion.

Whence the semicircle contains 180 degrees and the quadrant 90. As four right angles can be constituted about a point, 90 degrees must be the measure of a right angle. For the purposes of abbreviation a degree is marked with a small circle, a minute with one accent, a second with two accents, &c. Thus 57° 17' 44''.806, denotes 57 degrees, 17 minutes, 44 seconds, and .806 the decimal, whose value is 806 thousandths of a second. This, being an arc whose length is equal to the radius as will be afterwards explained, is also expressed in degrees and decimal parts of a degree, thus 57°.2957795, a mode of using it, which in some cases has its advantages.

The number of these parts, in either case, contained in the arc between the lines constituting the angle, of which arc the angular point is the centre, indicates the measure of that angle accordingly.

Hence, if to any number expressed in sexagesimal degrees oneninth of itself be added, the sum will be the same number expressed in the centesimal degrees; and if from any number expressed in centesimal degrees one-tenth of itself be subtracted, the remainders will be the same number expressed in sexagesimal degrees.

The French have lately adopted the centesimal division, which, in many cases, is preferable to the sexagesimal. The whole circle is divided into 400 degrees, each degree into 100 minutes, and the centesimal division is continued. Hence the semicircle contains 200 degrees, the quadrant 100, and the ratio of the centesimal to the sexage-aimal is as 9 to 10.

To convert sexagesimal degrees into centesimal add \(\frac{1}{2}\) of the arc to itself. The converse is effected by subtracting \(\frac{1}{2}\) of the arc from itself.

SA JURY DROWN AS

DEFINITIONS.

21. If two straight lines intersect one another in the centre of a circle, the arc of the circumference intercepted between them is called the measure of the contained angle, whatever be the radius of the circle, since the arcs are proportional to their radii. Thus, the arc AB or A'B', is the measure of the angle ACB, and is expressed in degrees, &c.

22. The complement of an arc is its difference from a quadrant, its supplement, its difference from a semicircle, and its explement, its defect from the

whole circumference. Thus if AB be any arc, then BD is the complement, BE the supplement, and BDEFA the explement.

The same thing holds with regard to the angles of which the arcs are the measures, that is, if ACB be any angle, BCD its difference from a right angle is called the complement, BCE the supplement to two right angles, and BCA, measured by the arc BDEFA, the explement or difference from four right angles.

23. The sine of an arc, or of an angle of which the arc is the measure, is a perpendicular let fall from one of its extremities upon a radius or diameter passing through the other.

24. The versed sine or versine of an arc is that part of the diameter

intercepted between its sine and the circumference.

25. The tangent of an arc is a perpendicular to the extremity of the radius at one end of the arc, and limited by a straight line drawn from the centre passing through the other.

26. The secant of an arc is the straight line drawn from the cen-

tre to the extremity of the tangent.

27. It is usual to express the sine, tangent, and secant of the complement of an arc by the abbreviated terms cosine, cotangent, and cosecant.

28. Let ACDE be a circle of which the diameters AD and CE are at right angles to one another.

Take any arc AB, produce the radius OB, and draw BG, AK perpendicular to AO or AD, and HB, CI perpendicular to CE; then BG is the D sine, BH or GO the cosine, AG the versine, CH the coversine, DG the suversine, and HE the sucoversine of the arc AB. Also of that arc AK is the tan-



gent, CI the cotangent, OK the secant, and OI the cosecant.

29. Since the diameter which bisects an arc, also bisects the chord of that arc at right angles, therefore, the sine of an arc is equal to half the chord of twice the arc. Thus BG=\frac{1}{2} BF=half the chord of the arc BAF, the double of the arc AB.

30. In the right-angled triangle OGB, BG²+OG²=OB², that is, the squares of the sine and cosine are together equal to the square

of the radius.

31. The triangle OGB being similar to OAK, OG: GB:: OA: AK, or the cosine of an arc is to the sine as radius is to the tangent.

32. Also the triangles OGB, OAK being similar, as before, OG: OB:: OA: OK, the radius is a mean proportional between the cosine and the secant.

33. Since DG: GB:: GB: GA, it follows that the sine is a mean

proportional between the versine and suversine.

34. Again, AD: AB: AB: AG, or the chord of an arc is a mean proportional between the diameter and versine.

Cor.—Since AB²=AD. AG, then, because AD is constant, AB² varies as AG, or (4 AB)² or AG, that is, the square of the sine varies directly as the versine, or inversely as the cosine, of twice the arc.

35. The triangles OAK and ICO are similar, therefore AR: AO::
OC:CI; consequently the radius is a mean proportional between

the tangent and cotangent of an arc.

36. In the application of algebra to geometry, where the trigonometrical lines are employed, it is necessary to trace their changes in the several quadrants of the circle, since it is obvious that the same

lines treated of above, may be applied to each. In the first quadrant AC, if the sine BG and cosine GO be supposed positive, then the sine B'G' on the same side of the diameter AA', and in the same direction, still remains positive; but the cosine OG' having changed its position with respect to the centre O, or diameter CC', becomes negative. In the third quadrant, the cosine AG' and sine G'B", having both changed their positions, are both negative. In the fourth quadrant, the cosine K

having resumed its original position, OG is now positive, while the sine UB", remaining as in the third quadrant, is negetise. The tangents and secants depending upon the sines and cosines have their

signs determined accordingly.

From article 30, to 35 and inclusive, R being radius, &c. we obtain

	-	•		_
l. sin.	$= (R^{2} - \cos^{2})^{\frac{1}{2}}$	7. tan.	=	cos.
% cos.	$= (R^s - \sin^s)^{\frac{1}{2}}$	8. cot.	=	$\frac{8 \times \cos}{\sin}$.
3. tan.	$=(\sec^2-\mathbf{R}^2)^{\frac{1}{2}}$	9. sec.	±	R*
4. cot.	$=(\operatorname{cosec.}^{2}-\mathbf{R}^{2})^{\frac{1}{2}}$	10. cosec.	=	R*
5. sec.	$= (R^2 + \tan^2)^{\frac{1}{2}}$	11. versine	= _F	
6. cosec.	$= (R^2 + \cot^2)^{\frac{1}{2}}$	12. covers.		
	If radius be supposed unity,	then		
1. sin.	$=(1-\cos^2)^{\frac{1}{2}}$	7. tan.	=	ein.
2. cos.	$= (1-\sin^2)^{\frac{1}{2}}$	8. cot.	=	cos.
3. tan.	= (sec. 2—1)3	9. šec.	=	l cos.
4. cot.	$=(\csc^2-1)^{\frac{1}{2}}$	10. cosec.		$\frac{1}{\sin}$.
5. sec.	$=(1+\tan^g)$	11. versine	=1	sin. •
6. cosec.	$= (1 + \cot^2 j^2)$	12. covers.		

[•] In the above wood-cut, B" has been omitted near I", which may easily be supplied by the pen.

37. Now, since (7) $\tan = \frac{\sin}{\cos}$, then it follows from the principles of algebra, that when the signs of the sine and cosine are like, the sign of the tangent is positive, and when unlike, the sign of the tangent is negative. In like manner, the signs of the cotangent, secant, and cosecant may be determined from formulas (8), (9), and 10).

Table of the Signs of Trignometrical Lines.

Q	nadrants.	, Sine.	Cosine.	Tangent.	Cotangent.	Secant.	Cosecant.
1	5 9	+	+	W + -	13 42 200	not a	and not of
	6 10	4	-1-3	William II I	A Designation of	Diversity.	+ >
	7 11		11/1-	10 to 14	A 1+41111	The last	drive see
4	8 12, &c.	700	1+60	diam'r.	STATE OF THE PARTY OF	m+10	ano in or.

Of the Multiples and Powers of Arcs.

38. In most treatises on geometry, such as Leslie's, Legendre's, &c. the elementary propositions containing the principles of trigonometry are also given. It is therefore unnecessary to repeat them here, as it only puts the student to the expense of purchasing the same things in two or three different works. We shall only give a few of the results most generally useful, referring to those works on geometry and trigonometry where the requisite information may be obtained.*

If a and b are two given arcs of a circle of which the radius is

unity, then

sin.
$$(a+b)$$
=sin. a cos. b +sin. b cos. a . (1) cos. $(a+b)$ =cos. a cos. b —sin. a sin. b . (2) sin. $(a-b)$ =sin. a cos. b —sin. b cos. a . (3) cos. $(a-b)$ =cos. a cos. a +sin. b sin. a . (4)

If we divide these equations, the one by the other in succession, that is, (1) by (2), and (3) by (4), then

$$\tan (a+b) = \frac{\sin a \cos b + \sin b \cos a}{\cos a \cos b - \sin a \sin b}$$
 (5)

$$\tan (a+b) = \frac{\sin a \cos b + \sin b \cos a}{\cos a \cos b - \sin a \sin b}$$

$$\tan (a-b) = \frac{\sin a \cos b - \sin b \sin a}{\cos a \cos b + \sin b \sin a}$$
(5)

Dividing the two terms of the second numbers by cos. a cos. b, and substituting tan. a and tan. b for their values in terms of the sine and cosine

tan.
$$(a+b)$$
— $\frac{\tan a + \tan b}{1 - \tan a + \tan b}$. (7)

$$\tan (a-b) = \frac{\tan a - \tan b}{1 + \tan a \tan b}$$
 (8)

expressions which give the tangent of the sum and of the difference of two arcs in terms of the tangents of these arcs.

If we make a=b in the preceding formulæ, they give

$$\sin 2 a = 2 \sin a \cos a,$$
 (9)
 $\cos 2 a = \cos^2 a = \sin^2 a$ (10)

$$\tan 2 a = \frac{2 \tan a}{1 - \tan^2 a}$$
 . . . (11)

^{*} Those we would more particularly recommend are the treatises of Gregory, Woodhouse, Lardner, and Cagnoli. Dr Kelly's Spherics is a very good treatise for teaching the practice of the stereographic projection of spherical triangles.

(23)

expressions which give the sine, cosine, and tangent of twice the arc in terms of the sine, cosine, and tangent of the simple arc.

39. Returning to equations (1), (2), &c. we have by addition and subtraction

$$\sin \cdot (a+b) + \sin \cdot (a-b) = 2 \sin \cdot a \cos \cdot b$$
 (12)
 $\cos \cdot (a+b+\cos \cdot (a-b) = 2 \cos \cdot a \cos \cdot b$ (13)
 $\sin \cdot (a+b) - \sin \cdot (a-b) = 2 \sin \cdot b \cos \cdot a$ (14)

$$\sin \cdot (a+b) - \sin \cdot (a-b) = 2 \sin \cdot b \cos \cdot a$$
 (14)
 $\cos \cdot (a-b) = \cos \cdot (a+b) = 2 \sin \cdot a \sin \cdot b$ (15)

Let (a+b)=u, and (a-b)=v, then by addition and subtraction $a=\frac{1}{2}(u+v)$, $b=\frac{1}{2}(u-v)$, consequently the preceding formulae become

sin.
$$u + \sin v = 2 \sin \frac{1}{2} (u + v) \cos \frac{1}{2} (u - v)$$
 . (16)
sin. $u - \sin v = 2 \cos \frac{1}{2} (u - v) \cos \frac{1}{2} (u + v)$. (17)
cos. $u + \cos v = 2 \cos \frac{1}{2} (u + v) \cos \frac{1}{2} (u - v)$. (18)
cos. $v - \cos u = 2 \sin \frac{1}{2} (u + v) \sin \frac{1}{2} (u - v)$. (19)

expressions which serve to transform the sum or the difference of the sine or cosine into the product, and thus to unite the two terms into one.

If we divide formula (16) by formula (17) they give

$$\frac{\sin u + \sin v}{\sin u - \sin v} = \frac{\tan \frac{1}{2}(u + v)}{\tan \frac{1}{2}(u - v)} \qquad (20)$$

If we multiply these equations member by member, observing to substitute sin. 2 a=2 sin. a cos. a, formula (9), then

$$\sin^2 u - \sin^2 v = \sin \cdot (u+v) \cos \cdot (u+v)$$
 $\cos^2 v - \cos^2 u = \sin \cdot (u+v) \cos \cdot (u+v)$
(21)

Since sin. 2 $a=2 \sin a \cos a$, and cos. 2 $a=\cos^a a - \sin^a a$.

The second of these equations may be put under the two following forms:

cos.
$$2a=1-2\sin^2 a$$
, and cos. $2a=2\cos^2 a-1$
whence $\sin^2 a = \frac{1-\cos 2a}{2}$, and $\cos^2 a = \frac{1+\cos 2a}{2}$. (22)

These expressions are used when, for the squares of the sine and cosine, the first power of the cosine of the double arc is substituted.

40. Let 2a = u, then $a = \frac{1}{2}u$ formula (22), these formulæ become $\sin^{2}\frac{1}{2}u = \frac{1-\cos u}{2}, \cos^{2}\frac{1}{2}u = \frac{1+\cos u}{2}$

and dividing each corresponding number successively, they give

$$\tan^{g} \frac{1 - \cos u}{1 + \cos u} \qquad (24)$$

If b in formulæ (1), (2) be made 2a, 3a, &c. we may obtain multiple arcs thus:

sin.
$$3a$$
=sin. a cos. $2a$ +sin. $2a$ cos. a cos. $3a$ =cos. a cos. $2a$ —sin. a sin. $2a$

Substituting for sin. 2 a and cos. 2 a, their values, they become

sin.
$$3 a = 3 \sin a \cos^2 a - \sin^3 a$$
 (26 cos. $3 a = -3 \cos a \sin a + \cos^3 a$ (27)

These may be put under the form

$$\sin 3 a = \cos^5 a (3 \tan a - \tan^5 a)$$

 $\cos 3 a = \cos^5 a (1 - 3 \tan^9 a)$

In general n being any integer,

$$\sin n \, a = \cos^{n} \, a \, \left\{ n \, \tan . \, a - \frac{n \, (n-1) \cdot (n-2)}{1 \cdot 2 \cdot 3} \tan^{5} \, a + \frac{n \cdot (n-1) \cdot (n-2) \cdot (n-3) \cdot (n-4)}{1 \cdot 2 \cdot 3 \cdot 4 \cdot 5} \tan^{5} \, a \dots \&c. \right\}$$
(29)

$$\cos, na = \cos. na \left\{ 1 - \frac{n(n-1)}{1 \cdot 2} \tan^{2} a + \frac{n(n-1)(n-2)(n-3)}{1 \cdot 2 \cdot 3 \cdot 4} \tan^{4} a, &c. \right\} (29)$$

The coefficients of the different terms are those of the nth power of the binomial, whence these series may be collected under the following form:

sin.
$$n = \frac{1}{2\sqrt{-1}} \left\{ \cos a + \sqrt{-1} \sin a \right\}^n \frac{1}{2\sqrt{-1}} \left\{ \cos a - \sqrt{-1} \sin a \right\}^n (30)$$

cos. $n = \frac{1}{2} \left\{ \cos a + \sqrt{-1} \sin a \right\}^n + \frac{1}{2} \left\{ \cos a - \sqrt{-1} \sin a \right\}^n (31)$

cos. $na = \frac{1}{2} \{\cos a + \sqrt{-1} \sin a \}^n + \frac{1}{2} \{\cos a - \sqrt{-1} \sin a \}^n (31)$ These formulæ, by development, will give the two foregoing series, and are thus easily verified.

41. It may be shown* that if x represent any arc

sin.
$$x = x - \frac{x^5}{1.2.3} + \frac{x^5}{1.2.3.45} - \frac{x^7}{1.2.3.45.6.7} + , &c.$$
 (32)
cos. $x = 1 - \frac{x^2}{1.2} + \frac{x^4}{1.2.3.4} - \frac{x^6}{1.2.3.45.6} + , &c.$

In these expressions the arc x is supposed to be divided by the radius, which is here taken for the unit of length, and consequently if we wish to restore it we must write $\frac{x}{r}$ in place of x and $\frac{\sin x}{r}$ instead of $\sin x$ in the two members of these equations.

These formulæ might be carried much farther than can be introduced into this place. Most of them may be seen by consulting the books already referred to, but above all the analysis infinitorum of Euler.

Tables of Multiples and Powers of Arcs.

1. 2.
$$\sin a = s, s \begin{cases} \text{being the sine of the force } \\ \text{arc } a. \end{cases} \cos a = (1-s^2)$$

$$\sin 2 a = 2s (1-\sin^2) \frac{1}{2} \cos 2 a = 1-2s^2$$

$$\sin 3 a = 3s-4s^5 \cos 3 a = (1-4s^2) (1-s^2) \frac{1}{2}$$

$$\sin 4 a = (4s-8s^5) (1-s^2) \frac{1}{2} \cos 4 a = 1-8s^2+8s^4$$

$$\sin 5 a = 16s^5-20s^5+5s, &c. \cos 5 a = (1-12s^2+16s^4) (1-s^2 \frac{1}{2}) &c. \\ 3. \cot a = t, t \begin{cases} \text{being the tangent } a. \end{cases} \cot a = \cot.$$

$$\tan a = t, t \begin{cases} \text{being the tangent } a. \end{cases} \cot a = \cot.$$

$$\tan 2 a = \frac{2t}{1-t^2} \cot 2 a = \frac{\cot x^2-1}{2 \cot x}$$

$$\tan 3 a = \frac{3t-t^3}{1-3t^2} \cot 3 a = \frac{\cot x^3-3}{3 \cot x^3-1}$$

$$\tan 4 a = \frac{4t-4t^5}{1-6t^2+t^4} \cot 4 a = \frac{\cot x^4-6\cot x^2+1}{4\cot x^3-4\cot x^3-1}$$

$$\tan 5 a = \frac{5t-10t^5+t^5}{1-10t^2+5t^4}, &c. \cot 5 a = \frac{\cot x^5-10\cot x^5+5\cot x^5}{5\cot x^4-10\cot x^2+1}, &c.$$

Woodhouse's Trigonometry, third edition, page 245—Gregory, page 42 and 50.

5. cos. a = cos. a
2 sin. a = 1 - cos. 2a
4 sin. a = 3 sin. a - sin. 3 a

5. cos. a = cos. a
2 cos. a = 1 + cos. 2 a
4 cos. 3 a = 3 cos. a + cos. 3 a

 $8 \sin^4 a = 3 - 4 \cos^2 a + \cos^4 a = 3 + 4 \cos^2 a + \cos^4 a$

42. Having given a short abstract of the more useful formulæ relative to multiples and powers of arcs, we shall now proceed to shew the method of constructing the tables of sines, tangents, &c.

When the radius of a circle is unity, the semicircumference is 3.1415926536 nearly. Now there are 180° or 10800′ in a semicircle, consequently, if the former be divided by the latter, the result will be 0.0002908882, the measure of an arc of one minute, which, as the arc is so small, may be considered its sine.

Now, art. 35. 2, $\cos = (1 - \sin^2)^2$ consequently cos. 1' = 0.999999577. If these values are substituted in formulas, (32), and (33), art. 41 the sines and cosines may be obtained through the whole quadrant.

Thus let the arc a=1', and, therefore, sin. x=0.0002908882. Let $a=5^{\circ}$, then $\frac{5\times3.1415926536}{180}=0.08726646$ the length of a or x, and

$$x = +0.08726646$$

$$-\frac{x^5}{1.23} = -0.00011076$$

$$+\frac{x^5}{1.23.4.5} = +0.00000004$$

therefore, $x = \frac{x^5}{1.2.3} + \frac{x^5}{1.2.3.4.5}$, &c.=0.08715574= the natural sine of 5°, the logarithm of which is 8.740206, the log. sine the same arc. This method is easy when the arc is small, as the series then converges very rapidly, but it is rather laborious when the arc is large, in which case recourse must be had to other methods depending upon the properties of multiple arcs, as may be seen in most of our treatises on trigonometry.

As the sines are computed, the cosines of the same arcs may be found from art. 41, formula (33), or from art. 35, formula (2), the tangents and cotangents, from formula (7) and (8), and the secants and cosecants from (9) and 10).

SECTION IV.

Of the application of Tables of Sines, Tangents, Secants, &c. to plane Trigonometry.

CABE I.

43. In any plane triangle it is shewn in our usual treatises, that the sides are proportional to the sines of their opposite angles, or

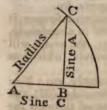
The sine of any one angle,
Is to the sine of another angle;
As the side opposite to the first,
Is to the side opposite to the second.

These terms may be taken alternately, inversely, &c.

44. When one of the angles is a right angle, then the preceding rule may either be applied, or a modification of it derived from the properties which are peculiar to right-angled triangles.

In right-angled triangles, it is usual to call that side subtending the right angle the hypotenuse, and the other sides which contain the right angle the legs, or the one the base and the other the perpendi-

Then if one of the sides of any triangle ABC, be assumed equal to the radius, the names of the other sides must be determined by art. 28, as follows:-







The names of the sides being thus known when three of the parts of a triangle including a side are given, the rest may be found by the following rules:-

> I .- To find a side. As the name of the given side, Is to the name of the required side; So is the given side, To the required side.

II .- To find an angle. As the side made radius, Is to the other given side, So is radius, To the name of this side.

Any side may be made radius to find a side, but one of the given

sides must be made radius to find an angle.

In the solution of plane triangles, it must be recollected that all the angles in any triangle are together equal to two right angles, or 180°. Whence if two of the angles are given, the other may be found by subtracting their sum from 180°; when one angle is given the sum of the other two may be found by subtracting it from 180°; and if one be right or 90°, the sum of the other two is also 90°, and the one is the complement of the other.

45. In a plane triangle when the two sides and contained angle are given.

I. As the sum of the given sides,

Is to their difference;

So is the tangent of half the sum of the opposite angles,

To the tangent of half their difference.

Half the difference added to half the sum of those angles gives the greater, and subtracted from half the sum gives the less.

All the angles being now known, the third side may be found by

the rules in case I.

Or, after having found half the sum and half the difference of the angles, the remaining side may be found without determining the actual angles, as proposed by Thacker in 1743, and recommended by Professor Wallace, in the Edinburgh Philosophical Transactions, in the following manner:

As the sine of half the difference of the opposite angles,
 Is to the sine of half their sum,

So is the difference of the containing sides;

To the remaining side; or,

III. As the cosine of half the difference of the opposite angles,

Is to the cosine of half their sum; So is the sum of the containing sides

To the remaining side.

These two methods may be used as a verification to each other, and will be found somewhat more easy in practice than the first method, as several of the quantities may be taken out from the tri-

gonometrical tables at the same time.

Should the sides come out in logarithms from some previous operation, then Gauss' table for finding the logarithm of the sum and difference of numbers from their logarithms, without first determining the natural numbers themselves, would be some advantage, though it was not thought sufficient to warrant an insertion of it among the tables.

The following method of resolving this problem is convenient, par-

ticularly when the logarithms of the sides are given.

IV. From the logarithm of the greater of the two given sides, having its index increased by 10, subtract the logarithm of the less side, the remainder will be the logarithm tangent of an arc, from which, 45° being subtracted, there will be obtained a remainder. To the logarithm tangent of this remainder add the log, tangent of half the sum of the opposite angles, the sum, rejecting 10 in the index, will be the log, tangent of half their difference, from which the angles themselves may be found.

CASE III.

46. In any plane triangle, when the three sides are given,

I. As the base

Is to the sum of the sides;

So is the difference of the sides

To the difference of the segments of the base made by a perpendicular upon it, or upon it produced from the opposite angle.

It may perhaps be convenient to call the longest side the base,

in order that the perpendicular may fall within the triangle.

When the three sides of a triangle are given, the difference of the segments of the base may thus be found. Then half the difference added to half the sum, that is, to half the base, will give the greater segment adjacent to the greater side; and half the difference taken from half the sum will give the less. From these the angles may be found by Rule II. § (44).

II. In a plane triangle, as the rectangle under any two sides, is to the rectangle under the excesses of the semiperimeter above those sides; so is the square of the radius to the square of the sine of half their contained angle, as shown in Leslie's Geometry. In practice, this rule, when logarithms are employed, may be stated as follows:

To the arithmetical complements of the logarithms of the two sides containing the required angle, add the logarithms of the differences between those sides and half the sum of the three sides, then half the sum of these four logarithms will be the log. sine of half the required angle.

III. To the arithmetical complements of the sides containing the required angle, add the logarithm of half the sum of the three sides,

and the logarithm of the difference between this half sum and the side opposite the required angle; half the sum of these four loga-

rithms will be the log. cosine of half the required angle.

IV. To the arithmetical complement of the logarithm of half the sum of the three sides, add the arithmetical complement of the difference between half the sum of the three sides and the side opposite the required angle, and the logarithms of the differences between that half sum and the sides containing the required angle; half the sum of those four logarithms will be the log. tangent of half the required angle.

It may be remarked that these three last rules will, in general, be the most commodious in practice, though, in particular cases, each may have its peculiar advantage when great accuracy is required.

When the required angle does not exceed 90°, Rule II. may be used, when it does, Rule III. may be employed; and in either case Rule IV. will give correct solutions. These observations depend upon the variation of the trigonometrical lines in certain parts of the circle, as, for example, near 90°, the sines vary very slowly, so that the true value of an arc cannot be obtained by our ordinary tables, while the tangents always vary by such perceptible quantities as to leave no doubt of the real value of the required arc. These remarks may be easily verified by examining any of our tables extended to six or seven places of decimals.

Of the Construction of Triangles.

47. Previous to the numerical solution of any triangle, it is generally first constructed geometrically. This is accomplished by means of what are termed mathematical instruments, consisting of scales, compasses, &c. contained in a case, at various prices, to suit the convenience of purchasers. Printed descriptions of these, as well as of many others, are to be found in Jones' edition of Adams' Geometrical and Graphical Essays.

In the construction of plane triangles the sides are taken from a scale of equal parts, and the angles are laid down by a scale of chords,

or more conveniently by a protractor.

EXAMPLES.

CASE I.

48. 1. Given the angles and hypotenuse of a right-angled triangle, to find the base and perpendicular.

Let the hypotenuse AC of the right-angled triangle ABC be 288,

and the angle A 39° 22'; it is required to find the sides AB and BC.

Construction.—In the indefinite straight line AB take any point A, and by a protractor or scale of chords, make the angle A equal to 39° 22′; from any convenient scale of equal parts take AC equal to 288, and from C draw CB, perpendicular to AB;

A C B

then ABC will be the triangle required. In order to simplify and preserve uniformity, the angles may, in general, be denoted by the capital letters A, B, C, and the opposite sides by the small letters a, b, c. The sides a and c being measured by the same scale from which b was taken, will be found to be 182.7 and 222.7.

Calculation

1. By natural numbers, § (43).

To find a.

As sin. B: sin. A:: b: a, or $a = \frac{\sin. A \times b}{\sin. B}$

1:0-634281::268: 0-634281 × 288 = 182.673=a

To find c.

And sin. B: sin. C, or cos. A:: b:c

 $1:0.773103::288:\frac{0.773103\times288}{1}=222.654=6$

2. By logarithms.

To find a.

As sin. B, or radius	10.000000
Is to sin. A 39° 22'	. 9.802282
So is <i>b</i> 288 .	. 2.459392
To a 182.673 .	. 2.261674
To fi	nd c.
As radius .	. 10.000000
Is to cos. A 39° 22'	. 9.888237
So is <i>b</i> 288 .	. 2.459392
To c 922 653	2 347690

The solutions may be varied by assuming any of the sides for radius, according to art. (44), and verified by Gunter's scales.

2. Given the angles and one side, to find the hypotenuse and the

other side.

Let the side AB be 758, and the angle C 39° 26'; to find the angle A, and the sides BC and AC.

Ans.—BC is 921.7, and AC 1193.36, and the angle A 50° 34'.

Construction.—From a scale of equal parts make AB equal to 758, the angle A 50° 34′, the complement of C, and draw BC at right angles to AB; produce AC and BC till they meet in C; then ABC is the triangle required, and a and b measured on the same scale from which c was taken will be found to be about 922 and 1193 respectively.

3. Given the hypotenuse and one side, to find the angles and other

side.

Let the hypotenuse AC be 544, and the base 464; to find the angles A, a and c, and the side BC.

Ana—The angle A is 31° 28', though C is 58° 32' and BC 284.

Construction.—Make AB equal to 464 from a scale of equal parts, and from B draw BC perpendicular to AB, then from the centre A at the distance AC equal to 544 describe an arc intersecting BC in C, join AC, and the triangle is constructed. The angle A being measured by a protractor or scale of chords, will be found to be 31° 28', consequently C is 58° 32', and the side BC 284 from the same scale by which the other sides were laid down.

4. Given the base and perpendicular, to find the angles and hypo-

tenuse.

Let the base AB be 558, and the perpendicular BC 456; required the angles A and C and the hypotenuse AC.

Ans.—A 39° 15′ 21″, and 50° 44′ 39″, and AC 720.622.

Construction.—Make AB equal to 558, and draw BC perpendicular to AB and equal to 456, join AC, and the triangle is constructed. The angle A will measure 39½, and the hypotenuse will be about 721 nearly on the scale of equal parts. The other side may be found by Euclid I. and 47, or Leslie's Geometry II. 10, and 13.

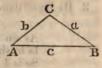
5. Given the angles and one side of an oblique-angled plane trian-

gle, to find the other sides.

In the triangle ABC, are given the side AC, 532, the angle A 38° 40′, C 92° 46′, and consequently the angle B 48° 34′; to find the sides AB and BC.

Ans.-AB 708.76, BC 443.34.

Construction.—Draw the indefinite AB, at A make the angle BAC equal to 38° 40′, and from a scale of equal parts make AC 532, at C draw CB making the angle ACB equal to 92° 46′, it will cut AB in B forming the triangle ABC which was required.



6. Given two sides, and an angle opposite one of them, to find the

other angles and the third side.

In the triangle ABC are given the side AB 274, AC 306, and the angle B 78° 13'; required the angles A and C, and the third side BC.

Ans.—The angle C is 61° 14′, the angle A 48° 33′, and the side BC 203.22.

Construction.—Make AB equal to 274, the angle B equal to 78° 13', and with an extent equal to AC, 306, intersect the line BC in

C; ABC is the triangle required.

If in this triangle the side B be greater than C, there may be two triangles formed, constituting what is called the ambiguous case, that is, it admits of two solutions, either of which answers the conditions required, unless from some known circumstances one of them must be adopted in preference to the other.

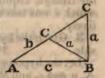
Thus in the oblique-angled triangle ABC there are given AB 318,

BC 195, and the angle A 32° 40'.

Ans.—The angle B is 61° 50' or 118° 20', the angle C is 85° 40'

or 29°, and the side AB is 360.246 or 175.15.

Construction.—Make AB equal to 318 from any convenient scale of equal parts, the angle A equal to 32° 40′, and with the centre B and distance equal to BC 195 describe an arc cutting AC in C or C′; ABC or ABC′ will be the triangle required.



CASE II.

49. Given two sides and the contained angle, to find the other

angles and the third side.

In the triangle ABC let the side AB be 920 and AC 500, and the contained angle A 36° 52′; required the angles B and C, and the third side BC.

Ans.-B is 20° 58′ 50″, C 113° 0′ 10″, and BC is 600.31.

Construction.—Make A point A make the angle AC equal to 500; join B required.	BAC equal 3	6° 52', and		C
By Calculation	on, art. 45, I		A	с В
As AB+BC 1420				3.152288
Is to AB—BC 420		•		2.623249
So is $\tan \frac{1}{2} (B+C)$	71° 34′ 10′	. •		10.477162
To tan. ½ (B—C)	41 35 10		•	0.948123
C	113 9 10			
B	29 58 50			
As sin. B 29° 58′ 5	50"	•		9.698714
Is to sin. A 36 52	0 .			9.778119
So is AB 500	·	•	٠	2.698970
To BC 600.31 Or by art. 45, II. a	nd III.	•	•	2.788375
As $\sin \frac{1}{2}$ (B—C)	41° 35′ 10″			9.822001
Is to $\sin \frac{1}{2} (B+C)$	71 34 0			9.977125
So is AB—BC	420	•	•	2.623249
To BC	600.31			2.778373

To BC 600.30 . 2.778374

The advantage of these two last methods consists in its being unnecessary to find the values of the angles C and B to determine BC, and that several of the quantities are found among the tables at the same opening of the book, and if computed both ways they are a check upon each other.

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CASE III.

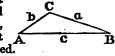
50. Given the three sides of a triangle, to find the angles.
In the triangle ABC, there are given AB 800, AC 320, and BC 562; to find the angles.

Construction.—Draw the line AB equal to 800 from a scale of equal

parts, then from the same scale take an extent equal to AC 320, and with the centre A and distance 320 describe an arc, in like manner, with the centre B and distance BC 162, intersect the former arc in C; ABC is the triangle required

As cos. ½ (B—C) 41° 35′ 10″ Is to cos. ½ (B+C) 71 34 0

So is AB + BC



the former arc in C; ABC is the triangle required.

In the solution of this question, if the angles A or B are first to be determined, then rules II. or IV. § 46, will be found most convenient and accurate; but if C be wanted first, then if great accuracy is required it would be improper to use rule II., but rule III. or IV. should be employed, so as to give the angle with all the requisite accuracy in nice operations.

INTRODUCTION.

By Calculation.

Rule II.	
AB 800 AC 320 ar. co. BC 562 art. co.	7.494850 7.250264
Sum 1682	
Half 841 1st diff. 521 log. 2d diff. 279 log.	2.716838 2.445604
Sum	19.907556
Half 64° 1′ 54″.4 sin 2	9.953778
C 128 3 48 .8	
RULE III. AB 800	
AB 800 AC 320 ar. co BC 562 ar. co	7 494850 7 250264
Sum 1682	
Half 841 log	2.924797 1.612784
Sum · · · .	19.282694
Half 64° 1′ 54″.9 cos	9.641347
C 128 3 49 .8	
RULE IV. AB 800 AC 320 BC 562 . Sum 1882	
Half 841 ar. co	7.075204 8.387216 2.716883 2.445604
Sum	20.624862
Half 64° 1′ 54″.7 tan. 2 C 128 3 49 .4	10.312431
O 180 O 30 11	

From these solutions it appears that the first and second differ about 1" from each other, while the second and last only differ 0".4.

Had the angle C been nearer 180°, the first and second solutions might perhaps have differed more considerably, while the second and third would have agreed more nearly. Hence it is clear that the proper rules, when great nicety is required, must be chosen according to the nature of the angle.

EXAMPLES FOR EXERCISE.

51. 1. What angle will one foot subtend at the distance of fifty

miles? Ans.— $0^{\prime\prime}$.78.

2. The hypotenuse of a right-angled triangle being 5472 feet, and the acute angle adjacent to the base, 29° 50′ 58″, what are the base and perpendicular?

Ans.—The base 4746.064, and the perpendicular, 2723.538.

3. If the base of a plane triangle be 384, and the other two sides 288 and 192, what is the length of the perpendicular upon the base, and the length of the segments of the base made by a line bisecting the vertical angle?

Ans.—Perp. 139.4274, segments 230.4 and 153.6.

4. There are three towns, A, B, C, so situated that the bearing of B and C from A forms an angle double that of A and C from B, and that of A and B from C double that of A and C from B, or the angle opposite b is double of that opposite c, and the circuit round all the three is just one hundred miles; what are their relalative distances from each other in succession?

Ans.—19.8073, 35.6861, and 44.5066 miles.

5. In the right-angled triangle right-angled at B, given the base AB 70, and the sum of the hypotenuse and perpendicular AC and BC 200, to find the hypotenuse and perpendicular, and the remaining angles?

Ans.—The angle ACB is 37° 16', AAC 51° 24', and AC 112.52,

and BC 87.68.

6. In an oblique-angled triangle ABC let the side BC be 532, the angle BAC 110° 30′, and the sum of the sides AB, AC 637; required the angles C and B, and the sides AB and AC?

Ans.—The angle C is 45° 5', B 24° 25', and the side AB 402.3 and

AC 234.7.

7. In the oblique-angled triangle ABC, let the side BC be 250, the angle BAC 96° 50′, also the difference between the sides AB and AC 106; required the angles ACB and ABC, together with the sides AB and AC′?

Ans.—ACB is 57° 55', ABC 25° 15', and AB 213.4, and AC 107.4.

8. Given the base 214, the vertical angle 49° 16', and the sum of the other two sides 459; to find the sides and remaining angles?

Ans.—The acute angle is 33° 44′ 48″, the obtuse angle is 91° 59′ 12″, the side opposite the acute angle is 176.75, and the side opposite the obtuse angle is 282.245.

9. Given one of the sides 252, the opposite angle 20° 46', and the excess of the base above the remaining side 86; to find the remaining

angles and sides.

ľ

Ans.—The vertical angle is 94° 22′ 28″, the remaining angle is

55° 51′ 32″, the base is 507.08, and the other side 421.08.

10. Given the base 1514, the vertical angle 75° 24′ 50″, and the perpendicular 972.41; required the remaining sides and angles.

Ans.—The sides are 1298 and 1172, and the angles are 56° 4′ 5°

and 48° 31′ 5" respectively.

52. The various sailings in navigation are only the applications of

trigonometry in particular circumstances.

The course is the angle formed between the meridian and the point on which the ship sails, the distance is the hypotenuse, and the difference of latitude and departure, the legs of a right-angled triangle.

Thus let AB represent the meridian; then if a ship sails north-easterly, the line AC is drawn to D the right-hand, making an angle BAC equal to the course, and AC represents the distance, AB, the difference of latitude, and BC the departure. If she sails north-westerly, then BAD is supposed. to be the angle of course shown by the compass, and is generally in points and quarter points, AD the G distance,-AB the difference of latitude and BD

the departure. Again, if the ship sail south easterly, AF is the distance, AE the different latitude, EF the departure, and FAE the course. If, however, AE' be the meridian difference of latitude, E'F' is the difference of longitude, E'AF' is the course, and AF is still the distance. Hence the course and distance between two places can be found, by this method, when their latitudes and longitudes are known. This is commonly called Mercator's sailing.

Parallel, middle latitude, and oblique sailings, may readily be explained on similar principles, though these can only be completely

discussed in regular treatises on navigation.

See Mackay's, Norie's, Riddle's, Inman's, or Robertson's Navigation.

EXAMPLES.

1. A ship from latitude 47° 30' N, sails S. W. by S. 98 miles; what latitude is she in, and what departure has she made?

Ans.—Difference of latitude 81.48, departure 54.45 miles, and the

latitude come to 46° 9' N.

- 2. A ship from latitude 48° 32' N. sails between north and west till her departure is 54 miles, and then finds herself in latitude 49° 54' N.; what course did she steer, and what distance did she run? Ans.—Course 32° 22' N. W., and distance 98.18 miles.
- 3. Coasting along shore I saw a cape bearing N. E. by N. After standing N. W. 20 miles the same cape bore E. N. E. Required the distance of the ship at each station.

Ans.—From the first station 33.26, and from the second 35.31

miles.

4. Required the course and distance from Caithness point in Scotland, in latitude 58° 46' N. longitude 3° 17' W., to New York in North America, in latitude 41° 5′ N. and longitude 74° 15′ W.

Ans.—Course 68° 32′ or W. S. W. nearly, and distance 2899.2

miles.

5. A ship from latitude 60° 24' N. and longitude 43° W. sails between South and West till she is in latitude 56° 30' N., and has made 226 miles of departure; required her course, distance, and longitude?

Ans.—Course S. E. nearly, distance 325.4 miles, and the longitude

of the ship 35° 47' W.

6. Required the course and distance between the Isle of May, in lati-

tude 56° 12' N. longitude 2° 33' W., and Heligoland in latitude 54° 12' N. longitude 7° 53' E?

Ans.—Course S. 71° 27' E. and Dist. 377 miles.

7. A ship from the Isle of May sailed on the following true courses; required her situation?

Courses.	Dist.	Diff.	Lat.	Depar	rture.
		N.	S.	E.	W.
S. E. S. S. E. N. E. S. E. <i>b</i> . S.	40 50 20 60	14.1	28.3 46.2 49.9	28.3 19.1 14.1 33.3 184.8	
E. S. E. W. b. S. N. N. W. N. E. b. N. E. S. E. \(\frac{3}{4} \) E.	200 15 20 76 60	18.5 63.2	76.5 2.9 14.6	42.2 58.2	14.7 7.7
S. 711 E.	378	95.8	218.4 95.8	380.0 22.4	22.4
			122.6	357.6	}
Diff. of Lat. Lat. left		. 50	2° 3′S. 3 12 N.		
Lat. in		54	9 N.		

Hence the ship is about 3 miles south of Heligoland light.

SECTION V.

Application of Plane Trigonometry to the Mensuration of Heights and Distances.

53. One of the most important applications of plane trigonometry is the mensuration of heights and distances. The data are some of the sides and angles of a triangle. The sides are measured by rods, lines, tapes, or chains, constructed according to the degree of accuracy required; and the angles are measured by some angular instrument, such as the quadrant, sextant, reflecting circle, repeating circle, or theodolite. The repeating theodolite is perhaps, in general, the most convenient of all for taking the necessary angles, and the chain, properly constructed, the best for measuring the side called the base, though, to military engineers, the small pocket circular box-sextant, or semicircle, as improved by Sir Howard Douglas, will be found highly useful, when accompanied by the box-measuring tape. One of Schmalcalder's surveying compasses will also be found very commodious in military and nautical surveying. A complete description of these instruments would far exceed our limits, and their use is best

Those who wish for written descriptions may consult Jones' edition of Adam's Geometrical and Graphical Essays, already mentioned, Biot's Traits d'Astronomie Physique, Delambre's Astronomie, Base du Systeme Metrique, Woodhouse's, Vinco's, and Pearson's Treatises of Astronomy.

learnt under the superintendence of a master. In general, it may be remarked, that an allowance must be made for the height of the eye above the horizontal plane; and when the base above-mentioned is inclined to the horizon, it must be reduced to it according to the given inclination, though in nice operations the base is selected so as to be, if not exactly, at least nearly level. Then, from a little attention, by driving in stakes at moderate distances, and levelling their tops, on which deals properly prepared are laid, an exact horizontal line may be obtained. This truly level line is to be most carefully measured, allowance being made for the contraction or expansion of the materials of which the chain is composed according to the state of the thermometer; in nice operations reduced to the level of the sea; and such other precautions as the nature of the case may require must be observed, in order to insure the greatest possible accuracy; many examples of which may be seen in the Trigonometrical Survey of the British islands under the direction of the Board of Ord-A number of the more useful problems connected with trigonometrical surveying may be seen in the third volume of Hutton's Course of Mathematics by Dr O. Gregory, in Baron Zach's Work on the Attraction of Mountains, in the Base du Systeme de Metrique Decimal, and in Piussant's Geodesie.

EXAMPLE I.

To determine the distance of a tower, inaccessible by reason of an intervening river, I measured, on a horizontal plane, the base AB, 500 yards, and at each end took the angle included between the

other end and the tower, which were 50° 56' and 75° 10' respectively: What is the distance of the tower from each end of the base?

In the annexed figure,

AB = 500

 $CAB = 50^{\circ} 56^{\circ}$

CBA = 75° 10', and consequently Angle $C = 180^{\circ} - (A + B) = 53^{\circ} 54'$

Hence, sin. C 53º 54 9.907406 Is to AB 500 2.698970 So is sin. A 50° 56' 9.890093

To BC 480.46 2.681657 So is sin. B 75° 10'

9.985280

To AC 590.2

2.776844

9.907406

2.698970

The perpendicular or nearest distance C d may, if required, be easily found thus:

As radius 10.000000 Is to AC 598 2 2.776844 So is sin. A 50° 56' 9.890093

2.666937

To Cd 464.45

These distances might have been determined without an instrument to measure the angles. Thus, suppose that, in the

[•] There are several methods of approximating to the heights of objects by means of mirrors, shadows, staffs, geometrical squares, and Gunter's quadrants; but as they are seldom used where much accuracy is required, they are omitted here.

continuation of the base AB, and the lines CA, CB, the four distances, AD, AE, BF, BG, were taken all equal to 100 feet, and DE measured 86, and FG 122 feet, the respective chords, to a radius of 180 feet, of the exterior angles DAE, FBG, which are equal to their vertical interior angles CAB, CBA. Now, since half the chord is the sine of half the angle, we have $\frac{100}{100} = \frac{43}{100} = \frac{1}{100} = \frac{1}{100}$

Note 1.—The number 100 was chosen for the sake of simplicity; but any other convenient number may be adopted, taking care to divide

half the measure of the chord by it.

Note 2.—The same thing may be accomplished when the sides of the triangles bear any proportion to each other, by finding from them the angles DAE, FBG. Also the supplements EAB, ABG of the original angles may be found in the same manner, or otherwise by joining AG and BE.

EXAMPLE II.

Wanting to know the breadth of a river, I measured 100 yards in a straight line by the side of it; and at each end of this line I found the angles subtended by the other end, and a tree close by the opposite side, to be 53° and 79° 12′; what is its perpendicular breadth?

Ans.—105.89.

EXAMPLE III.

In order to find the distance between two trees A and B, which could not be directly measured on account of a pool of water which occupied the intermediate space, I measured the distance of each from a third object C, which were 588 and 672 yards respectively, and then at C took the angle ACB between the two trees 55° 40. Required their distance.

180° 0'
Angle C 55 40

A+B 124 20

1 (A+B 62 10

As BC+AC 1260

Is to BC—AC 84

1.924273

So is tan. \(\frac{1}{2}(A+B)62^\circ 10'\) 0" 10.277379



To tan. 🖠	(A–	-B)	7	11	53	
Angle A			69	21	53	
Angle B			54	58	7	
As sin. A	699	21'	53"			9.971203
Is to BC						2.827369
So is sin. C	55	4 0	0			9.916859
To AB 592	2.96				_	2.773025

EXAMPLE IV.

In the trigonometrical survey of Britain, Colonel Mudge found, from computations depending on former operations, that the logarithm of the number expressing the distance between Cheviot and Cross Fell in feet was 5.4654017, and between Cheviot and Wisp Hill 5.2672278, and the angle contained by these, corrected for

In some of the examples the computations in proportion are performed by compaging the sines of the angles with the sides, a method sometimes more easy to beginners.

spherical excess, was 53° 30′ 18″. Required the other angles, and the distance between Wisp Hill and Cross Fell, without first finding the value of the given sides in natural numbers.

Ans.—The angle at Wisp Hill is 87° 14′ 4″.

Cross Fell 39 15 46

The distance of Wisp Hill from Cross Fell 235018.6 feet.

EXAMPLE V.

In order to determine the height of a tower, I measured in a direct line AB 366 feet on a horizontal plane. I then took the angle Cab 37° 30′, the height Aa of my instrument being 5 feet. Required BC the height of the tower.

Ans. bC =280.84. Add Aa 5.00.

Height BC =285.84.



Walking along the side of a river, I observed an obelisk on the opposite side, which on account of the river was inaccessible, but whose height I wanted to acceptain. For this pur-

whose height I wanted to ascertain. For this purpose I took at B the angle CBD 50° 39′ at A the angle CAB 33° 30′, which was distant from B 368 feet. Required the height of the obelisk and the distance of the station D from its base.

Solution.—Because the angle CBD=CAB+ACB, ABCB=CAB=ACB=50° 39′—33° 30′=17° 9′, hence ABCB=D CAB=ACB=50° 39′—31° 9′, hence ABCBC are now given BC and the angle CBD, to find DC and BD, 521 and 427.2 feet respectively.

EXAMPLE VII.

A solution of this problem, more easy and commodious in practice,

may be obtained thus:-

Let CD represent any object whose height is to be determined; at the points A and B observe the angles of elevation, and measure the distance AB, the points A,B,C, and D being in the same plane. See preceding figure.

For in the triangles ABC, CBD,

sin. ACB: AB:: sin. A: BC,

and R: BC:: sin. CBD: CD, from which we have sin. ACB: AB \times BC:: sin. A \times sin. CBD: BC \times CD or sin. ACB \times BC \times CD = sin. A \times sin. CBD \times AB \times BC; radius being unity.

Hence CD= $\frac{\sin. A \times \sin. CBD \times AB}{\sin. ACB}$; or, making the terms homo-

geneous, and substituting cosec. for 1/sin.

 $R^3 \times CD = \sin A \times \sin CBD \times \csc ACB \times AB$.

That is, to the sines of the observed angles of elevation, add the cosecant of the difference of these angles, and the logarithm of the measured distance; the sum, rejecting 30 from the index, will be the height of the object.

Let the angles of elevation be 55° 54', and 33° 20' respectively, and the distance between the stations 100 feet. Required the

height of the object.



Angles of elevation	{ 55° 54′ sine 33 20 sine	9.918062 9.739975
Difference . Distance .	22 34 cosec. 100 feet	10.415942 2.0000 00
Height . Height of the eye	118.5 5.5	2.073979
Height of object.	124.0 feet.	

EXAMPLE VIII.

In order to determine the distance of two inaccessible objects lying in a direct line from the bottom of a tower 90 feet high, on the top of which I took the angles of depression of the two objects; that of the most remote being 24° 48′, and that of the nearest 58° 36′. Required their distance from the tower, and from each other.

Ans.-139.842 feet.

EXAMPLE IX.

Wanting to know the distance between two boats lying at anchor in a straight line from a light-house, which is 110 feet high, on the top of which I took the angle of depression of the farthest, and found it to be 18° 26′, and that of the nearest 56° 44′. What was their distance?

Ans.—129.5286 feet.

EXAMPLE X.

From the top of a hill I observed two mile-stones on a horizontal road, which ran straight from its bottom, and took their respective angles of depression below the horizontal plane passing through the place of my eye; that of the nearer mile-stone was 36° 12′, and that of the more distant 15° 26′. Required the height of the hill.

Ans.—780.17 yards.

EXAMPLE XI.

In order to find the height of an obelisk standing on the top of a regularly sloping hill, I measured from its bottom a distance of 40 feet, and then found the angle formed by the inclined plane, and a line from the top of the obelisk to centre of the instrument, to be 41°; and, after measuring downward in the same direction 60 feet farther, the angle formed as before was only 23° 45′. What was the height of the obelisk and the angle of the inclined plane with the horizon?

Ans.—Height 57.623 feet. Inclination 21° 54½.

EXAMPLE XII.

Wishing to know the height of a tower standing on the top of a regularly sloping hill, to the bottom of which I could not approach on account of a ditch around it, at the outside of which I took the angle formed by the inclined plane, and a line from the centre of the instrument to the top of the obelisk, and found it 41; but after measuring downward in the same sloping direction 54 feet farther, I found the angle formed in like manner to be 23° 45′. What was the height of the obelisk itself, and that of its top above the last place of observation, supposing the angle formed by the inclined plane and the horizon to be 21° 54′½?

Ans. 51.86 feet the height of the obelisk, and 83.51 above the last

place of observation.

ALIEN STANKE SHEET OF CHECK DEC

Being on a horizontal plane, and wanting to know the height of a tower on the top of an inaccessible hill, I took the angle of elevation of the top of the hill 40°, and of the top of the tower 51°; then measuring in a direct line 100 feet farther from the hill, I took in the same vertical plane the angle of elevation of the tower 33° 45. Required the height of the tower?

Ans.-46.666 feet.

EXAMPLE XIV.

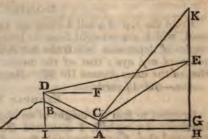
In order to know the height of a castle standing on a hill, I took the angle of elevation of the top of the castle above the horizontal plane 58°, and of the top of the hill 25°; but could not, as in last example, measure a sufficient distance directly from the castle. I therefore measured in an oblique direction 52 yards, making with the castle an angle of 72° 10′, at the farther end of which the angle, in the same manner, was 64° 30′. What was the height of the castle?

Ans .- 34.464 feet.

EXAMPLE XV.

Wanting to ascertain the height of a tower standing upon a hill, the height of the hill, and the horizontal distance from the nearest place of observation, on account of the nature of the ground I proceeded as follows:—

At A I took the angle GCK 3° 38', and GCE 2° 44'; then having set up a staff AC equal in height to the centre of the theodolite, I measured 1810 feet up the sloping ground AB in a direct line with the tower, keeping the points K, E, C, B, in the same vertical plane. At B I took the angle FDC = BAI = 1° 54',



and EDF=1° 32' Required the height of the tower, the height of the hill, and the horizontal distance from the first place of observation.

1. In the triangle DCE, are given the side DC=1810 feet, the angle ECD 175° 22′, EDC 3° 26′, and DEC 1° 12′; to find CE=5175.89 feet.*

2. In the triangle CKE, the angle K=86° 22′, CEK=92° 44′, KCE=0° 54′ and CE=5175.89; hence EK=81.463 feet.

3. In the triangle CGE, the angle GCE=2° 44', and CE=5175.89; hence CG=AH=5170 feet; and GE=246.826.

4. In the triangle ABI, AB=1810, the angle BAI=1° 54'; hence AI=1809 feet, and BI=60.011 feet.

If EK, the height of the tower, were only wanted, it may be found thus:

In calculations where the same number is used which has been found from previous computation, its log. should be reserved from the first to be used in the next, &c.

Sin. DEC: DC:: sin. CDE: CE=DC sin. CDE. cosec. DEC, sin. K: CE (=DC. sin. CDE. cosec. DEC):: sin. KCE: KE, and R4KE=DC. sin. CDE. sin. KCE, sec. GCK. cosec. DEC.

	By loga	rithms.	
sin.	CDE 3° 26′	•	8.777333
sin.	KCE 0° 54'		8.196102
sec.	GCK 3° 38'		10.000874
cosec.	DEC 1° 12.		14.678923
	DC 1810	•	3.257679
EK 8	1.463	•	1.910961

EXAMPLE XVI.

At the top of a castle which stood a hill near the sea-shore, the angle of depression of a ship's hull at anchor was 4° 52°; at the bottom of the castle the angle of depression was 4° 2°. Required the horizontal distance of the vessel, and the height of the hill on which the castle stands above the level of the sea, the castle itself being 64 feet high.

Ans.—4373.75, and 308.4 feet respectively.

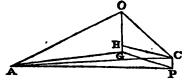
EXAMPLE XVII.

From a window in the lower part of a house, nearly on a level with the bottom of a steeple, I took the angle of elevation of the top of the steeple 40°; and from another window 18 feet directly above the former, the same angle of elevation was 37° 30′. Required the height and distance of the steeple.

Ans.—210.44, and 250.79 feet respectively.

EXAMPLE XVIII.

Suppose A and C to be two stations on sloping ground, O an object on the top of a hill, and the angles OCA, OAC, measured with a sextant, to be 79° 29' and 63° 11' respectively; also let the angle of elevation of AO above the horizon.



tal plane be 6° 36', and that of CO 5° 22'; what are the horizontal distances and height of the object, AC being 410 yards?

In the triangle AOC are given all the angles, and the side AC; to find AO and CO. Again, in the triangle AGO right-angled at G, are given the angle OAG and the side AO; to find AG=660.3 and OG=76.4. Lastly, in the triangle COB, right-angled at B, are known CO and the angle OCB; to find CB 600.7, and OB 56.4, and OG—OH=76.4—56.4=20 yards nearly =HG=CP, the difference of the heights of the stations, supposing AP to be horizontal. Now in the right-angled triangle APC are given AC and CP, to find AP= $\{(AC+CP)(AC-CP)\}^{\frac{1}{2}} = \sqrt{430 \times 390} = \sqrt{167700} = 409.5$ yards. Hence the sides of the horizontal triangle APG are given, to find the angles, which may be determined by Case III, Plane Trigonometry, to be AGP=37° 31′ 29″, GAP=63° 19′ and GPA=79° 9′ 31″

The present may serve as an example of reducing hypotenusal lines to their horizontal measure, and of determining the height of an object above each place of observation in most common cases.

EXAMPLE XIX.

The height of the mountain called the Peak of Teneriffe was found,

barometrically, by the methods described in Gregory's Mechanics, Vol. I. book 5, to be 12,356 feet, or 2.34 English miles, and the angle of depression of the horizon, from the mean of a great number of observations, 1° 58′ 12′′; it is required to determine the diameter of the earth, supposing it to be a perfect sphere.

Ans.—7913.6 miles.

Let C be the centre of the earth, the circle BTG a vertical section passing through the centre, AB the height of the Peak, AT the tangential line drawn from its top to the visible horizon, and AD a line perpendicular to a plumb-line hanging freely: also, let BE, a tangent to the earth's surface at B, meet the other tangent AT in E. Then, in the triangle ABE, right-angled at B, there are given BAE the complement of DAT, the angle of depression=88° 1' 48", and AB=2.34, hence R: AB::tan. A : BE :: sec. A : AE. But since the triangles



CBE, CTE, are right-angled at B and T, have the side CB=CT and CE common, they are (Leslie's Geom. I, 22, or Hutton's Geom. theo. 34, cor. 2) equal, and therefore BE=ET; hence, AE+BE=AE+ET=AT. In the triangle ATC, right-angled at T, we have R: AT:: tan. A: TC, the radius of the earth. The operation thus performed occupies but small compass, which may still be farther shortened. For since tan. $A + \sec$. $A = \tan$. $(A + \frac{1}{2} \text{ comp. } A)$ we shall by incorporating the proportions from which AE, BE, and CT are deduced, have WARDON ALLEY COME LUMBER

 R^2 CT=AB tan.(A+ $\frac{1}{2}$ comp. A) tan. A; or, log. CT=log. AB+log. tan. (A+1comp. A)+log. tan. A-20, in

The logarithmic computation is as follows:—

Depression 1° 58′ 12″

and can TAT I'V WITTE TO THE STORE THE PROSENT CASE, the are may be superficient for the red color added to the red by the case are may be superficient for the red color of the red by the case are may be superficient for the red color of the re Comp. depress. 88 1 48 tan. 11.4634852

89 0 54 tan. 11.7646436 Height of Peak 2.34 miles, log. 0.3692159 had a 2.5973447

(5.00009 + log. AB to to to to

vol. III. page ISB.

Diameter and 7913.6 to main ade dip od beauty and and

Distance 136.1 2.1338595

If AT were required, we have only to take radius (10) from the sum of the two last lines, and the remainder, 2.1338595, is the log. of 136.1, the distance sought.

Note 1 .- This method of determining the earth's radius, though elegant in theory, is useless in practice, at least where any thing more than an approximation is wanted, by the great irregularity of the horizontal refractions.

Note 2 .- When the diameter of the earth is known, and height of the object given, the distance of the visible horizon may be easily found; for, Euc. III. 36. AB. AG-AT2.

By logarithms. 2.34 log. 0.300016 AB 7913.6 BG AB+BG=AG 7915.94 log. 3.808503 **L.2677**10 **2.133869**• As before 136.1 miles, log.

Note 3.—The depression of the horizon, or the dip, as it is called at sea, is the angle DAT contained between the true and visible horison. For if an observer, whose eye is althated at A on the deck of a vessel, takes the altitude of a celestial object with Hadley's quadrant or sextant, by bringing that object to the surface of the water at T, instead of the true horizon AD, the altitude is evidently too great by the angle DAT=TCA. This may be calculated by the usual formulæ of trigonometry for that purpose; but as it will, at any probable altitude, be a small quantity, those which give the cosine or secant of its value are not sufficiently correct; for which reason we shall give the following method:-

(BG+AB)×AB=AT°, (Euc. III. 36.), hence BG×AB+AB°—AT°, or 2BC×AB+AB°=AT°, and AT° being, at any probable elevation, but a small quantity in comparison of AC, it may be safely measured; therefore $\sqrt{(2BC \times AB)}$ =AT. But CT(=BC): B:: AT $\sqrt{(2BC \times AB)}$: tan. C=tan. DAT = $\sqrt{(2BC \times AB)}$ = $\sqrt{(2BC \times$

Now since $\frac{2 R^2}{RC}$ is a constant quantity, and BC being taken in gene-

ral at 8956 miles = 20887680 feet, hence the log. of $\frac{2R^2}{RC}$ is 12.96114, and tan. DAT= $\frac{1}{2}$ (12.98114+log. AB). Since, in the present case, the arc may be substituted for its tangent, the radius, therefore, becomes 57° 17' 44".8=206264".8; and we have log. DAT in seconds

=1(3.00999 + log. AB in feet).
The dip is affected by terrestrial refraction, which is very variable, and by different authors it is estimated at different quantities. Dr Maskelyne estimated it at one-tenth of the whole; M. Delambre, oneeleventh, and Col. Mudge, one-twelfth. See Dr Hutton's Course, vol. III. page 138.

Ex.—Required the dip, the height of the eye being 40 feet, and estimating the terrestrial refraction at 1s.

Constant log. Height of eye 40 feet 1.60206

5.21205 403".6 log. 2.60602 33.6 Refrac. sub. 🖓 370=6' 10". Dip†

See also the method by Leulie in his Geometry.
 The dip in minutes is equal to the equare rest of the height in feet nearly.

Note 4.—Since AB×BG+AB²=AT², therefore

 $AB(AG + AB) = AT^2$, and $AB = \frac{AB}{BG + AB}$

Now, if AB is the unknown quantity, and being small in comparison of BG, it may be found approximately by making, first, $AB' = \frac{AT^2}{RG}$ nearly, substituting this value of AB' for AB in formula (1.), and

AT (2.)BG + AB's say to more hard and to mole say the

which will be sufficiently correct for most purposes. If not, the operation may be repeated till it is so.

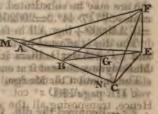
This is useful in determining the height of an object considerably

Now, the mean diameter of the earth is about 7912 miles, or 1775360 feet =GB, of which the logarithm is 7.620920, and its arithmetical complement is 2.379080; therefore to twice the log. of AT, in feet add the constant log. 2.379080, the sum, rejecting tens in the index, will give AB', which will be sufficiently correct if AT does not exceed 1000 feet. If more distant, the operation must be repeated. This correction must always be added to heights determined geometrically as the usual instruments give their eleva-EXAMPLE XX.

Given the angles of elevation of any distant object, taken at three places in a horizontal straight line, which does not pass through the point directly below the object; and the respective distances between the stations: to find the height of the object, and its distance from either station.

Let AEC be the horizontal plane; FE the perpendicular height of the object F above that plane; A, B, C, the three places of observa-

tion; FAE, FBE, FCE, the respective angles of elevation, and AB, BC, the given distances. Then, since the triangles AEF, BEF, CEF, are all right- MA angled at F, the distances AE, BE, CE, will manifestly be as the cotangents of the angles of elevation at A, B, and C; and men about the minny we must determine the point E, so that these lines may have that ratio.



Construction.

To effect this geometrically, we must take BM, or AC produced, equal to BC, BN equal to AB; and make

MG: BM (=BC):: cot. A: cot. B, and good HA and T BN (=AB) : NG : : cot. B : cot. Co all priving line yd

With the lines MN, MG, NG, construct the triangle MNG; and join BG. Draw AE so, that the angle EAB may be equal to MGB; this line will meet BG produced in E, the point in the horizontal plane falling perpendicularly under Firmed and and bassanger anisation and interior Demonstration, within several at het to not

(10)

By the similar triangles AEB, GMB, we have

AE: BE: MG: MB:: cot. A: cot. B, and

BE: BA (=BN): BM: BG.

Therefore the triangles BEC, BGN are similar; consequently

BE : EC :: BN : NG :: cot. B : cot. C. Whence it is obvious that AE, BE, CE, are respectively as cot. A, cot. B, cot. C.

Calculation.

In the triangle MGN are given all the sides, to find the GMN, equal to the angle AEB. Then, in the triangle MGB, are given two sides, and the contained angle; to find the angle MGB, equal to the angle EAB. Hence, in the triangle AEB are known the side AB, and all the angles; to find AE and BE. And then EF=AE. tan. A=BE . tan. B.

Analytically.

Let AB=r, BC=s; also let the cotangents of the angles FAE,

FBE, FCE, be denoted by the letters a, b, c, respectively. Then, putting EF = x, we have, to radius 1, 1:a::x:ax = AE, 1:b::x:bx = BE, 1:c::x:cx = CE; and on AC from E, letting fall the perpendicular ED, we have (Euc. II. 12) $a^2 x^2 = b^2 x^4 + r^2 + 2r$. BD; hence BD = $\frac{a^2 x^2 - b^2 x^2 - r^2}{2s}$. In like manner CD =

$$r^{2}+2r$$
. BD; hence BD= $\frac{u^{2}x^{2}-r^{2}}{2s}$. In like manner CD=

$$\frac{b^{9} x^{2}-c^{2} x^{2}-s^{2}}{2 s} = BD - BC = BD - s: \text{ whence } BD = \frac{b^{9} x^{2}-c^{3} x^{2}+s^{9}}{2 s}.$$

Therefore
$$\frac{b^2 x^2 - c^2 x^2 + s^2}{2s} = \frac{a^2 x^2 - b^2 x^2 - r^2}{2r}$$
. Hence $x^2 = \frac{rs^2 + rs^2}{s(a^2 - b^2) - r(b^2 - c^2)}$, and $x = \sqrt{\frac{rs(r+s)}{s(a^2 - b^2) - r(b^2 - c^2)}}$.

Otherwise thus;

If AB and CB be conceived to be bisected in M' and N', and BD a perpendicular upon AC, which are however omitted to avoid complexity in the figure; then, (Leslie's Geometry, II, 21.) AE -BE $=AB \times 2M'D$, and $CE^2 - BE^2 = BC \times 2N'D$; therefore, $AE^2 \times BC$ $-BE^{g} \times BC = AB \times BC + 2M'D$, and $CE^{g} \times AB - BE^{g} \times AB = AB$ \times BC \times 2N'D. Adding equals to equals, and AE^a \times BC+CE* \times AB $-AC \times BE^{\circ} = AB \times BC \times AC$; consequently $AE^{\circ} \times BC + CE^{\circ} \times AB$ $=AC \times BE^{\circ} \times AC \times AB \times BC$.

If AB=BC, then AE²+CE²=2AB²+2BE², the line EB being drawn from the vertex E of the triangle ACE, to any point B in the base. Put AB=D, BC=d, EF=x, and then expressing algebraically the foregoing theorem.

The equation thence resulting is,

 dx^2 cot. ${}^2A + Dx^2$ cot. ${}^2C = (D+d)x^2$ cot. ${}^2B + (D+d)Dd$. Hence, transposing all the unknown terms to one side of the equation, dividing by the sum of the coefficients, and extracting the

square root, we shall have $x = \sqrt{\frac{(D+d)D d}{d \cot^{9}A + D \cot^{9}C - (D+d)\cot^{9}B}}$ Thus EF becoming known, the distances AE, BE, CE, are found by multiplying the cotangents of A, B, and C, respectively, by EF.

Cor.—When D=d, or D+d=2D=2d, the expression becomes $x=d+\sqrt{(\frac{1}{2}\cot^2 A+\frac{1}{2}\cot^2 C-\cot^2 B)}$, which is pretty well suit-

ed to logarithmic computation. The rule may, in that case, be thus expressed.—Double the logarithm cotangents of the angles of elevation of the extreme stations, find the natural numbers answering thereto, and take half their sum; from which subtract the natural number answering to twice the logarithm contangent of the middle angle of elevation: then half the log. of this remainder subtracted from the log, of the measured distance between the first and second. or the second and third station, will be the logu of the heights of the object.

. Let AB=60 feet, BC 72 feet; angle FCE=50° 23', the angle FBB=40° 38', and the angle FAE=30° 48'; required the distances AE, BE, CE, and EF, the height of the object. Ans.—AE=159.09 feet, BE=110.84 feet, CE=78.51 feet, and

EF=94.84 feet.

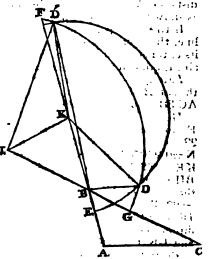
2. Let the three angles of elevation be 36° 50', 21° 24', 'and 14° and the two equal measured distances 84 feet; required the height Ans.-53.964 feet. of the object.

EXAMPLE XXI.

Given the angles of elevation at which an object is seen from three given points in a horisontal plane; to find its position and altitude;

Let A, B, and C be the three points of observation, and D the bottom of the perpendicu-Jar from the given object to the horizontal plane. It is evident that the horizontal dissances AD, BD, and CD are proportional to the cotangents of the vertical angles at the stations A. B. C.; let these coctangents be respectively denoted by the L, M, and N.

and Divide AB internally and externally at the points E and Fin the ratio of L to M : and the lines DE and DF joining in the vertex D must hisect internally and externally the angle, whence EDF is a right angle, and contained in a semicirale; wherefore on EF de-



acribe a semicircle. In the same manner, divide CB internally and externally at G and H* in the ratio of M to N, and on GH describe (a semicircle. The point D common to both semicircles must occur in their intersection.

From this construction the trigonometrical calculation is readily deduced. For L+M: M:: AB: BE and L-M: M:: AB: BF;

BE + BFwhence DE == -== 1, or madius KE is found. In like S & 15 mg 13 (1) manner N+M: M:: CB: BG, and N-M:M:: CB: BH; come-BG+BH. In the triangle IBK, the sides BI and "BK, with their included angle, = ABC, are given; and, therefore,

^{*} See Lealie's Geometry, fourth edition, page 275. To avoid extending the figure too much, the point H, which should be in continuation of BI, in the same way as BF is in continuation of BK, as well as the lines joining DE and DF, is omitted.

" it samples

the angle BKI and the hase IK are found. Again, till the sities of the triangle IDK being given, the angle IKD is foundmilleness in the triangle BDK the whole angle BKD and its containing sides are given ; and, therefore, the base BD, or the horisontal distance from the station B, and consequently its altitude, is determined.

It is obvious, that the opposite semicircles will likewise, by their insersection, give, on the other side, a second position D' for that point. In practice, however, this ambiguity could be easily removed. It may be remarked too, that the point D may fall either with-

in er without the triangle.

If the object be seen at the same elevation from all the three points, the arcs of the circles will evidently become tangents, which bisect at right angles the sides of the triangle ABC. The projection Disf the object on the horisontal plane, will then be the centre of the circle circumscribing that triangle; and, therefore, the radius or distance AD may be found by prop. 18, book VI. Leslie's Geometry, as shown in the notes, page 347.

If the three points of observation should lie in the same straight line, the centres of the determining circles will occur in that line or its extension; and hence the process of calculation will be greatly abridged, and will coincide with the foregoing proposition. It is a few the coincide of elevation of the object at A; be 60° 45′,

that at B 58° 15', and that at C 46° 45'; also the side AB 34' yards, AC 38, and BC 50. Required its height?

Hence L = cot. 50° 45', M = cot. 58° 15', and N = cot. 45° 45'.

From the given sides the angle ACB = 27° 35' 10"; ABC = 47" 9 22", and BAC 105° 15' 28". Also L = 0.8170348, M = 0.6168188, N=0.9407061; therefore, BE = 10.343, and BF = 74.929, whence KE = 42.6355, and BK = 32.2925. In like manner, BG = 19.846, BH = 96.123, hence DI = 57.9845, and IB = 38.1385. From these the angle IKB = 77° 11′ 24″, and KIB 55° 39′ 14″; and the side IK =23.677. Now from the three sides ID, IK, and KD, the angle IKD = 107° 10′ 20″. To this, by applying the angle IKB by addition and subtraction we obtain the angle BKD = 184° 21′ 50″, and BKD = AKD = 29° 59′ 2″.

From the sides BK and KD, and the contained angle BKD, are found the angle KBD = 102° 16′ 30″, and KDB = 47° 44′ 19″, from which BD = 21.8065, and the height of the object 35.84 yards. THE Should the point D' be the foot of the perpendicular, the angle $KBD' = 2^{\circ} 29^{\circ}$ and $KD'B = 1^{\circ} 52' 50''$, and BD' = 74.876; whence

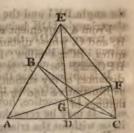
rithe height above D' will be 121 yards.

: enth seiwest Die Ed is tound. In like Given the angles of elevation of the object from three points in -9 the said plane forming a triangle, of which the sides are known; to find the position of the object referred perpendicularly to that plane and its altitude above it.

Construction.—The perpendicular from the object to the plane

and the state of t

may fall either within or without the triangle. In both cases, let A, B, and C be the points of observation, and a, s, and y the angles of elevation at these points respectively. Join A, B, and C, and on AB produced, B if necessary, make AE equal to AC, and AD to AB, join ED, and upon it construct the triangle EDF so that cotangent & : contangent \$:: AE : EF, and cotangent \$: cotangent y :: AD : DF. Join AF, and from A



B draw BG, making the angle ABG equal to the angle ATE, and join CG. The point G in which the straight lines BG and AF intersect each other will be the point at which a perpendicular let fall from the object would meet the plane, thus ascertaining the position of the object, from which, and the given angles, its alti-

tyde may be found. It have he show of hounted bound A

Demonstration .- It is obvious that the straight lines drawn from each of the points of observation to the point at which a perpendicular let fall from the object meets the plane, ought to be in proportion to the cotangents of the angles of elevation at these points respectively. The proposition therefore resolves itself into this. To find a point in a plane from which straight lines drawn to three given points in the same plane shall have to each other a given ratio which follows from the construction just given.

Solution .- In the triangles ABG, AFE, the angles at B and F are equal by construction, and the angles BAG is common to both these two triangles are therefore similar. And AG: BG:: AE: EF

:: cot, a : cot. s. Hence EF = AC × cot. s . Again AG : AE : :

AB: AF or AG: AC:: AD: AF; and as the angle at A is common to the two triangles AGC, and ADF; these triangles similar, consequently AG : CG :: AD : FD :: cot. a : cat y, whence FD= AB x cot. y.

cot. a

The triangles ADE, ABC having the sides AD, AE of the one equal to the sides AB, AC of the other, and the angle at A, common to both, are equal, and the side ED is equal to the side BC. Therefore in the triangle ADE, the three sides are given, and those of the triangle FDE are already found; whence the angles AED and FED, and consequently the angle AEF may be obtained; and from the angle AEF, with the sides AE and EF, the angle AFE or ABG, which is equal to it, may be determined. Then in the triangle ABG, having the two angles at A and B, and the side AB the distance, BG may be found, consequently, with it and the angle

8, the height of the object becomes known.

Example.—Let the side AB be 80 feet, BC=119, and AC=140, also the angle at A or $\alpha=50^{\circ}$, that at B or $\beta=60^{\circ}$, at C or $\gamma=55^{\circ}$;

required the height of the object.

From these EF=96.329, DF=66.758; the angle AED=34° 48', EDA=87° 6′ 23″, EAD=87° 6′ 23″, EAD=58° 5′ 37″, GEF=34° 6′ 57″, AFE, or ABG=70° 37′ 8″, FAE or AGB=40° 28′ 16″, BG =55.673; and the height 96.392 feet.

the entire of their

EXAMPLE XXIII.

From a convenient station P, there could be seen three objects A', B, and C, whose distance from each other were AB=8 miles, AC=6 miles, BC=4 miles; I took the horizontal angles APC=33° 45′, BPC=22° 30′. It is hence required to determine the respective distances of my station from each object. Here it will be necessary, as illustrative and preparatory to the computation, to describe the manner of

Construction.

Draw the given triangle ABC from any convenient scale. From the point A draw a line AD to make with AB an angle equal to 22° 30′, and from B a line BD to make an angle BDA equal to 33° 45′. Let a circle be described to pass through their intersection D, and through the points A and B. Through C and D draw a straight line to meet the circle again in P, which is the point required. For drawing PA, PB, the angle APD is evidently equal to ABD, since it stands on the same arc AD; and, for a like reason, BPD =BAD. So that P is the point where the angles have the assigned value.

Computation.

In the triangle ABC, all the sides are given; to find the angles. In the triangle ABD, all the angles are known, and the side AB; to find one of the other sides AD. Take BAD from BAC, the remainder, DAC is the angle included between two known sides AD, AC; from which the angles ADC and ACD may be found. The angle CAP = 180°—(APC + ACD). Also, BCP = BCA—ACD; and PBC=ABC+PBA=ABC+ sup. ADC. Hence, the three required distances are found by these proportions.

As sin. APC: AC:: PAC: PC, and:: sin. PCA: PA; and, lastly, as sin. BPC: BC:: sin. BCP: BP. The operation at length is as under:

By Rule II., Case III., we have

40.00

ADB 123 45

Sin.
$$\frac{1}{4}$$
 BAC = $\sqrt{\frac{1 \times 3}{8 \times 6}} = \sqrt{\frac{1}{18}} = \frac{1}{4} = 25 = \sin . 14^{\circ} 28' 39''$, and BAC = $28^{\circ} 57' 18''$.

Sin. $\frac{1}{4}$ ABC = $\sqrt{\frac{1 \times 5}{8 \times 4}} = \frac{1}{8} \sqrt{10} = 3952847 = \sin . 23^{\circ} 17' 1'' \frac{1}{4}$, and ABC = $46^{\circ} 34' \frac{3''}{3}$.

Sin. $\frac{1}{4}$ ACB = $\sqrt{\frac{3 \times 5}{6 \times 4}} = \sqrt{\frac{4}{8}} = \frac{1}{4} \sqrt{10} = 7905694 = \sin . 52^{\circ} 14' 19'' \frac{1}{4}$, and ACB = $104^{\circ} 28' \frac{39''}{39''}$.

DAB = $22^{\circ} 30'$ CAB = $28^{\circ} 57' 18''$ 180° 0' 0'' DBA 33 45 DAB = $22^{\circ} 30'$ 0 DAC = 6 27 18

Sum $56 \ 15$ DAC = 6 27 18 ADC + ACD = $173 \ 32 \ 42$ 180 0 $\frac{1}{4}$ (ADC + ACD) = $86 \ 46 \ 21$

	9.7447390
	. 0.7279826 10.7781513
Arc . 48° 18′ 7″ tan. Subtract 45 0 0	10.0501687
Remainder 3 18 7 tan.	8.7611283 11.2487967
1(ADB—ACD) 45 39 17 tan.	10.0099250
AND DESCRIPTION OF THE PARTY OF	0.2552610
	the winterest or All and
PAC 105 7 56 sin. AC 6 miles log. 0.7781513	9.9846740 0.7781513
PA 7.10199 miles 0.8513801	in the transfer A letter
PC 10.42525 miles ACB=104° 28′ 39″ ACD= 41 7 4 BCP+BPC=	1.0180863 180° 0′ 0′ 85 51 35
BCP= 63 21 35 PBC= As sin. BPC 22° 30′ 0″ ar. co. Is to BC 4 miles So is sin. BCP 63° 21′ 35″	94 8 25 0.4171603 0.6020600 9.9512594
To PB 9.34285 miles	0.6704797
The computation of problems of this kind, shortened by means of the following	however, may be a little

shortened by means of the following

General Investigation.

Put AC=a, BC=b, APC=P, BPC=P', ACD=C, and let there be taken for unknown quantities PAC=x, PBC=y. The triangles PAC and PBC give

Sin. APC: sin. CAP:: AC: CP, and Sin. BPC: sin. CBP:: BC: CP; that is, Sin. P: $\sin x :: a : \frac{a \sin x}{\sin P} = CP$, and Sin. P': sin. $y::b:\frac{b\sin y}{\sin P'}$ =CP.

Hence, $\frac{a \sin x}{\sin P} = \frac{b \sin y}{\sin P}$; which may be reduced to a sin. P' sin. $x-b \sin P \sin y=0.$

^{*} See Lacroix Trigonometrie, and Gregory's Trigonometry.

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The quadrilateral ACBP, we have CBP 3600 APC BPCA CAP, or y=360-P-P'-C-x.

Make 3600 P-P'-C=R, then we shall have y=3 ; and consequently, a \sin P' \sin x - b \sin P (sin. R cos, x—cos. R. \sin x)=0.
 SECURITY by sin. x, there results, a sin. P'—b sin. P(A) R cos. T sin. x
  Whence we have \frac{\cos x}{\sin x} = \cot x = \frac{a \sin R}{0} + \sin R \sin R
      This expression separated into two parts, we have
                                                     a sin. P' pacos. Al & rabiliscred
 3.7611283
 TOUTGLE HOOL & = b sin. P sin. R Think Pir Record to 400A)
  0.0200(0.0) \text{ [cot. } x = \frac{\text{cos. R}}{1000} / \frac{a \sin. P}{1000}
                                               sin. R (b sin. Pros. Ret b); (%) A.-. ROA)
                                                                        a sin. P
                           cot. x = \cot R \left(\frac{b \sin P}{b \cos R}, \frac{1}{1 \cos V}, \frac{1}{1 \cos V}, \frac{1}{1 \cos V}, \frac{1}{1 \cos V}, \frac{1}{1 \cos V}\right)
                                                                                                          ACD 410 7" 4" Shi
collada Ann. P' cosec. P cosec & cost Recet. R + cosp Rrs 0 4 68 39A
      Hence, x being thus determined, we get y from the equation y
R-x; and CP from either of the expressions given shows. Will
      We shall now apply the foregoing formula to the solution of the
 quastion lest proposed.
                                                                                                               PAC 105 7 56 site
             EXAMPLE XXIV.

a = 6 P = 33° 45' ()' PAC=x
b = 4 P' = 22 30 Q PBC=y

ACB = 104 28 39 found by computation
                                                                                                              AC Orailes log.
 Here a \stackrel{\text{Elcisty}}{=} 6
                                                                                                                   7.10199 mile.
     Eliment Line
                                                                                                                 PC 10.425:ni miles
                                             160 43 39
  1002 0 1001
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                                            360
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                                                                                                   ACD at 41 🔞 🐺
     SE 17, 40
                                 R = 199 16 21
     3 6 45 a
                                                                                                    20. (2.33) * 生斑
cot. x = \frac{a}{b} \sin \frac{P}{\cos c} cosec. P, cosec. R cot. R + cot. R; or it was known as \frac{P}{\cos c}
cot. x = \cot R \frac{\text{Cloudsin. P'}}{\text{bein. P }\cos R} + 1) and using logarithms
                             = MC.04257
                                                                                            3 log. 0.4771912; UT 5T
elitics of year (1979 %) # long side 2 ar. co. 9.6989700 quan adT

P = 280,30 0' sin, 9.5838397 q bonotrods

P = 33° 45° 0" ar. co. S. 0.2552610

R whose cos, is neg. 159° 15° 21° ar. co. C. 0.0250452
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    + 1.00000
ACCAP CP
                                                                                                  cot. R
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cot. x
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                            33° 45′ 0″ ar. co.
As sin.
Is to sin. x 105 8 10.
So is 6 0.27781613
                                                                                                           red sin. P sing from
                           10.4251
                                                                      1.0180783
Whence the rest may be found on the mount of the second of
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In using these formulæ great attention must be paid to the signs of the quantities.

EXAMPLE XXV.

Suppose the objects A,B,C, are seen from D, and have their distances AB 7½ miles, BC 12 miles, and AC 8 miles, the angle BDA 25°, and CDA 19°; it is required to determine the distances DA, DB, DC.

Ans.—DA 10.0286, DC 16.7857, DB 14.9095 miles.

EXAMPLE XXVI.

Suppose the objects A, B, C, are seen from D, and have their distances AB 8 miles, BC 12, and AC 7½; the angle BDC being 17° 47′ 19″. Required the distances DA, DC, and DB.

Ans.—DB 12, DC 22.85, and DA 20 miles.

EXAMPLE XXVII.

If, AB be 8, AC 7.2, and BC 12 miles, and the angle ADB 107° 56' 13". Required the distances DA, DC, and DB. Ans.—DB 5, DA 4.892, and DC 7 miles.

EXAMPLE XXVIII.

Let the objects A, B, C, be in a straight line; and their distances AC 3.626, AB 12, and BC 8.374, the angle ADC being 19°, and BDC 25°. Required the distances DA, DC, and DB. Ans.—DA 9.4711, DC 10.861, and DB 16.8485.

EXAMPLE XXIX.

Let the objects A, B, C, as seen from D, be within the triangle; and let the distance AB be 6 miles, BC 12, and AC 9, the angle BDC being 123° 45', and ADC 132° 22'. Required the distances DA, DC, and DB.

Ans.—DA 1.372, DB 5.523, DC 8.018.

EXAMPLE XXX.

A ship from Bombay in latitude 18° 57' N, sailed S. W. by S. 224 miles. Required the latitude come to, and the departure. Ans.—The difference of latitude is 186.2, and the departure 124.4

Latitude of Bombay 18° 57' N. Diff. of lat. 186 miles = 3 6 S.

Latitude come to

15 51 N.

EXAMPLE XXXI.

Having occasion to travel through the counties of Kent and Surrey, I perceived the fort built by Lady James, on Shooter's hill, which bore from me N. N. E.; and after going 20 miles in a W. N. W. direction, I perceived the fort again, which now bore N. E. by E. Required my distance from it at each station.

Ans.-29.93 miles, and 36 miles.

EXAMPLE XXXII.

From a ship at sea, I observed a point of land to bear E. by S., and after sailing 12 miles N. E., it bore S. E. by E. Required the distance of the last place of observation from the point of land. Ans.-26 miles.

EXAMPLE XXXIII.

Sailing N. N. W. at the rate of 6 knots an hour, at 8h. P. M. I discovered two light-houses, the northernmost of which bore N. N. E. and the other E. by N., and at 10h. 30m. the northernmost light bore E. N. E., and the other E. S. E. The bearing and distance of

the lights from each other are required.

Calculation.—In the triangle ACD are given the side AC equal to 15 miles, the angle ADC 3 points, the interval between E by N. and E. S. E. and the angle CAD 4 points, the distance between S. S. E. the opposite point to N. N. W., and E. S. E.; to find CD = 19.09. Again, in the triangle ABC are given AC as before equal to 15 miles, the angle ABC equal to 4 points, the interval between N.N.E. and E.N.E. and the angle ACB also 4 points, the interval between the N. N. W. and N. N. E. points; hence the angle CAB is a right angle; consequently, we get BC = 21.21.

Lastly, in the triangle BCD are given the sides CB, CD, equal to 21.21 and 19.09 respectively, and the included angle BCD 5 points, the interval between N. N. E. and E. by N.; to find the angles CDB $=67^{\circ} 30'$, CBD $=56^{\circ} 15' = 5$ points, CBE = BCN = 2 points, and

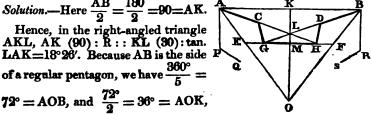
the distance BD = 19.09.

Example XXXIV.

The side AB of a pentagon being 180 toises, the face of the bastion AC 50, the normal or perpendicular KL 30; it is required to find, by trigonometrical calculation, all the other lines and angles of the fortification, supposing the line of defence AH to be equal to a line drawn from A to D.

Solution.—Here $\frac{AB}{2} = \frac{180}{2} = 90 = AK$.

Hence, in the right-angled triangle AKL, AK (90): R:: KL (30): tan. LAK=18°26'. Because AB is the side P of a regular pentagon, we have $\frac{360^{\circ}}{5}$ =



whence 90° = 36° = 54° = EAK, and 54° = 18° 26' = 35° 34' = EAC, which being doubled is 71° 8′, the sallent angle PAC or DBR. Join BC, then will ABC be a triangle in which are given AB, AC, and their contained angle BAC; to find ABC=6° 48′. Now sin. ABC (6° 48'): AC (50):: sin. BAC (18° 26'): BC = 133.52, equal to the line of defence AH or BG. In the triangle BCG, ABG—ABC=18° 26'-6' 48' = 11° 38' = CBG. Because BC = BG, we have $\frac{168^{\circ} 22'}{2} = 84^{\circ} 11' = CGB.$ 1**90**°—11° 38′

Again, because AB and EF are parallel, and AH, BG equal; we have the angles BAH, ABG, AHE, and BGF all equal, that is, each equal to 18° 26'.

In the triangle CGH, we have the angle CGB+BGH = 84° 11' $+18^{\circ} 26' = 102^{\circ} 37' = CGH; 180^{\circ} - (CGH + CHG) = 180^{\circ} - (102^{\circ})$ $37' + 18^{\circ} 26') = 58^{\circ} 57' =$ the angle HCG; and the side CH = AH -AC = 133.52 - 50 = 83.52 = CH. Then sin. CGH (102° 37'): CH (83.52):: sin. CHG (18° 26'): the flank CG or DH = 27.062:: sin. $HCG (58^{\circ} 57')$: the curtain GH = 73.323.

TABLE OF THE MEASURES OF THE PRINCIPAL LINES AND ANGLES IN REGULAR FORTRESSES, FROM FOUR TO TWELVE SIDES INCLUSIVE.

Company of the Contract of the	Names of Polygons.					1000			
Names of Sides and Angles.	Square	Pentag	Hexag	Hepta.	Octag.	Nonag.	Decag.	Undec.	Dodec
Exterior side, in toises	180.	180.	180.	180.	180.	180.	180.	180.	180.
Radius of exterior side	127.3	153.1	180.0	207.4	235.2		291,2		347.7
nterior side	115.5	125.9			140.0		144.3		148.1
Radius of interior side -	81.7	105.4	130.6	157.0	183.0		233.4		286.1
Capital	45.6	47.7	49.5		52.2	54.2	57.8		61.7
Normal	22.5	27.0	30.0		34.0		39.0		43.0
Curtin	78.0	77.1	76.4	75.9	75.3		73.7		69.3
Face	20.3	24.5	27.3	50.0	31.1 50.0	33.0 50.0	35.8	37.0	58.1
Line of defence	133.0	50.0 134.2	135.1	135.8	156.4	137.2	50.0 138.2	51.0 138.2	52.0 138.2
Demigorge	18.7	23.4		30.2	32.4	34.1	35.3	37.4	39.4
Angle of the Centre .	9090	7200	600 0	51926	4500	4000	369.0	32944	30°
Angle of the Polygon .	90. 0	108 0	120 0	128 34	135 0	140 0	144 0	147 16	150 (
Angle of the Curtin	97 1	98 21	99 13					102 15	102 46
Angle of the Shoulder .	111 3	115 3						126 45	128 18
Angle of Bast., or Flank. Angle	61 56			89 26	93 36		97 8	98 16	98 5
Diminished Angle	14 2		18 26	19 34	20 42		23 26	24 50	25 3
Exterior Flanking Angle .	151 56	146 36	143 8	140 52	138 36	156 24	133 8	131 0	128 56
Breadth of Foss, in Toises	15	16	17	18	19	20	21	22	23

APPENDIX.

and any of the second s

BAROMETRIC MEASUREMENT OF ALTITUDES,

Having given a pretty full view of the method of measuring the heights of objects geometrically, we shall here subjoin that of determining them by the barometer, thermometer, and hygrometer.

That the observations may be carefully and properly made, the persons who undertake them should be provided with two portable barometers of the best construction, filled with mercury of the same specific gravity, on which, by means of a vernier properly adapted to the scale, the height of the mercurial columns may be read off to the 500th part of an inch; each barometer being fitted up with an attached thermometer, set in the wooden frame in the same manner as the barometer tube is. The ball of each thermometer would be best if nearly of the same diameter as the barometer tube. Besides these, they must also be provided with two other thermometers detached from the barometers. Of these barometers, one, with its attached and detached thermometers, is to be placed in the shade at the top of the eminence, while the other remains below. Let them continue in their places at least a sufficient time for the detached thermometer to acquire the temperature of the air, that is to say, till the contained fluid is stationary. Then the observer on the eminence must note down the height of the mercurial column in the barometer, as well as the temperatures exhibited by the attached and detached thermometers; and, at the same time, the other observer must make like observations upon the instruments below. If, in

this manner, three or four sets of observations be taken, at each station, after short intervals of time, and the mean of the results furnished by these sets respectively be taken, the probability of error in the true altitude deduced by the following rules will be much diminished. When our third method of computation is adopted, two of Daniell's hygrometers must be employed to determine the dew points at each station. If the observations be repeated on several successive days, the position of the instruments ought to be changed at each station alternately, at the same time comparing each pair of instruments to determine their index error should there be any. It is also advisable to make the observations in screne weather, between 11 and 12 o'clock. For it has been found that the computed heights are too small, when the observations have been made near sunrise or sunset, or when the wind blows fresh from the south; and that, on the contrary, the computed results are too great, when the observations are made about three o'clock in a hot summer day, or during a brisk wind from the north or east.*

I. Dr Robison's Method.

In this method no tables are required; it will be sufficiently exact for most purposes, and is not difficult to remember. It was deduced from the following considerations:

1. The height through which we must rise in order to produce any fall of the mercury in the barometer is inversely proportional to the density of the air, that is, to the height of the mercury in the barometer.

2. When the barometer stands at 30 inches, and the air and guicksilver are at the temperature of 32° of Fahrenheit's thermometer, we must rise through 87 feet to produce a depression $\frac{1}{10}$ of an inch.

3. But if the air be of a different temperature, this 87 feet must be

increased or diminished by about 0.21 of a foot for every degree of difference of the temperature from 32°.

4. Every degree of difference of the temperatures of the mercury at the two stations makes a change of 2.833 feet in the elevation.

Hence the following rules:

I. Take the difference of the barometric heights in tenths of an

inch; call this D.

II. Multiply the difference d between 32° and the mean temperature of the air by 21, and take the sum or difference of this product and 87 feet. This is the height through which we must rise to cause the barometer to fall from 30 inches to 29.9; and may be called h.

Thus $\frac{30Dh}{m}$ is the approximated elevation very nearly.

IV. Multiply the difference & of the mercurial temperatures by 2.833 feet, and add this product to the approximated elevation if the upper barometer has been the warmest; otherwise subtract it; then will the resulting sum or difference be the corrected elevation.

Or, this rule may be expressed by the following formula, where d is the difference between 32° and the mean temperature of the air, D is the difference of barometric heights in tenths of an inch, m is the

One person may perform the whole operation with one set of instruments, by making the observations two or three times alternately at the top and bottom, and taking a mean of the results at each station.

mean barometric height, & the difference between the mercurial temperature, and E is the correct elevation.

 $E = \frac{30(87 \pm 0.21 d)}{m} \pm 3 \times 2.833.$

For an example, suppose that the mercury in the barometer at the lower station was 29.4 inches, its temperature 50° of Fahrenheit's thermometer, and the temperature of the air 45°; the height of the mercury at the upper station 25.19 inches, its temperature 46, and the temperature of the air 39°.

Here D = 294 - 251.9 = 42.1 $h = 87 + (10 \times 21) = 89.1$ $m = \frac{1}{6}(29.4 + 25.19) = 27.295$

$\frac{30D h}{m}$ = approximate eleva	tion	=	- 32 1	-		4123.24
Correction for temp. merc.	4×	2.833	= .			11.33
Correct elevation in feet Do in fathoms	0		The state of	N best	- 7	4111.91 685.32

II. Dr Hutton's Method.

1. Observe the height of the barometer at the bottom of any height or depth intended to be measured, with the temperature of the quick-silver by means of a thermometer attached to the barometer, and also the temperature of the air in the shade by a detached thermometer.

2. Let the same thing be done also at the top of the said height or depth, and, at the same time, or as near the same time as may be. And let those altitudes of the barometer be reduced to the same temperature, if it be thought necessary, by correcting either the one or other; that is, augment the height of the mercury in the colder temperature, or diminish that in the warmer, by its $\sqrt[3]{600}$ th part for every degree of difference of the two. The altitudes so corrected being denoted by M and m.

3. Take the difference of the common logarithms of the two heights of the barometer, corrected as above, if necessary, cutting off 3 figures next the right hand for decimals, when the log. tables go to 7 figures, or only 2, when they go to 6, and so on; or, in general, remove the decimal point 4 places more towards the right hand, those on the left

are fathoms in whole numbers.

4. Correct the number last found for the difference of temperature of the air as follows: Take half the sum of the two temperatures for the mean one; and for every degree which this differs from the temperature 31° , take so many times the $\frac{1}{135}$ th part of the fathoms above found, and add them if the mean temperature be above 31° , but subtract them if the mean temperature be below 31° ; and the sum or difference will be the true altitude in fathoms; or, being multiplied by 6 it will be the altitude in feet.

Thern	nometers.	Barometers.
Detached 45 39	Attached 50 46	29.4 lower 25.19 upper
Mean 42	Diff. 4	Charles Service of the

As 9600: 4::29.4:.0123 Mean 42 corr. .0123

Stand 31 M = 29.3877 log. . . . 4681656

Diff. 11 m = 25.19 log. . 4012282

435 : 11 :: 669.374 : 16.924 Corr. 16.924

The altitude sought 686.298 fathoms.

Let the state of the barometers and thermometers be as follows to find the altitude.

Thermometers.

Detached.
57
42

Attached.
57
43

Attached.
Lower 29.68
Upper 25.28
Altitude 719.897 fathoms.

The foregoing methods have been found from experience to give results tolerably correct in ordinary circumstances, though they deviate considerably from the truth in peculiar cases. To obviate this, as far as possible, we have given another method, which, it is hoped, will prove very accurate.

In this case let B be the height of the English barometer at the lower station, b that at the upper, t, the temperature by Fahrenheit at the lower, and t' that at the upper, L the latitude of the place of observation, f the elastic force of vapour at the lower, and f' that at the upper, and H the height of the one place above the other in feet, then

the upper, and if the neight of the one place above the other in rest, then
$$H = 60000 \left\{ \frac{\frac{t+t'}{2} - 32}{2} + \frac{32}{180} (1 + 0.00268 \cos. 2 L) \times \left(1 + \frac{f+f'}{B+b\{1+0.0001(t-t')\}}\right) \log \cdot \left(\frac{B-\{f'\}}{b\{1+0.0001(t-t')\}-\{f'\}}\right) \right\} \cdot (A)$$

$$\frac{t+t'}{2} - 32$$

The factors (1.375) 180 and 1+0.00268 cos. 2 L, may be reduced into tables; and, if given in logarithms, they will be very readily applied. If the centigrade thermometer be used, then

$$\mathbf{H} = 60345.6 \left\{ (1.375)^{\frac{t+t'}{200}} (1 + 0.00268 \cos 2 \mathbf{L}) = \left(1 + \frac{f + f'}{\mathbf{B} + b\{(+0.00018(t-t')\}} \log \left(\frac{\mathbf{B} - \mathbf{f}f}{b\{1 + 0.00018(t-t')\} - \mathbf{f}f} \right) \right\} (\mathbf{B})$$

In which case also B, b, f, and f' may be given in reference to the French standard metre.*

The log. of the constant 60000 feet may be employed with advantage, being 4.778151.

If Laplace's constant 18393 metres, or 60345.6 feet, be taken, the constant logarithm would be 4.780646, and the factor 1+0.00268 cos. 2 L must be used.†

^{*} See Biot's Traité de Physique, Tome I. p. 531.

+ As Laplace's constant is perhaps the more accurate, it may be used in both cases.

BAROMETRIC TABLES.

TABLE I.

TABLE OF THE DEPRESSION OF MERCURY IN GLASS TUBES.

Diam.	Ivory.	Depressions by Laplace.	Young.
In.	In.	In.	In.
0.05	0.29494		0.2964
0.10	0.14028	0.13940	0.1424
0.15	0.08628	0.08538	0 0880
0.20	0.05811	0.05798	0.0589
0.25	0.04075	0.04117	0.0404
0.30	0.02916	0.02965	0.0280
0.35	0.02110	0.02165	0.0196
0.40	0.01534	0.01591	0.0139
0.45	0.01117	0.01174	0.0100
0.50	0.00835	0.00868	0.0074
0.60	0.00443	0.00462	0.0045
0.70	0.00228	0.00244	
0.80	0.00119	0.00128	

This table is to be used only when two barometers, differing considerably in their internal diameters, are employed.

The expansion of the volume of mercury for 1° Fahr. = 0.000886, more correctly than 0.0001, though the difference in the nicest hard-metric observations is almost insensible.

TABLE II.

MR DALTON'S TABLE OF THE ELASTIC FORCE OF AQUEOUS VAPOUE.:

Barometer 30 Inches.

Temp.	Force.	Temp.	Force.	Temp.	Force.	Temp.	Force.	Temp.	Fores.
Fahr.	Inches of Mercury.	Fahr.	Inches of Mercury.	Fahr.	Inches of Mercury.	Fahr.	Inches of	Fahr.	inches of Mercury.
0∘	0.064	20	0.129	40	0.263	6 0	0.524	80	1.000
1	0.066	21	0.134	41	0.273	61	0.542	81	1.040
2	0.068	22	0.139	42	0.283	62	0.560	82	1.070
3	0.071	23	0.144	43	0.294	63	0.578	83	1.100
4	0.074	24	0.150	44	0.305	64	0.597	84	1.140
5	0.076	25	0.156	45	0.316	65	0.616	85	1.170
6	0.079	26	0.162	46	0.328	66	0.635	86	1.210
7	0.082	27	0.168	47	0.339	67	0.655	87	1.240
8	0.085	28	0.174	48	0.351	68	0.676	88	1.280
9	0.087	29	0.180	49	0.363	69	0.698	89	1.820
10	0.090	30	0.186	50	0.375	70	0.721	90	1.860
11	0.093	31	0.193	51	0.388	71	0.745	91	1.400
12	0.096	32	0.200	52	0.401	72	0.770	92	1.440
13	0.100	33	0.207	53	0.415	73	0.796	93	1.480
14	0.104	34	0.214	54	0.429	74	0.823	94	1.530
15	0.108	35	0.221	55	0.443	75	0.851	95	1.580
16	0.112	36	0.229	56	0.458	76	0.880	96	1.630
17	0.116	37	0.237	57	0.474	77	0.910	97	1.680
18	0.120	3 8	0.245	58	0.490	78	0.940	98	1.740
19	0.124	39	0.254	59	0.507	79	0.971	99	1.800

TABLE III.
LOGARITHMS OF THE BULK OF GAS,

From the formula $\frac{x}{180} \times \log$. 0.1383027, in which x is the number of degrees above 32° Fahrenheit.

emp.	Log. Bulk.	Temp.	Log. B.	Temp.	Log. B.	Temp.	Log. B.
09	1.975413	250	1.994622	50°	0.013830	75°	0.033039
ĩ	.976181	26 27	.995390	51	0.014599	76	0.033807
2	.976950	27	.996158	52	0.015367	77	0.034567
CH. 415	.977718	28	.996927	53	0.016135	78	0.035344
4	.978486	29	.997695	54	0.016904	79	0.036112
5	.979255	30	.998463	55	0.017672	80	0.036881
6	.980023	31	.999232	56	0.018440	81	0.037649
7	.980791	32	0.000000	57	0.019209	82	0.038418
8	.981560	33	0.000768	58	0.019977	83	0.039186
9	.982328	34	0.001537	59	0.020745	84	0.039954
10	.983096	35	0.002305	60	0.021514	85	0.040723
11	.983865	36	0.003073	61	0.022282	86	0.041491
12	.984633	37	0.003842	62	0.023050	87	0.042259
13	.935401	38	0.004610	63	0.023819	88	0.043028
14	.986170	39	0.005378	64	0.024587	89	0.043796
15	.986938	40	0.006147	65	0.025356	90	0.044564
16	.987706	41	0.006915	66	0.026124	91	0.045333
17	.988475	42	0.007683	67	0.026892	92	0.046101
18	.989243	43	0.008452	68	0.027661	93	0.046869
19	.989911	44	0.009220	69	0.028429	94	0.047638
20	.990780	45	0.009989	70	0.029197	95	0.048406
21	.991548	46	0.010757	71	0.029966	96	0.049174
22	.992317	47	0.011525	72	0.030734	97	0.049942
23	.993085	48	0.012294	73	0.031502	98	0.05071
24	.993853	49	0.013062	74	0.032271	99	0.051489

P. P. 1 2 3 4 5 6 7 8 9 to tenths 77 153 238 307 384 46I 538 615 691

TABLE IV. LOGARITHMIC VALUES OF 1 + 0.00268 cos. 2 L.

ias	Log.	Lat	Log.	Lat.	Log.	Lat.	Log.
.00	0.001162	13°	0.001045	26°	0.000716	399	0.000242
11	0.001162	14	0.001027	27	0.000684	40	0.000202
2	0.001160	15	0.001007	28	0.000651	41	0.000162
13	0,001156	16	0.000986	29 30	0.000617	42 43	0.000122
4	0.001151	17	0.000964	30	0.000582	43	0.000081
5	0.001145	18	0.000941	31	0.000546	44	0.000041
6	0.001138	19	0.000916	32	0.000510	45	0.000000
7	0.001129	20	0.000891	33	0.000473	46	9.999959
8	0.001118	21	0.000864	34	0.000434	47	9.999919
9	0.001106	22	0.000836	35	0.000398	48	9.999878
10	0.001093	23	0.000808	36	0.000360	49	9.999838
11	0.001078	24	0.000778	37	0.000321	50	9.999798
12	0.001062	25	0.000747	38	0.000281	51	9.999758

TABLE IV.—Continued.

Lat.	Log.	Lat	Log.	Lat.	Log.	Lat.	Log.
52°	9.999719	629	9.999349	720	9.999059	82°	9.998882
53	9.999679	63	9.999316	73	9.999036	83	9.998871
54	9.999640	64	9.999284	74	9.999014	84	9.998862
55	9.999602	65	9.999253	75	9.998993	85	9.998855
56	9.999566	66	9.999222	76	9.998973	86	9.998849
57	9.999527	67	9.999192	77	9.998955	87	9.998844
58	9.999490	68	9.999164	78	9.998938	88	9.998840
59	9.999454	69	9.999136	79	9.998922	89	9.998838
60	9.999418	70	9.999109	80	9.998907	90	9.998838
61	9.999383	71	9.999084	81	9.998894	[75 A)	The of Be

EXAMPLE I.

To determine the height the following observe feet.	ght of Arth ations, the	nur's Seat height by	above the levelling k	sea at Leith being 802.66
Leith Pier 29.567 Arthur's Seat 28.704	Att. ther. 55.25 51.75	Det. ther. 54°.0 50 .5	Dew point. 50°.0 48 .5	f = 0.375 f' = 0.357
Fah. ther. 54°.0 50 .5		×0.0001 × 8.704+0.0	3.5 = 0.010	f+f'=0.732 nearly, and =28.714
Sum 104.5 Consta	nt log. of	80000 feet	77 - 2000 10 - 10 - 10 - 10 - 10 - 10 - 10 - 1	4.778151
Half 52.25 log. B B=29.567, B= $\frac{1}{5}f$ =29.5 b =28.714, b= $\frac{1}{5}f$ =28.7	67-0.062	=29.505 log =28.655 log	g. 1.469895 g. 1.457201	0.015367 153 38
Difference .			0196041	- 100 tas
Difference	0 00	OF BOTH	.0120941	og. 2.103462
$1 + \frac{f + f'}{B + b} = 1 + \frac{0.732}{58.281} = \frac{1}{58.281}$	=1.01256 1	og.	10120941	0.006181 206
TRUSCERS INC. LOO		RAWS AND	CAPO	0.006181

[•] The t and t' in the denominators of the fractions in the formula should have been τ and τ' , the temperatures of the attached, to distinguish them from those of the detached thermometers.

100 FE 100 FE 100 FE

Laplace's constant log.	in feet .	•	4.780646
1 + 0.00268 cos. 2 L for	. 56° .	•	9.999566
Mean temperature 52.2	5 log. B .	•	0.01 <i>5367</i> 1 <i>5</i> 3
			38
Difference of logs of co	rrected altitudes, log.		2.103462
Difference of logs of co.	recent atmended roll.	•	138
1.01256 log.			0.005181
	•		206
			25
H = 803.12			2.904782
H'=802.66	•	•	70
			. —
Excess = 0.46 foot, or 5	inches		12
•	Example II.		
Required the height of		len above	Caernarvon
quay from the following a	set of observations?		
Bar.	Att. Ther.	Det. Ther.	Dew Point.
Caernarvon Quay 29.984	Att. Ther	55.25	. 50°.25
Snowden Peak 26.271	42.75 .	43.00	. 41 .00
Constant logarithm	·. ·		4.780646
Correction for latitude	53° 4′ .	•	9.999679
$\frac{55^{\circ}.25 + 43^{\circ}}{2} = 59^{\circ}.125 1$	og. B		0.013062
2	•		MH
$B = \frac{1}{6}f = 29.920 \log.$	1.475962		77 15
$b' = \frac{1}{6}f' = 26.262$	1.419328		4
·			31
Difference, .	0.056634 log		2.753047
Difference, $1 + \frac{f+f'}{B+b} = 1 + \frac{0.656}{56.18}$	$\frac{6}{100000000000000000000000000000000000$		0.004751
B+b 56.18	32 = 1.01100 log.	•	
			247
			33
H = 3561.2 feet			3.551592
H' = 3555.4		•	0.001001
Excess 5.8			
	Example III.		
Captain Sabine found	the height of a hill	at Spitzb	ergen, deter-
mined geometrically, to	be 1644 feet; requir	ed its heig	ht barometri-
cally from the following			
Observed height of the b		om.	
Barometer, (diam. of tul	in. In. ne 0.30) 29.6735	Attached	d ther. 39°.75
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Capacity	0.0561	Dew poi	nt. 34.00
Capillary action (Young) + 0.0280		niell's hygro-
Index	+0.1960	meter	· · · · · ·
	+0.1479	•	•
	T 0.12/9		
True height .	. 29.8214		

The second secon	10.4 354 lgml
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+0.0330	A LINE SEE THE
True height . 28.0405	
Constant logarithm	4.780646 9.998907 66
Difference 0.026806 log.	$\bar{2.428135}$
Mean temperature $\frac{34.9 + 35.5}{2} = 35.2 \log. B$	B. J. Phonager rough in c.
f+f' 0.214+0.225 0.439	153
$1 + \frac{f + f'}{B + b} = \frac{0.214 + 0.225}{57.86} = 1 + \frac{0.439}{57.86} = 1.00759 \log.$	0.003029
or gives a formula for the bacomeric measurepayet of	247
Bar. H = 1635 Geo. H = 1644	3.213488
Difference — 9 feet	
By another set of observations.	Manage and
	The second second
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Captain Sabine thinks there is some error in the second set of experiments, arising from the circumstance, that Mr Foster, his assistant, was obliged to hold the instruments to prevent their agitation by the wind.

It is proper to remark, that Captain Sabine finds 1644.58 for the first and 1630.66 for the second set of observations, as stated in the Philosophical Transactions of the Royal Society of London, but the particular formula he used is not mentioned. The usual formulæ given by Roy, Shuckburgh, and Laplace may give the height more near the geometrical method in certain cases, such as in a mean state of the atmosphere, than that which we have given, though there is no doubt but that the circumstances which have induced us to give a new method, involving considerations not usually attended to in such measurements, are more conformable to the laws of nature, and will in time become more accurate as those branches of physical science on which they depend are rendered more perfect.

The dew point is supposed to be found by Daniell's hygrometer. If that instrument is not at hand, the dew point may be found by two good thermometers, one of which has its ball covered with moistened tissue-paper, as proposed by Mr Anderson, Rector of the Academy of Perth, who also gives a formula for the barometric measurement of altitudes, in which in some of the corrections I have been antici-

pated.

Let F, the elastic force of vapour by Dalton's table be thus reduced to f according to the difference between the naked and covered thermometers, then $f = F - \frac{0.028 \delta t \times p}{30} = F - 0.00092 \delta t \times p$, in which

 ∂t is the difference between the temperatures of the thermometers, and p the barometric pressure.

Now let φ be the elastic force at the dew point, then

$$\varphi = \frac{f}{1 + 0.002084(t - t')} = \frac{F - 0.00092p t}{1 + 0.0021(t - t')} \text{ nearly}$$
 (1)

Here t', the temperature of the dew-point is unknown, but may be determined, first approximately from the numerator of the formula, and then substituted in the denominator, and a second approximation obtained, which will generally be sufficiently correct.

To exemplify this, let the thermometer with the dry ball show 60°F, and that covered with moistened tissue paper 51½

Now if the barometer be at 30.4 inches we have from the numerator of formula (1) $f = 0.524 - 0.00092 \times 81 \times 30.4 = 0.524 - 0.238 = 0.236$. This f corresponds, by the table of Dalton to 42° mearly, which being substituted for t' in the denominator of the formula

gives $\phi = \frac{0.286}{1+0.0021(60-42)} = \frac{0.286}{1.0378} = 0.2756$ which finally gives $t'=41^{\circ}.3$, the dew point. This is perhaps one of the best methods of determining the point of deposition, as the instruments are not, like the hygrometers of Deluc and Saussure, liable to be deteriorated by time, and besides, may still answer other purposes which none of the usual hygrometers can.

Cor.—From the same principles, may be derived a formula to determine the weight of moisture in 100 cubic inches of air or

 $W = \frac{0.6854 \, \phi}{1 + 0.0021 \, (t - 32)}$ at the freezing point. When $\phi = 2756$ and t' = 41.3 we get from the expression W = 0.1837 grains when the air is completely saturated with humidity. But when the temperatures are 60° and 41° the $W = \frac{0.1837}{1 + 0.0021 \, (60 - 41)} = 0.1767$ grains in 100 cubic inches. Perhaps this method may be conveniently compared with Mr Daniell's, to show their relative accuracy and consistency. It may be added, that Mr Dalton states from experiments at moderate heights, that an elevation of 240 feet gives a depression of 1° temperature Fah. and an elevation of 390 feet gives a depression of 1° F. of the dew point. Hence, if t be the temperature and D the dew point

$$\Delta t = \frac{\Delta H}{240}$$
, and $\Delta D = \frac{\Delta H}{390}$.

Method IV.

For ordinary heights, such as those usually met with in Britain, the following method, requiring no tables, which is somewhat simpler and more easily recollected than Dr Robison's, is subjoined.

Let B be the barometric altitude at the lower situation, and b that at the upper corrected for the difference of temperature in the usual manner, the atmosphere being in its mean state with regard to aqueous vapour, &c.

Then H=13100
$$\frac{(B+b)(B-b)}{Bb}$$
 {1+0.00245($\frac{t+t'}{2}$ -32°)} in feet.

Bar. in. Att. Ther. Det. Ther.
$$Ex$$
.—Leith Pier 29.567 $55^{\circ}\frac{1}{4}$ 54° Arthur's Seat 28.704 $51\frac{3}{4}$ $50\frac{1}{4}$ $28.704 \times 0.0001 \times 3.5 = 0.010$, and $28.704 + 0.010 = 28.714 = 6$

$$1+\left(\frac{54+50\frac{1}{2}}{2}-32^{\circ}\right)\times0.00245=1+20\frac{1}{4}\times0.00245=1.04961$$
, hence

$$H=13100 \times \frac{58.281 \times 0.853}{29.567 \times 28.714} \times 1.04961 = 805 \text{ feet.}$$

Height by levelling . 803

Examples for Exercise.

2 feet.

- 1. If the base of an oblique-angled plane triangle be 40, and the other two sides 20 and 30, what is the length of the perpendicular?

 Ans.—14.52369.
- 2. If the base of a plane triangle be 40, and the other two sides 20 and 30, what are the segments of the base made by a line bisecting the vertical angle?

 Ans.—24 and 16.

3. The hypotenuse of a right-angled triangle is 19630040, and one of the legs 19630000; required the two acute angles?

Ass.—6' 56".4, and 89° 53' 3".6.

Difference

- 4. If the sides of a plane triangle be in proportion to each other as the numbers \(\frac{1}{2}\), \(\frac{1}{2}\), and \(\frac{1}{2}\); what are the angles?

 Ans.—117° 16′ 46″, 36° 20′ 10″, and 26° 23′ 4″.
- 5. At the Observatory on the top of the Calton-hill, 350 feet above the sea at Leith, the angle of depression of the horizon marked by

the sea down the frith of Forth was 18' 12" by observation. Now supposing the effect of refraction to be one-twelfth part of the whole, this must be increased by one-eleventh of itself, or the true depression would be 19' 51".28. Required the earth's diameter?

Ans.-7946 miles.

6. Suppose the height of Melville's Monument, in St Andrew's Square, Edinburgh, to be 60 feet, and that the figure placed upon the top of it is 12 feet high, at what distance from the monument may the statue be viewed under an angle of 3°, and what is the greatest angle under which it can be seen?

Ans.—It will be seen, under an angle of 3°, at the distance of 208.23, or 20.75 feet, and the greatest angle under which it can be

seen from a point in the horizontal plane is 5° 13'.

7. It is required to find the distances from the Edystone light-house to Plymouth, Start Point, and the Lizard respectively from the following data:

		th to Lizar		1
The distances from		to Start Poi		miles.
	Start P	oint to Plyr	nouth 20)
Plymouth)	•	•	(North	
Lizard >	bears from	n Edystone	: ≺ W. S. ¹	W.
Start Point			E. by I	N.
,	(Lizard	53.04)	,
Ans.—From Edys	stone to 🖁	Plymouth	14.33	miles.
•	and the state of t	Start	17.36	1,11
8. Barometers.	Therm	ometers.	Required	the Altitude. "
Lower 29.45	Attach.	Detach.		9.61 fathoms,
Upper 26.82	38	31	or 2458	feet, by Hut-
**	41	35	ton's m	
	• •			

EXAMPLES BY THE FRENCH MEASURES.

Observer Humboldt.	. Height of Barometer.	Attached Thermometer.	Detached Thermometer.	Dew Point.	Latitude,
	0=.509818 0 .762944		18°.75 cent. 25 .30	16°.0 cent. 20 .0	5° 0 N. H=3543***
	0377275 0 .762000		— 1°.6 cent. +25 .3		1° 45′ N. H=5925°

Calculation of the last Example by Method III.

Constant 18393 met	•	•	•	4.264653
$(1.375)^{\frac{11.33}{100}} = \frac{11.88}{100}$	$\frac{5}{0} \times 0.138303 =$	•	•	0.016389
Latitude 1° 45' log.				0.001161
$B = \frac{1}{6} f = 0.759114$	log. 1.880307			
b = 1 f' = 0.377471	log 1.576884			
Difference	0.303423 log.	•		ī.482048
$1 + \frac{f + f'}{B + b} = 1 + \frac{0.05}{1.15}$	$\frac{22373}{86585} = 1.019686$	•		0.008467

H=5925.4 metres 3.772718 Or 19441 English feet, the height of Chimborazo above the level of the Pacific Ocean.

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Chipper Law Stelling SPHERICAL TRIGONOMETRY.

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Definitions, Principles, and General Properties.

1. Spherical Trigonometry is that branch of mathematics by which we are enabled, in all cases, where three of the six parts of a triangle formed by arcs of great circles in the surface of a sphere are given,

to compute or determine the other three.

2. In plane trigonometry the knowledge of the three angles is not sufficient for ascertaining the sides; for in that case the relations only of the three sides can be obtained, and not their value; whereas, in spherical trigonometry, when the sides are circular arcs, whose value depends on their proportion to the whole circle, that is, on the number of degrees they contain, the sides may always be determined when the three angles are known. Among other remarkable differences between plane and spherical triangles are,

(1.) That in the former, two known angles always determine the

third; while in the latter they never do.

(2.) The surface of a plane triangle cannot be determined from a knowledge of the angles alone; while that of a spherical triangle always can.

3. A sphere or globe is a round body formed by the revolution

of a semicircle about its diameter, which remains fixed.

4. The centre of the sphere is the same with that of the revolving semicircle.

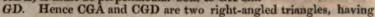
5. The axis of the sphere is the straight line about which the semicircle revolves.

PROPOSITION I.

6. If a sphere be cut by a plane, the section will be a circle. Let the sphere AEBF be cut by the plane ADB; then will the

section ADB be a circle. Draw the chord, or diameter of the section AB, perpendicular to the section ADB, and through the centre C draw the axis of the sphere ECGF, which will (Euc. III. 3.) bisect the chord AB in the point G. Also, join CA, CB; and draw CD, GD, to any point D in the perimeter of the section ADB.

Then, because CG is perpendicular to the plane ADB, it must be perpendicular both to GA and



the perpendicular CG common, and the hypotenuse CA equal to the hypotenuse CD, being both radii of the same sphere; therefore their third sides GA, GD, are also equal. In like manner, it may be shown, that any other line drawn from G to the circumference of the section ADB, is equal to GA, or GB; and consequently that section is a circle.

Cor.—If a sphere be cut by a plane through the centre, the section is a circle, having the same centre with the sphere, and equal to the circle by the revolution of the half of which the sphere was described. For all the straight lines drawn from the centre to the surface of the sphere are equal to the radius of the generating semicircle. Therefore the common section of the spherical surface, and of a plane passing through its centre, is a line lying in one plane, having all its points equally distant from the centre of the sphere, and is consequently the circumference of a circle, having for its centre the centre of the sphere, and for its radius, the radius of the sphere, that is, of the semicircle by which the sphere is described. It is therefore equal to the circle of which that semicircle is a part.

7. Any circle formed from the section of a sphere, by a plane

through its centre, is called a great circle of the sphere.

Cor.—All great circles of the sphere are equal; and any two of

them bisect each other.

They are all equal, because they have all the same radii, as has just been shewn, and any two of them bisect one another; for, as they have the same centre, their common section is a diameter of both, and therefore bisects both.

8. The pole of a great circle of the sphere is a point in the surface of the sphere equidistant from every part of the circumference of

that circle.

9. A spherical angle is an angle on the surface of a sphere contained by the arcs of two great circles which intersect each other, and is the same as the inclination of the planes of, or tangents at the point of intersection to, these great circles.

10. A spherical triangle is a figure on the surface of a sphere formed by the intersection of three arcs of great circles, each of which is

less than a semicircle.

11. A right-angled spherical triangle has one right-angle; the sides about the right-angle are called legs, and that opposite the right-angle is called the hypotenuse.

12. A quadrantal spherical triangle has one side equal to a qua-

drant, or 90°.

13. An oblique-angled spherical triangle has none of its angles

14. Spherical triangles are also called equilateral, isosceles, or soalene, according as they have three sides equal, two sides equal, or all the three sides unequal.

15. Two arcs, or angles, when compared together, are said to be alike, or of the same affection, when both are less, or both are greater than 90°. But when one is less, and the other greater than 90°, they are said to be unlike, or of different affections or characters.

16. Every spherical triangle has three sides and three angles;

[·] Hence the intersections of the circumferences of two great circles are two points. diametrically opposite to each other.

and if any three of these six parts be given, the other three may be found.

17. A lune is a part of the surface of a sphere contained by the semicircumferences of two great circles.

18. A small circle of the sphere is that whose plane does not pass

through the centre of the sphere.

19. The small circles of the sphere do not fall under the consideration of spherical trigonometry, but such only as have the same centre with the sphere itself. And hence it is that spherical trigonometry is of so much use in practical astronomy, the apparent heavens assuming the shape of a concave sphere whose centre is the same as the centre of the earth.

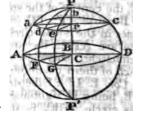
20. The sides of a spherical triangle are all arcs of great circles, which, by their intersection on the surface of a sphere, constitute

that triangle.

21. If ABDG be a great circle of the sphere whose centre is C and PCP a diameter of the sphere perpendicular to its plane, the points P, P' are the poles of that circle. And if the small circle abcd be perpendicular to PP', we call P, P' the poles of that small circle also.

22. The great circles PAP', PGP', passing through the poles P, P' of the great circle ABDG, are called secondaries to that

circle.



PROPOSITION II.

23. If two arcs of circles meet each other they make two angles,

Which are together equal to two right-angles.

Let the arc AB meet the arc CD in the point B; then will the two angles ABC, ABD be equal to two right-angles. For, suppose the arc BE to be perpendicular to CD, then the angles EBC, EBD are right-angles.

And since the angle EBD is equal to the angles C EBA, ABD, the three angles, ERC, EBA, ABD,

are equal to the two right-angles.

But the two angles, EBC, EBA, are equal to the angle ABC; whence the two angles, ABC, ABD, are also equal to two right-angles.

Proposition III.

24. If two arcs of a circle intersect each other, the vertical, or opposite angles, will be equal.

Let the two arcs, AB, CD, intersect each other in B, then will the angle AEC be equal to DEB, and

AED to CEB.

For since the arc AE meets the arc CD, the angles AEC, AED are together equal to two right-angles, (Prop. II.)

And because the arc DE meets the arc AB, the angles DEB, DEA are also equal to two right-angles.

Taking away from each the common angle AED, and the re-



maining angle, AEC will be equal to DEB. In the same manner

it may be proved that the angle AED is equal to CEB.

Cor.—Hence if any number of arcs of circles intersect each other, all the angles formed about the point of intersection are together equal to four right-angles.

PROPOSITION IV.

25. The arc of a great circle, between the pole and the circum-

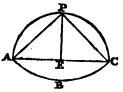
ference of another great circle, is a quadrant.

Let ABC be a great circle, and P its pole; if PC, an arc of a great circle, pass through P and meet ABC in C, the arc PC is a quadrant.

Let the circle, of which PC is an arc, meet ABC again in A, and

let AC be the common section of the planes of these great circles, which will pass through E, the centre of the sphere: Join PA, PC.

Because AP=PC, (def.), and equal straight lines in the same circle, cut off equal arcs, the arc AP = the arc PC; but APC is a semicircle, therefore the arcs AP, PC, are each of them quadrants.



Cor. 1. If PE be drawn, the angle AEP is a right-angle; and PE, being at right-angles to every line it meets with in the plane of the circle ABC, is at right-angles to that plane. Therefore the straight line drawn from the pole of any great circle to the centre of the sphere is at right-angles to the plane of that circle; and, conversely, a straight line drawn from the centre of the sphere perpendicular to the plane of any great circle, meets the surface of the sphere in the pole of that circle.

Cor. 2. The circle APC has two poles, as has been shewn in art. 21., one on each side of its plane, which are the extremities of a diameter of the sphere perpendicular to the plane APC; and no

other points but these can be poles of the circle APC.

PROPOSITION V.

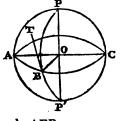
26. If the pole of a great circle be the same with the intersection of other two circles, the arc of the first circle intercepted between the other two, is the measure of the spherical angle which the same two circles make with one another.

Let the great circles AP, BP, on the surface of the sphere of

which the centre is O, intersect each other in P, and let AB be an arc of another great circle of the pole as P, AB is the measure of

the spherical angle APB.

Join PO, AO, BO; since P is the pole of AB, PA, PB are quadrants, and the angles POA, POB are right; therefore the angle AOB is the inclination of the planes of the circles PA, PB, and is equal to the spherical angle APB; but the arc AB measures the angle AOB therefore it also measures the spherical or



AOB, therefore it also measures the spherical angle APB.

Cor. If two arcs of great circles, PA, PC, which intersect each other in P, be each of them quadrants, P will be the pole of the

great circle which passes through A and B, the extremities of those arcs. For since the arcs PA and PB are quadrants, the angles POA, POB are right-angles, and PO is therefore perpendicular to the plane AOB, that is, to the plane of the great circle which passes through A and B. The point A, therefore, is the pole of the great circle which passes through A and B. make the arc PB at B is at right-angles to AB at II

Proposition VI.

27. An angle made by any two great circles of the sphere is equal to the angle of inclination of the planes of these circles.

Let BAE be a spherical angle made by two great circles CBA,

CEA; then will this angle be equal to the angle of inclination of the planes of those circles. For, take the arcs AB, AE, each equal to 90°, or a quadrant, and through the points B, E draw the arc of the great circle BE, and from D, the centre of the sphere, draw DB, DE.

Then, because AB, AF are quadrants, A and C are the poles of the circle of which BE is a part, and the lines DB, DE are each perpendicular to the common section AC; consequently BDE is the angle of inclination of the planes CBA, CEA. But since DB, DE are equal, being radii of the same sphere, the angle BDE, which is measured by the arc BE, is equal to the

angle BAE, which is measured by the same arc.

And if FH be drawn in the plane CBA, and FG in the plane CEA, each perpendicular to the common section AC, the angle HFG, which is equal to the angle BDE, will also be equal to the angle BAE.

Cor. The angle BAE made by two great circles of the sphere BA, EA, is equal to the angle n A m, formed by two tangents drawn from the angular point A, one in each plane, these tangents being each perpendicular to the diameter AC.

PROPOSITION VII.

28. The distance of the poles of any two great circles of the sphere is equal to the angle of inclination of the planes of those circles.

Let AEB, CED be two great circles, and P, P' their poles; then will the arc PP' be equal to the angle of their

inclination AOC or BOD.

amothew, cach to each.

For, since P is the pole of the circle AEB, and P' of CED, the arc PA will be equal to PC, being each quadrants, or 90°; and if PC, A which is common to each, be taken away, the remaining arc, PP', which is the distance of two poles, is equal to CA, the measure of the angle of inclination ACC the angle of inclination AOC. The sade and the and growth one spherical triangle be

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PROPOSITION VIII.

29. The circumference of a secondary is at right angles to the circumference of its great circle at the point of intersection. The direction of the circumference of a great circle at any point being the same as the diameter of its tangent at that point, the angle OBT, (figure prop. V.), is a right-angle, BT being a tangent to BP at the point B. POB is also a right-angle, and the arc PB is in the plane POB, therefore the direction of the circumference PB at B must be parallel to PO. But PO is perpendicular to the circle ABC; therefore the circle PBP' is at B perpendicular to the circle ABC; hence the arc PB at B is at right-angles to AB at B. For the same reason PAB is also a right-angle.

Cor. 1.—If a great circle, PBP, be perpendicular to ABC, and

BP, BP' be taken each equal to a quadrant, or 90°, P, P' are the

poles of the circle ABC.

Cor. 2.—If any two great circles, PAP', PBP', be perpendicular to the circle ABC, they meet at the poles P, P of that circle.

PROPOSITION IX.

30. In an isosceles spherical triangle the angles at the base are equal. Let ABE (figure prop. VI.) be a spherical triangle, having the side AB equal to the side AE, the spherical angles ABE, ABE are equal.*

Cor. 1.—Hence, if two of the angles of a triangle be equal, the

sides opposite to them are likewise equal.

Cor. 2.-A perpendicular drawn from the vertex of an isosceles spherical triangle to the base, bisects both the base and the vertical angle, except when the two sides are quadrants; in which case there are an indefinite number of perpendiculars.

PROPOSITION X.

31. If the three sides of one spherical triangle be equal to the three sides of another, each to each, the angles which are opposite the equal sides are equal.

PROPOSITION XI.

32. If two sides and the included angle of one spherical triangle be equal to two sides and the included angle in another, these two tr ingles are equal.

PROPOSITION XII.

33. If from the angles of a spherical triangle, as poles, there be described on the surface of the sphere three arcs of great circles, which, by their intersections, form another spherical triangle, each side of this new triangle will be the supplement of the measure of the angle which is at its pole, and the measure of each of its angles the supplement to that side of the primitive triangle to which it is opposite.

Proposition XIII.

34. If the three angles of one spherical triangle be equal to the three angles of another, each to each, the sides which are opposite to the equal angles are equal.

Proposition XIV.

35. If a side and two adjacent angles of one spherical triangle be equal to a side and two adjacent angles of another, each to each, their remaining sides and angles will be equal.

The demonstrations, which may be seen in Playfair's or Legendre's Geometry, are omitted, as they would swell this work too much, but may perhaps appear in a more complete treatise on trigonometry that has been long meditated.

Proposition XV.

36. The sum of any two sides of a spherical triangle is greater than the third side; and the difference of any two sides is less than the third side.

Cor.—The shortest distance between any two points on the surface of a sphere is the arc which passes through these points.

Proposition XVI.

37. The greater side of any spherical triangle is opposite to the greater angle, and the less side to the less angle.

And, in a similar manner, it may be shown that the less side is opposite to the less angle, and the less angle to the less side.

Proposition XVII.

38. The sum of the three sides of any spherical triangle is less than the circumference of a circle, or 360°; and the difference of any two sides is less than 180°.

PROPOSITION XVIII.

39. The sum of the three angles of every spherical triangle is greater than two right-angles, or 180°, and less than six, or 540°.

Cor.—The sum of any two angles of a spherical triangle is great-

er than the supplement of the third angle.

For the angles A+B+C, being greater than two right-angles, or than ACB+ACG, if ACB or C be taken away, the sum of the remaining angles A+B, will be greater than ACG.

PROPOSITION XIX.

40. If the sum of any two sides of a spherical triangle be equal to, greater, or less than a semicircle, the sum of their opposite angles will, accordingly, be equal to, greater, or less than two right-angles; and conversely.

And, in a similar manner, it may be shown, that if the sum of the two angles B and C be equal to, greater, or less than 180°, the sum of the opposite sides AB and AC, will also be equal to, greater, or

less than 180°.

Cor. 1.—If each side of a spherical triangle be equal to, greater, or less than 180°, each of the angles will, accordingly, be right, obtuse, or acute; and conversely.

Cor. 2.—Half the sum of any two sides of a spherical triangle is

of the same kind as half the sum of their opposite angles.

Proposition XX. 41. In any right-angled or quadrantal spherical triangle, the legs or sides are of the same kind or affection as their opposite angles,

and conversely.

The same will also hold if the triangle be quadrantal; for its sides and angles being the supplements of the angles and legs of the polar triangle, which in this case is right-angled, the similarity will be the same as before.

PROPOSITION XXI.

42. In any right-angled spherical triangle the hypotenuse is less or greater than 90°, according as the two legs, or the two angles, or a leg and its adjacent angle, are alike or unlike.

SECTION II.

Solution of Spherical Triangles.

HAVING given a view of the general principles and properties of spherical triangles, the solution of the various problems in spherical trigonometry ought necessarily to follow. These problems may be resolved either by geometrical construction or by arithmetical calculation. There are various methods of construction, but the most simple, and generally employed, is the stereographic, in which all the circles of the sphere are represented by straight lines or circles.

Of the Stereographic Projection of the Sphere.

DEFINITIONS.

I. To project an object, as it is commonly called, is to represent every point of that object upon the same plane, as it appears to the eye in a certain position.

II. That plane upon which the object is projected is called the plane of projection, and the point where the eye is situated, the pro-

jecting point.

III. The stereographic projection of the sphere is that in which a great circle is assumed as the plane of projection, and one of its poles as the projecting point.

IV. The great circle, upon the plane of which the projection is

made, is called the primitive.

V. By the semitangent of any arc is meant the tangent of half

that arc

VI. The line of measures of any circle of the sphere is that diameter of the primitive, produced indefinitely, which is perpendicular to the line of common section of the circle and the primitive.

VII. The projection, or representation of any point in the sphere, is the point in which the straight line drawn from it to the project

ing point intersects the plane of projection.

THEOREM J.

Every great circle of the sphere, which passes through the projecting point, is projected in a straight line, passing through the centre of the primitive; and every arc of it, reckoned from the other pole of the primitive, is projected into its semitangent.*

Cor. 1 .- Every small circle, which passes through the projecting point, is projected into that straight line which is its common section.

with the primitive.

Cor. 2.—Every straight line in the plane of the primitive, and produced indefinitely, is the projection of some circle on the sphere passing through the projecting point.

Cor. 3.—The stereographic projection of any point on the surface

The second second second second second For the investigation of the properties of this method of projection, see Gregory's or Keith's Treatises of Trigonometry, and West's Mathematics.

of the sphere, is distant from the centre of the primitive by the semitangent of the distance of that point from the pole opposite the projecting point.

THEOREM II.

Every circle of the sphere, which does not pass through the projecting point, is projected into a circle.

Cor. 1.—The centres and poles of all circles parallel to the primi-

tive, have their projections in its centre.

Cor. 2. The centre and poles of every circle, inclined to the pri-

mitive, have their projections in the line of measures.

Cor. 3.—All projected circles cut the primitive in two points diametrically opposite.

THEOREM III.

The centre of the projection of a great circle is distant from the centre of the primitive by the tangent of the inclination of the great circle to the primitive, and its radius is the secant of the same.

THEOREM IV.

The centre of projection of a small circle, perpendicular to the primitive, is distant from the centre of the primitive by the secant of the distance of the circle from its nearest pole, and the radius of projection is the tangent of the same.

THEOREM V.

The projections of the poles of any circle inclined to the primitive, are in the line of measures distant from the centre of the primitive by the tangent and cotangent of half its inclination.

THEOREM VI.

Any two circles upon the sphere, passing through the poles of two great circles, intercept equal arcs upon them.

THEOREM VII.

If, from either pole of a projected great circle, two straight lines be drawn to meet the primitive and the projection, they will intercept corresponding arcs of these circles.

Solution of Right-Angled Spherical Triangles.

The solution of right-angled spherical triangles may be accomplished by formulæ investigated expressly for that purpose. We are indebted to Napier, however, for a comprehensive rule of great advantage to the memory, by reducing all the theorems employed in the solution of right-angled triangles to two. This is called the rule of the circular parts, and is perhaps one of the happiest examples of artificial memory that is known.

DEFINITIONS.

I. If in a right-angled spherical triangle the right-angle be set aside, and the five remaining parts of the triangle alone be considered, consisting of the three sides, and the two oblique angles, then, the two sides containing the right-angle, and the complements of the other three, namely, of the two angles, and of the hypotenuse.

are called the circular parts.

II. When, of the five circular parts, any one is taken for the middle part, then, of the remaining four, the two which are immediately adjacent to it on the right and left are called adjacent parts: and the other two, each of which is separated from the middle part by an adjacent part, are called opposite parts.

This arrangement being made, the solution is obtained by the fol-

lowing

THEOREM.

In any right-angled spherical triangle, the rectangle under the radius, and the sine of the middle part, is equal to the rectangle under the tangents of the adjacent parts; or to the rectangle under the co-SINES of the opposite parts.

This theorem, or rule, may be easily remembered, by remarking, that the first vowels in sine, tangent, cosine, are respectively the same

as the first in middle, adjacent, opposite,

or, $R \times \sin$ mid=rect. tan adj. = rect. cos. op.

It is usual to convert the equation under consideration into an analogy having the unknown quantity for the last term, though, to those acquainted with algebra, it would be more convenient to make it alone the first term of an equation, and the remaining terms, combined properly according to the rules of algebra, the last.

PROBLEM I.

Given three of the six parts, as, for example, the hypotenuse and one of the angles of a right-angled spherical triangle, to find the sides and the remaining angle.

On the first of May 1826, the sun's longitude was 1 10° 32′ 12′, and the obliquity of the ecliptic 23° 27′ 40"; required the right as-

cension and declination?†

Ans.—R. A. 2^h 32^m 27'.3; dec. 14° 59′ 47″ N.

Construction.—With the chord of 60° describe the primitive circle EPQP' on the plane of the solstitial colure, and draw the diameters EQ and PP' at right-angles to one another, then ? will EQ represent the equator, and PP the E polar axis. Lay off from the same line of chords I $\to e=23^{\circ} 27' 40''$, the obliquity of the ecliptic,

ecliptic, at right-angles to which draw p p',

roles of the ecliptic. From the line of semitangents, (Theorem I.), lay off the sun's longitude 1° 10° 32′ 12″, or 40° 32′.2 on the ecliptic, from A to C, then C will be the place of the sun, and scm a parallel of declination. Through the points PCP' draw a circle of right ascension, cutting the equator EQ

(1)

[•] Should either of the oblique angles, or hypotenuse, be one of the parts, then, instead of the word in the fermula, use that derived from its complement, that is, for sine read cosine, for cosine read sine, and so on.

+ For the explanation of these terms the usual treatises on astronomy may be consulted. To those acquainted with the use of the globes, correct ideas relative to these problems may be readily obtained. It may be added, that the sun's longitude, and the shifted of the clinitic are computed from astronomical tables. obliquity of the ecliptic, are computed from astronomical tables.

at right-angles in B, then will AB be the right ascension, BC the declination, and BCA the remaining angle or angle of position, as it is sometimes called, which, in astronomy, is seldom of much use.

Calculation.—In the triangle ABC there are given AC=40° 32′ 12″, and the angle BAC=23° 27′ 40″, to find BC, the distance of the sun from the equator EQ, or the declination, as it is usually called. Now, since in spherical trigonometry the sines of the sides are proportional to the sines of their opposite angles, Therefore.

As sine Is to sine So is sine	ABC o	23°	27'	40"	•		٠	10.000000 9.600021 9.812870
To sine	BC	14	59	47				9.412891

To find AB we may employ the method of the circular parts. In the triangle ABC are given AC and the angle BAC, to find AB the right ascension. Now, since the side CA, the angle CAB, and the side AB are all connected, that which stands in the middle or the angle A is called the middle part, and the sides AC and AB adjacent to it on each side are called the adjacent parts.*

Consequently $R \times \cos$. $A = \cot$. $AC \times \tan$. AB; and resolving this into an analogy, as is frequently done in this country, we have,

As cot. AC	40° 32′ 12″	•	10.067939
Is to radius		•	10.000000
So is cos. A	23 27 40		9.962526
	a) aa- am a		
To tan. AB.	2 ^h 32 ^m 27·.3	•	9.894587

or, since cot.: R:: R: tan., or tan.=\frac{1}{\cot.} to radius unity (\sqrt{35}, page 11.)

As radius Is to tan. AC	40° 32′ 12″	•	•	10.000000 9.932061
So is cos. A	23 27 40	• •	•.	9.962526
Totan AB	Oh 20m 04 2			0.004507

To tan. AB 2^h 32^m 27.3 . . 9.894587 the same as before.

To those acquainted with algebra, it is better, after the manner of foreign mathematicians, still to retain the form of an equation thus:

tan. $AB = \frac{R \times \cos. A}{\cot. AC} = \cos. A \times \tan. AC$, the radius being represented by unity; in which case ten must be rejected in the index.

To log. cos. Add log. tan.	A AC	23° 40	27′ 32	40″ 12		. •		9.962526 9.932061
Sum tan.	AB	2 ^h	32 ^m	27.:3	•			9.894587

To find the angle ACB, since the parts under consideration are still all connected, AC standing in the middle is assumed as the middle part, and the angles A and C are the adjacent parts, whence

[•] It may be remarked, that if the parts are all connected, that which stands in the middle is called the middle part, and the other two are called the adjacent parts. If two only are connected, and one stands by itself, then this is called the middle part, and the other two are called the opposite parts.

 $R \times \cos$. $AC = \cot$. $A \times \cot$. C, and \cot . $C = \frac{\cos$. $AC}{\cot$. $AC \times \tan$. A, hence To log. cos. AC 40° 32′ 12" 9.880808 Add log. tan. A 23 27 40 9.637496 71 44 42 .2 9.518304 Sum = cot. C18 15 17 .8, is called properly the angle of posi-Or the comp. tion, sometimes useful in computing the parallaxes in solar eclipses

and occultations of the fixed stars and planets by the moon. By assuming different parts of the triangle ABC for the middle

part, may be resolved the following

Examples for Exercise.

1. On the first of June, 1827, at noon on the meridian of Greenwich, the sun's longitude will be 2 10 9' 45", the obliquity of the ecliptic 23° 27′ 36″; required the right ascension and declination?

Ans.—R. A. 4^h 34^m 7.6; Dec. 21° 59′ 34″ N.

2. August 12th, 1827, the obliquity of the ecliptic being 23° 27' 36", the sun's right ascension will be 9h 25m 29.3; required his longitude and declination?

Ans.—Longitude 4 18 56 28", Dec. 15 9 32" S.

3. On the 10th November, 1828, on the meridian of Greenwich, the sun's right ascension will be 15^h 2^m 32.7, and declination 17° 14' 12" S.; required the sun's longitude and the obliquity of the ecliptic?

Ans. Longitude 7' 18' 6' 7", and obliquity of the ecliptic 23°

27' 34".

4. On the 2d of March, 1828, when the sun's declination was 7° 5′ 18" S., and obliquity of the ecliptic 23° 27′ 35"; required his longitude and right ascension?

Ans.—Longitude 11° 11° 56′ 34″; R. A. 22° 53° 24°.

PROBLEM II.

When the celestial object is not upon the ecliptic, as the moon, or the planets, and some of the fixed stars, the right ascension and declination are found by the solution of two right-angled triangles.

1. On the 17th of January, 1826, at noon, on the meridian of Greenwich, the moon's longitude was 1' 11° 5' 14", and her latitude 2° 34′ 3″ N.; required her right ascension and declination, the obliquity of the ecliptic being 23° 27′ 40″? To resolve this example it is necessary to employ two right-angled spherical triangles.

In the foregoing figure, the longitude of the moon or any star S, is AD, the latitude DS, the obliquity of the ecliptic BAC, the right ascension AB and declination BS. Now, supposing a line drawn from A to S, there would be formed the right-angled spherical triangle ADS, right-angled at D, of which AD and DS are given to find the angle DAS and the side AS. If the position S of the star is without the ecliptic, then to the obliquity of the ecliptic BAC, add the angle DAS, the sum will be the angle BAS; but if S is within the ecliptic, that is between it and the equator, subtract the angle DAS from the obliquity BAC, and the remainder will be the angle BAS. Since the side AS, and the angle BAS, are now known, AB the right ascension, and BS the declination, may be found.

Calculation.—By the rule of the circular parts, first AD and DS

are given to find AS, and since the last is separated from the two
first by the oblique angles, it will be the middle part, and AD and
DS are the opposite parts; therefore, $R \times \cos$. AS = \cos . DS $\times \cos$.
AD, or cos. $AS = \cos$. DS $\times \cos$. AD to radius unity.

To log. cos. DS. 2° 34′ 3″		04 3	2	E2 / 100	9.999564
Add log. cos. AD 41 5 14				*	9.877204
Towns AC AL DIAL	- 0	- HI - 1	90	12 9 1	0.076760

Again, to find DAS, since the right angle does not separate the parts, DA standing in the middle is called the middle part, and the side DS and the angle DAS are the adjacent parts, hence Rxsin.

 $DA = tan. DS \times cot. DAS$, and, therefore, cot. $DAS = \frac{sin. DA}{tan. DS} =$

sin. DA × cot. DS, consequently To log. cot. DS 2° 34′ 3″ Add log. sine DA 41 5 14	11.348322 9.817634
Sum=log, cot. DAS 3 54 14	11.165956

Sum = angle BAS 27 21 54

Hence AS and BAS are now known, to find AB and BS.

First to find AB. In this case the parts are connected; therefore BAS is the middle part, and AB and AS are the adjacent parts, whence

 $R \times \cos$. BAS = tan. AB × cot. AS, or tan. AB = $\frac{\cos$. BAS, and

tan, AB = cos. BAS x tan. AS, hence	
To log. cos. BAS 27° 21′ 54″	9.948460 9.941505
Sum = log. tan. AB 37° 49′ 5″ Or in time R. A. 2° 31° 16°.3	9.889965

To find BS, the angle BAS and side AS are connected, and BS is disjoined, whence $R \times \sin$. BS = \sin . AS $\times \sin$. BAS, or since the sines of the sides are proportional to the sines of their opposite angles.

As sine ABS or	radius	II II a	m.di	- Paradi	0	advo ad	10.000000
Is to sine AS	410 9	1"	might	n vad Jo		417 In	9.818274
So is sine BAS	27 21	54	2 10	Supple 3	STO	1000	9.662434
To sing Dog BS	17 26	96 N	200	E STORA ST		DEREN	0.490709

The foregoing method is general and applicable to any part of the ecliptic, provided proper attention be paid to the situation of the celestial object with respect to the ecliptic and equator. As this problem and its converse is of frequent occurrence in practical astronomy, rules and formulæ, and even tables, have been formed for the purpose of facilitating the computations. The following rules, given by the late Dr Maskelyne, will be found very convenient for this purpose.

PROBLEM II.

Given the right ascension, the declination, and the obliquity of the ecliptic, to find the longitude and latitude.

Let RA denote the right ascension, O the obliquity of the ecliptic, and D the declination.

Tan. D-sin. RA = tan. A, North or South as the declination is. Call O in the first six signs of RA South or S. and in the last six signs North or N.

Then A+O=B, regard being had to the algebraic signs,

A being less than 45°, and using logarithms. Sec. A+cos. B+tan. RA = tan. lon. of the same kind as RA, unless B be more than 90°, when the quantity found of the same kind as RA must be taken from twelve signs.

A being more than 45°.

Tan. $A + \csc$. $A + \cos$. $B + \tan$. $RA = \tan$. lon. of the same kind as RA, unless B be more than 90°, when the quantity found of the same kind as RA must be taken from twelve signs.

Lon. being nearer III. and IX. signs than O and VI. signs.

Sin. lon. + tan. B = tan. lat. of the same name as B. Lon. nearer O and VI. signs, than III. and IX. signs.

Tan. Lon. $+\cos$ lon. $+\tan$ B = \tan lat. of the same name as B.

EXAMPLE.

On Monday the 12th of June, 1826, the moon's R A at noon, was found by observation to be 10^h 39^m 31° and her declination 2° 51' 58" N.; required her longitude and latitude?

 $D = 2^{\circ} 51' 58'' \text{ N. tan. } 8.699533$

RA=10h 30m 31' sine 9.536560 tan. 9.563908

8° 16′ 50″ N. tan. 9.162973 sec. 0.004551 23 27 40 S.

15 10 50 S. 9.984575 tan. 9.433497 cos.

Lon. 160 20 17 9.553034 sine 9.526946 tan.

Lat. 12 59 tan. 8.960443

Problem III.

Given the longitude and latitude of a celestial object, and the obliquity of the ecliptic; to find the right ascension and declination.

Tan. Lat.—sine Lon. =tan. A, North or South as the latitude is. Call O North in the six first signs, and South in the six last signs. A+O=B, as before.

A being less than 45°, sec. $A + \cos B + \tan \log C = \tan RA$ of the same kind as the longitude, unless B be more than 90°, when the quantity found of the same kind as the longitude must be subtracted from twelve signs.

A being more than 45°, tan. A + cosecant A + cos. B + tan. lon. tan. RA of the same kind as the longitude, unless B be more than 90°, when the quantity found of the same kind as the longitude must be subtracted from twelve signs.

If RA be nearer III. signs and IX. signs, than O and VI. signs,

sine RA + tan. B = tan. Dec. of the same name as B.

And RA being nearer O and VI. signs, than III. and IX. signs, tan. RA+cos. RA+tan. B = tan. Dec. of the same name as B.*

[•] These rules may, in general, be depended upon, except in peculiar circumstances, which a consideration of the figure will enable the computer to correct, as when the longitude, or RA, fall upon FP, or py, &c.

See Dr Abram Robertsen's paper in the Phil. Trans. for 1816, page 1884 which want of room cannot be given here.

EXAMPLE.

On the 1st of January, 1820, the mean longitude of the Star Fo-malhaut was 11° 1° 19′ 34″, the mean latitude 21° 6′ 45″ S.; required the right ascension and declination, the obliquity of the ecliptic being 23° 27′ 46″?

Lat. 21° 6' 45" S. tan. 9.586721

Lon. 331 19 34 sine 9.681082 tan. 9.737901

A= 38 49 26 S. tan. 9.905639 sec. 0.108420 O= 23 27 46 S.

B= 62 17 12 S. cosine . . 9.667498 tan. 10.279585

RA=341 55 14 tangent . . 9.513819 sine 9.491831

Dec. 30 34 21 S. . . . tan. 9.771416

Examples for Exercise.

1. The mean longitude of & Arietis, on the 1st January, 1820, was 1° 5° 8′ 48″, and mean latitude 9° 57′ 34″ N. when the obliquity of the ecliptic was 23° 27′ 46″; what was the right ascension and declination?

Ans.-R. A. 1h 57m 3'; Dec. 22° 36' 24" N.

2. Required the right ascension and declination of Pollux, when the longitude was 3° 20° 43′ 58″, the latitude 6° 40′ 17″ N. the obliquity of the ecliptic being 23° 27′ 46″?

Ans.—R. A. 7h 34m 17.5'; declination 28° 27' 8" N.

3. The mean longitude of Spica Virginis is 6' 21° 19' 50", latitude 2° 2' 24" S. and the obliquity of the ecliptic 23° 27' 46"; required the right ascension and declination?

Ans.—R. A. 13h 15m 43.5s; declination 10° 13' 4" S.

4. The mean right ascension of & Aquilæ is 19h 42m, and declination 8° 24' 4" N. the obliquity of the ecliptic being 23° 27' 46"; required the longitude and latitude?

Ans.—Longitude 9º 29º 14' 14', Latitude 29° 18' 36" N.

5. Required the longitude and latitude of a Pegasi, of which the right ascension is 22^h 55^m 48^s, declination 14° 14′ 21″, the obliquity of the ecliptic being 23° 27′ 46″?

Ans.-Longitude 11' 20° 58' 47", Latitude 19° 24' 36" N.

PROBLEM IV.

Given the latitude of the place, and the sun's declination, to find

his altitude and azimuth at 6 o'clock.

1. At Edinburgh, in latitude 55° 57' 20" N. on the 21st of June, 1826, the sun's declination was 23° 27' 36" N.; required his altitude and azimuth at 6 o'clock in the morning or evening, his declination being supposed to remain the same.

Construction .- Describe the primitive HPON on the plane of the

meridian. Let HO represent the horizon, ZN the prime vertical at right angles to the former. Make OP, from a scale of chords equal to the latitude of the place, North in the present instance; draw PP', the six o'clock hour circle in this case, and at right angles to it draw the equator EQ; describe the small circle nm at the distance of 23° 27' 36" from the equator, representing the parallel of declination, and it will cut the six

E C F C O

o'clock hour circle PP' in F, the sun's place at the given time.

Through Z, F, and N, describe the azimuth circle ZFN cutting the horizon in D, then FD is the altitude, FZ the zenith distance, and the angle FZP, or its measure, the arc DO, is the azimuth; consequently, the things given and required fall in either of the triangles FZP, or FDA, which are supplemental to each other. For, since OP is the latitude, PZ is the colatitude, AF is the declination; consequently, FP is the polar distance, DF being the altitude, FZ must be the zenith distance.

Calculation.—In the right-angled spherical triangle FPZ, rightangled at P, FP and PZ are given, to find the angle FZP and FZ; or in the triangle ADF, right-angled at D, there are given the angle FAD, equal to the latitude of the place, and AF, the sun's declination, to find DF, the altitude, and the side AD the azimuth.

By the rule of the circular parts FP, PZ, and PZF, are all connected, therefore PZ is the middle part, and PZF and PF are the

adjacent parts, where							
$R \times \text{sine } ZP = t$	m. F	F×	COS.	PZF	, or		
$R \times \cos$. lat. = co	os de	c. X	COS.	azimi	uth,	therefore	
\cos azimuth $=\frac{c}{c}$	cos. l	ec.	= cos	. lat.	× taı	a. dec.	
To log. cos. lat.	55°	57'	20′′				9.748061
To log. cos. lat. Add log. tan. dec.	23	27	36	•	•	•	9.637472
Sum = log. cos. az Again, to find FZ the	. 76	20	38 tudo	tha		a things	9.385533
$R \times \cos FZ = \cos ZP$	ue c	. Tri	uue, D	nine	Patition	e uungs	being given,
To log. sine lat.	55°	57'	20"				9.918347
Add log. sine dec.	23	27	36	•	•	•	9.600002
Sum = log. sine alt	. 19	15	40			•	9.518349

PROBLEM V.

Given the latitude of the place, and the sun's declination, to find the altitude and hour when the sun is due East or West.

Example.

At Edinburgh, on the 21st June, 1826, what was the sun's altitude and hour when due East or West, the declination being 23° 27' 36" N.

In the last figure, let ZAN meet the parallel nm in K, and suppose a circle to be drawn through the points PKP, forming the triangle ZKP, right-angled at Z, then ZK is the coaltitude, and ZPK the hour from noon; hence

R × cos. PK = cos. ZP × cos. ZK, or
cos. ZK =
$$\frac{\cos. PK}{\cos. ZP}$$
 = cos. PK × sec. PO, or
sine alt. = sine dec. × sec. lat.
Dec. 23° 27′ 36″ sine 9.600002
Lat. 55 57 20 sec. 0.081653

Alt. 28 42 55 sine 9.681655 $R \times \cos ZPK = \tan ZP \times \cos PK$, or $\cos T = \cos \cdot \text{lat.} \times \tan \cdot \text{dec.}$

Dec. 23 27 36 tan. 9.637472

Time 4º 51° 48° cos. 9.467186

From noon, that is, at 7° 8° 12° A. M., and 4° 51° 48° P. M.

This problem is of considerable utility to the navigator and practical astronomer, for the purpose of determining time accurately when an altitude instrument is used. As the change of altitude, on which the accuracy of the determination of the time depends, is quickest when the object is on the prime vertical, the most proper time for observing an altitude for that purpose is, therefore, when the object is due East or West, as any small error in the observation has then the least possible effect on the time. Other errors are also in this case in a great degree avoided, or at least considerably lessened, particularly that arising from any small error in the estimated latitude at the time of observation. To facilitate its application, tables, corresponding to the latitude and declination (which must be of the same name with the latitude), have been given in books on Nautical Astronomy, such as those of Mendoza Rios, Mackay, and Lax. When the latitude and declination are of different names, the altitude must be as near the horizon as is consistent with accuracy, so far as depends upon the uncertainty of the horizontal refraction. Altitudes under 5° should not be used when great accuracy is required.

PROBLEM VI.

Given the latitude of the place and the sun's declination, required his amplitude and ascensional difference.*

At Edinburgh, on the 21st of June, 1826, from the data given, on

what point, and at what time, did the sun rise and set?

In the triangle ABC, in the last figure, there are given the angle BAC, equal to the colatitude, and BC the sun's declination; to find AC and AB.

 $R \times \text{sine } BC = \text{sine } AC \times \text{sine } BAC$, or $\frac{\text{sine } BC}{\text{sine } BAC} = \text{sine } BC \times \text{cosec. } BAC$. BC, or dec. 23° 27′ 36″ N. sine 9.600002

Latitude, 55 57 20 sec. 10.251939

AC, 45 19 33 sine 9.851941
CO, 44 40 27, in which case AC is the amplitude reckoned from the East or West, to the North and South, according to the name of the declination, and CO is that reckoned from the meridian, or from the North or South, according to the name of the declination.

Again, in the same triangle AB is the ascensional difference, and $R \times \sin AB = \cot BAC \times \tan BC$, or sine $AB = \tan \tan A$. lat. $\times \tan A$.

Lat. 55° 57' 20" tangent, . 10.170286 Dec. 23 27 36 tangent, . 9.637472

A. D. 2^h 39^m 52^s sine . 9.807758

8 39 52 = time of setting.
3 20 8 = time of rising, the latitude and de-

By the ascensional difference is meant the time before or after 6 o'clock the sun rises or sets. By this problem, therefore, the lengths of the day and night are determined the variation of the mariner's compass.

clination being of the same name, or if instead of sine we read cosine, then we would get the time of rising if the latitude and declination are of the same name, and the time of setting if of different names. This, however, is only the approximate time, as no allowance is made for the effects of a change of declination, the horizontal refraction and parallax in the case of the sun and planets. For these see Mackay on the longitude, or they may be found by the following rule. First, let the approximate time be found. To this time let the declination of the object be reduced. With it find the ascensional difference as formerly. Now, find the sum and difference of the natural cosine of the reduced declination and natural ral sine of the latitude, which may be carried to four places of figures only, these being sufficiently accurate for this purpose, and take half the sum of the logarithms of these quantities, to which add the constant logarithm 7.1761, and the proportional logarithm of the difference between the horizontal parallax and the sum of the horizontal refraction and dip of the horizon, the sum, rejecting 10 in the index, will be the proportional logarithm of the correction which is to be subtracted from the time of rising, or added to the time of setting, if the horizontal parallax is less than the sum of horizontal refraction and dip, otherwise the correction must be added in the first case, and subtracted in the second.

EXAMPLE.

Required the time of rising and setting of the sun on the 1st of April, 1826, in latitude 33° 42′ N., and longitude 16° 20′ W. the height of the eye, above the sea, being 28 feet.

Dec. 4° 28' N. cos. 9960

Sum 15517 log. 4.1908

(K)

Let. 33 42 N. sine 5548

Diff. 4421 log. 3.6455 Dip to 28 feet - 5' 16" 7.8363 -34 17 Hor. refrac. Parallax 3.0181 const. log. 7.1761 - 39 24 P.L. 0.6508- 3" 10 P.L. 1.7540

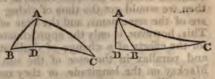
The correction to be subtracted from the time of rising, or added to the time of setting. As the moon's horizontal parallax is in general greater than the effects of dip and refraction, the correction thus obtained would have been applied with a contrary sign. This method of determining time may sometimes be of use when a better cannot be obtained, and in the case of the sun or moon, a mean of the times of appearance of the upper and lower limb may be taken.*

Solution of Oblique-Angled Spherical Triangles. The different cases of oblique-angled spherical triangles may be solved by the fellowing theorems:-

[•] To find the rising and setting of a star or planet, the transit over the meridian must be first computed as follows:—From R. A. of the star subtract that of the sun for noon the remainder is the approximate time of transit. Reduce the R. A. of both to this time and the given longitude, and subtract as before, and the remainder will be the true time of transit, which, properly applied to the semidiarnal arc, will give, when corrected for dip, &c., the true time of rising or setting.

soling hors we take to I am THEOREM I. was all to prind onitantia

In every spherical triangle the sines of the sides are proportional to the sines of the angles opposite to them,* Or, sin. AB: sin. AC::sin. C: sin. B.



Pires der alle supposess THEOREM II.

In oblique-angled spherical triangles a perpendicular arc being drawn from any of the angles upon the opposite side, the cosines of the angles at the base are proportional to the sines of the segments of the vertical angle, or cos. B: cos. C:: sin. BAD: sin. CAD.

THEOREM III.

The same things remaining, the cosines of the sides are proportional to the cosines of the segments of the base, or cos. AB: cos. AC:: cos. BD: cos. CD. THEOREM IV:

The same construction remaining, the sines of the segments of the base are reciprocally proportional to the tangents of the angles at the base, or sin. BD: sin. CD:: tan. C: tan. B.

THEOREM V. It legislated by THEOREM V. It should be DORL Single. The same construction remaining, the cosines of the segments of the vertical angles are reciprocally proportional to the tangents of the sides, or cos. BAD: cos. CAD::tan. AC:tan. AB.

THEOREM VI.

If, from an angle of a spherical triangle, there be drawn a perpendicular to the opposite side or base, the tangent of half the sum of the segments of the base is to the tangent of half the sum of the two sides of the triangle, as the tangent of half the difference of those sides to the tangent of half the difference of the segments of the base, or tan. \(\frac{1}{3}\) (BD+CD): tan. \(\frac{1}{3}\) (AB+BC):: tan. \(\frac{1}{3}\) (AB \(\sigma\) AC): tan. \(\frac{1}{3}\) (BD or CD).

When the three sides or the three angles are not the given parts of the triangle, to have sufficient data for the solution of the problem, the perpendicular must be so drawn, that two of the given things in the oblique-angled triangle may be known in one of the resulting right-angled triangles. of the street but he was been also

THEOREM VII. main maintaneously to their

If a perpendicular be drawn from an angle of a spherical triangle, to the opposite side or base, the sine of the sum of the angles at the base is to the sine of their difference, as the tangent of half the base is to the tangent of half the difference of its segments: And the sine of the sum of the two sides is to the sine of their difference, as the cotangent of half the angle contained by the sides is to the tangent

^{*} See Playfair's Geometry, article Spherical Trigonometry, Prop. XXIV., or Legendre's Geometry, article LXXVI., and the following in order.

of half the difference of the angles which the same sides make with the perpendicular, or sin. (B + C): sin. $(B \omega C)$: tan. $\frac{1}{2}BC$: tan. $\frac{1}{4}BC$: tan. $\frac{1}{$ (BAD & CAD).

THEOREM VIII.

The sine of half the sum of any two angles of a spherical triangle, is to the sine of half their difference, as the tangent of half the side adjacent to these angles, is to the tangent of half the difference of the sides opposite to them. And the cosine of half the sum of the same angles, is to the cosine of half their difference, as the tangent of half the side adjacent to them, is to the tangent of half the sum of the sides opposite, or $\sin \frac{1}{2} (A + B) : \sin \frac{1}{2} (A \cap B) : : \tan \frac{1}{2} AB : \tan \frac{1}{2} (BC \cap AC)$. And $\cos \frac{1}{2} (A + B) : \cos \frac{1}{2} (A \cap B) : : \tan \frac{1}{2} AB : \tan \frac{1}{2} (BC \cap AC)$.

Corollary.—The sine of half the sum of any two sides of a spherical triangle, is to the sine of half their difference, as the cotangent of half the angle contained between them, is to the tangent of half the difference of the angles opposite to them: And the cosine of half the sum of these sides is to the cosine of half their difference, as the cotangent of half the angle contained between them, is to the tangent of half the sum of the angles opposite to them, \dagger or sin. $\frac{1}{2}$ (AB ω BC):: cot. $\frac{1}{2}$ A: tan. $\frac{1}{2}$ (B ω C) cos. $\frac{1}{2}$ (AB ω BC): cot. $\frac{1}{2}$ A: tan. $\frac{1}{2}$ (B ω C) cos. $\frac{1}{2}$

THEOREM IX.

It will be sometimes more easy in practice to compute an angle from the three given sides by the following formulæ and rules, than by any of those already given: thus, suppose A, B, C, are the angles as before, and a, b, c, the sides opposite; then

Sin.
$$\frac{1}{2} A = \sqrt{\frac{\sin \left\{ \frac{1}{2} (a+b+c)-c \right\} \cdot \sin \left\{ \frac{1}{2} (a+b+c)-b \right\}}{\sin b \sin c}}$$
 (1)

Cos.
$$\frac{1}{4}$$
 A = $\sqrt{\frac{\sin \frac{1}{4}(a+b+c)\sin \frac{1}{4}(a+b+c)-a}{\sin b \sin c}}$ (2)

Sin.
$$\frac{1}{2}A = \sqrt{\frac{\sin \left\{\frac{1}{2}(a+b+c)-c\right\} \cdot \sin \left\{\frac{1}{2}(a+b+c)-b\right\}}{\sin b \sin c}}$$
 (1)
Cos. $\frac{1}{2}A = \sqrt{\frac{\sin \left(\frac{1}{2}(a+b+c)\sin \left(\frac{1}{2}(a+b+c)-a\right)\right\}}{\sin b \sin c}}$ (2)
Tan. $\frac{1}{2}A = \sqrt{\frac{\sin \left(\frac{1}{2}(a+b+c)-b\right) \cdot \sin \left(\frac{1}{2}(a+b+c)-c\right)}{\sin \left(\frac{1}{2}(a+b+c)-c\right)}}$ (3)

Rules in Words.

I. From half the sum of the three sides subtract each of the two sides which contain the required angle. Then to the cosecants of the sides which contain the required angle add the sines of the two remainders; half the sum of these foregoing logarithms will be the sine of half the required angle.

II. Find the difference between half the sum of the three sides, and the side opposite the required angle. Then to the cosecants of the two containing sides add the sines of the half sum and difference; half the sum of these four logarithms will be the cosine of half the required angle.

III. To the cosecant of half the sum of the three sides add the

This theorem forms Proposition XXX. in Playfair's Spherical Trigonometry, where it is partly erroneous. It is also given in Mr J. Wallace's edition of Brown's Logarithmic Tables. Erroneous rules and impossible triangles should always, if possible, be avoided.—See the French Edition of Cagnoli's Trigonometry, § 1063, 1108 and 1160. + Legendre, § LXXXIII.

cosecant of half that sum diminished by the side opposite the required angle, and the sines of the same half sum diminished by each of the sides containing the required angle; half the sum of these four logarithms will be the tangent of half the required angle. See remarks annexed to Case III., Plane Trigonometry.

THEOREM X.

Given two sides and the contained angle, to find the side opposite

that angle.

To twice the sine of half the contained angle, add the sines of the two containing sides, and from half the sum of these three logarithms subtract the sine of half the difference of the sides; the remainder will be the tangent of an arc, the sine of which being subtracted from the half sum of the three logarithms already found, leaves the sine of half the required side.

THEOREM XI.

The two sides and contained angle being given, the third side may

be found in the following manner.

To twice the sine of half the contained angle add the sines of the two containing sides; half the sum of these three logarithms, after rejecting 20 in the index, will be the cosine of an arc. Also find half the difference of the two containing sides.

To the sine of the sum of these two last arcs add the sine of their difference; half the sum of these two logarithms will be the cosine of

half the required side.

It may be remarked, that when the side is not greater than 90°, theorem X. may be used; when it is greater than 90°, theorem XI. may be employed when great accuracy is required.

THEOREM XII.

The three angles of a spherical triangle being given, to find the sides.

From half the sum of the three angles subtract each of the angles next the required side, then to the cosecants of the adjacent angles add the cosines of the two remainders; half the sum of these four logarithms will be the cosine of half the required side.

THEOREM XIII.

The same things being given; from half the sum of the three angles subtract the angle opposite the required side, then to the cosecants of the adjacent angles add the cosine of half the sum and the cosine of the difference; half the sum of these four logarithms will be the cosine of half the required side.

Either of these theorems may be employed, which will give the

more accurate result.

Having stated the theorems on which the solutions in oblique-angled spherical triangles depend, it is necessary to illustrate them by examples which will chiefly consist of those applicable to the usual cases that occur in practical astronomy and navigation.

PROBLEM I.

Given the latitude of the place, the sun's altitude and declination, to find the time and the azimuth.

At the observatory of Edinburgh, on the Calton-hill, in latitude 55° 57' 21" N., on the third of June, 1826, the following observa-

tions of the sun's lower limb were taken in the morning; required the time and azimuth, the barometer being at 29.56 in., and the thermometer at 64° F.?

CHEMINISTER STOR L'.	
Times by Watch.	Allitudes.
7º 1º 20°	26° 51′ 20′′
2 18	26 59 30
3 25	27 7 15
4 30	27 15 40
5 27	27 23 45
7 7 7	07 07 00
5 17 0	35 37 30
l ance	***************************************
Means. 7 3 24	27 7 30 Lower limb.
Or observed Z.D.	62 52 30
Z. D. 62° 52′.5 log. 3 4	2.03692
Thermometer 64° F. log	. 9.98751
Barometer 29.56	. 9.99358
Thermometer 64.0 F.	. 9.99940
1 met mometer Oz.O 1.	. 0.00010
$r = 106''.5 = 1'.46''.5 \log$. Z. dist. = 62° 52′ 30″ Refraction + 1 46 .5	2.01741
True Z. D. 62 54 16 .5 of the lower Semidiameter — 15 47 .5	limb.
True Z. D. 62 38 29 of the centre. Approximate time, June 2d, 19 ^h 4 ⁿ Longitude in time add + 12	
Estimated Greenwich time Daily variation of dec. 19 16 7' 42"	D. L. 0.09503 P. L. 1.36878
Prop. part. to 17 ^h 18 ^m + 6 11 Dec., June 2d, 22° 9 38 N.	P. L. 1.46381
Reduced declination 22 15 49 N. Polar distance 67 44 11	

Polar distance
1. Now in the figure, (page 70), there are given OP the latitude, and consequently ZP the colatitude, PK the polar distance, and ZK the zenith distance, the place of the sun being K near the prime vertical, as being most advantageous to determine the time with accuracy, or the three sides of the triangle KPL; to find the angle ZPK the time, and the angle PZK the azimuth from the southern meridian PEP. This, therefore, is solved by means of theorem IX.

Now the latitude being	55° 8	7' 9	h".	the colatitude is 34° 2° 38"
Z. D.	164	38	29	
Colatitude	34	2	39	cosec 0.251942
Polar dist.	67	44	11	cosec 0.033647
Sum	164	35	19	
Half .	82	12	39	
First rem.	48	10	0	sine . 9.872208
Second rem	14	2 8	2 8	sine . 9.397850
				19.555647
	3	2° 2	7" 2 2	.sine . 9.777824
Time from noon 3d	4	54	42	·
App. time, A. M.	7	5	18	·
Time by watch	7 7	3	24	
Watch slow		1	54	for apparent time
Again app. time	7	5	18	
Equation of time	_	2		
Mean time	7	2	55	
Time by watch	7	3		
Watch fast	 th an	the		for mean time.

2. To find the azimuth or the angle KZP, the point K being that in which the circles n m and ZIN cut each other, there are given the three sides of the triangle KPZ.

KP, or polar dist. PZ, or colatitude ZK, or Z. dist.	67° 44′ 11″ 34 2 39 62 38 29	cosec.	0.251942 0.051515
Sum	164 25 19		
Half Difference	82 12 39 14 28 28	sine sine	9.995974 9.39 7 850
•		• • •	19.697281
	45 7 41	cos	9.848640
	N. 90 15 22 44 52 19 2	E sin. or	

S. 89 44 38 E. or reckoned from the

South in north latitude, or from the North in south latitude.

This problem is very useful in navigation, for the purpose of finding the variation of the compass, which is the difference between the true and observed amplitude or azimuth.

To determine this, let the observer be supposed to look directly from the centre of the card towards the point representing the true azimuth; then if the observed azimuth is to the *left* of the true azimuth, the variation is easterly, but if to the right it is westerly to the amount of the difference between them.

Thus let the true azimuth be 8. 89° 44′ 38″ E. 65 24 38

Variation . . . 24 20 0 West.

Or about 21 points westerly.

These results for time and variation have been deduced strictly from the solution of the spherical triangle formed by the data, but they may be found more readily by rules derived from it, as may be seen in various books on navigation and nautical astronomy.

When tables which have proportional parts annexed to them are used, the following method may be advantageously employed

for determining the time.

Rule.—When the latitude of the place and the declination are of the same name, let their difference, but, if of contrary names, let their sum, be taken. Under this difference or sum place the senith distance, and let the half sum and half difference of these be taken; then add together the secant of the latitude, the secant of the declination, the sine of the half sum, and the sine of the half difference; half the sum of these four logarithms will be the sine of half the hour angle or time from noon, from which the apparent and mean time may be obtained as formerly.

	•		65
Latitude Declination	55° 57′ 21″ N. secant 22 15 49 N. secant		0.251877 0.033605
Difference	33 41 32		42
Zenith dist.			1
Sum Difference	96 20 1 half 48° 10′ 04″ 28 56 57 half 14 28 284	sine sine	9.872208 9.397821 233
			19.555652
	2 ^h 27 ^m 20 ⁺ 1 .05 P. P.	sine	9.777826 681
	2 27 21 .05		45 43
	4 54 42 .10 24		
	10 F 1F 00 TO 34		

June 2d, 19 5 17.90 P. M.,

In the above computation the several proportional parts are set down and summed all together, which renders the operation somewhat more easy when our tables are employed.

Several variations may be made on the six things here proposed, that may serve as a useful exercise, which, by a reference to the theorems and rules already given, will be easily performed.

PROBLEM II.

Given the latitude of the place and the sun's declination; to find the time when twilight begins and ends.

At what time will twilight begin and end at London, in latitude 51° 32′ N., on the second of May, 1827, the sun's declination being 15° 14′ N.?

In figure, (page 70), suppose a parallel n m to the equator EQ to be drawn at the distance of 15° 14′ above it, while another parallel to the horizon HO is drawn at the distance of 18° below it, these two would cut one another somewhere between c and m in S, forming the triangle ZPS, in which ZP, PS, and ZS, are given to find the angle ZPS, the angle between the meridian PEP and another meridian passing through the sun at the time he is 18° degrees below the horizon, his situation when twilight begins and ends.

Z s or zenith distance P s or polar distance PZ or colatitude	74 46 38 28	cosecant	0.015534 0.206168
Sum	221 14	her shelt digestron	con be token.
Half Difference .	110 37 2 37	sine sine	9.971256 3.659475
he the sing of hell the	Hairly and	The four mon, in	18.852433
T98020	4h 58m 6s 2	cosine	9.426216 443
Time from noon of Or at	56 12 in 2 4 48 in	n the evening n the morning.	227

PROBLEM III.

Given the right ascensions and declinations, or the longitudes and latitudes of two celestial objects; to find their angular distance.

In this problem there are given two sides and the contained angle to find its opposite side. The contained angle is the difference between their right ascensions or longitudes, and the containing sides are the complements of the declinations or latitudes. If the sun be one of the objects, as his latitude is very small, he may be supposed to be always in the ecliptic; then the triangle so formed will be right angled if the longitudes and latitudes are used, and the computation becomes more simple. By means of this problem the lunar distances in the nautical almanac are computed.

On the 1st of June, 1828, required the distance between the moon and a Pegasi, at noon, on the meridian of Greenwich, the moon's right ascension being 295° 23′ 46″, and declination 16° 11′ 45″ S., the star's right ascension being 22° 56^m 13°85, or 344° 3′ 28″, and north polar distance 75° 43′ 2″, or declination 14° 16′ 58″ N.

344° 3′ 20″—295° 23′ 46″ = 48° 39′ 42″ the angle at the pole. Instead, however, of following the operation derived from the spherical triangle, a more simple practical rule may be derived from it according to theorem IX.

To twice the sine of half the contained angle add the cosines of the moon and star's declinations, and take half the sum of these three logarithms. From this half sum subtract the sine of half the sum of the declinations if they are of contrary names, or that of half their difference if of the same name, the remainder will be the tangent of an arc, the sine of which being subtracted from half the sum of the three logarithms already found will give the sine of half the required distance.

Diff. of R. A.	48° 39′ 42″	,	
Half	24 19 51	sine × 2=19.220804	
Moon's declination Star's declination	16 11 45 14 16 58	S. cos. 9.989418 N. cos. 9.98364	
		39.198581	
Sum	30 28 43	19.5 0 9291 (a	١
Half .	15 14 211		,
Arc	56 31 18	tan. 10.179574	
Same arc		sine 9.921215 (6	·)
Half distance .	28 27 29 2	sine 9.678076 (a	—b)
True distance	56 54 58	. :	•

Examples for Exercise.

1. Required the distance between the moon and sun on July 2d, 1838, at noon on the meridian of Greenwich, the longitude of the sun being 3 10° 28′ 44′, the longitude of the moon 11° 17° 59′ 39′, and latitude 2° 51′ 40′′ N.?

Ans.-112° 27' 19" east of her.

2. Required the distance between the moon and sum on the 20th January, 1828, at noon, the sun's longitude being 9° 29° 29° 39°, that of the moon 11° 17° 54′ 42″, and latitude 3° 24′ 28″?

3. Required the distance between the moon and a Aquilar, at noon on the 10th of May, 1828, the right ascension of the moon being 6° 58′ 43″, the declination 4° 44′ 48″ N., the right ascension of a Aquilar in time, being 19° 42° 25°.62, and north polar distance 81° 34′ 41″?

Ans.=70° 54' fil" west of her.

4. Required the distance between the moon and Aldebaran, at madnight on the 16th of December, the moon's R. A., being 39° 31′ 30″, the declination 11° 18′ 11″ N., the R. A. of Aldebaran being 4, 26° 8.67, and N. P. D. 73° 50′ 37″.4?

Ans.—33° 21′ 10″.

PROBLEM IV.

On finding the latitude by observation.

The most simple practical method of sinding the latitude, is from the meridian altitude of a celestial body whose declination is known.

Should the object be the sun, moon, or some of the planets, the altitude or senith distance of the lower or upper limb, or both, are

observed, and by the application of several corrections that of the centre is obtained a bijent of diadigards

When reflecting instruments, such as the sextant, repeating circle, &c. with an artificial horizon, are employed, the arc read off must, from the principles of optics, be halved before the other corrections are applied.*

A meridian altitude of the sun, moon, or a planet taken at land, must be corrected for refraction, parallax, and semidiameter, and at

sea for the dip of the horizon.+

Observed altitude

Index error

Having found the true altitude, take its complement to 90°, which gives the zenith distance, denominated north or south, according as the observer is north or south of the object.

Now, if the zenith distance and declination are of the same name. their sum is the latitude; if of contrary names, their difference is the

latitude of the same name with the greater.

Ex. 1.—Edinburgh Observatory, March 28th, 1825, with an artificial horizon and one of Troughton's best sextants, the vernier of which showed 10", Captain Pringle Stokes, R. N. found the meridian altitude of the sun's lower limb to be 73° 32' 15", the index error being +2' 26", the barometer standing at 29.66 inches, and Fahrenheit's thermometer 56°; what was the latitude, employing the refractions in the table in the nautical almanac? 73° 32′ 15″

+ 2 26

a face west 23 36.3 N	73	34	41	
Halfold	36	47	20	
Refraction to 29.66 and 56° F. Parallax Semidiameter	1	16	8	
P 23 Md. the longitude of the moon 11 17 50 30.	37	Ser.	933	
The same of particular and particula	HEAL.	-	-	
Zenith distance Declination	52 2	57 59	43	NN
Latitude	55	57	28	3
Ex. 2.—To determine from the observations of Cap R. N., taken June 4th and 6th, 1822, the latitude of	San	Blas	th	ni
by estimation being about 21° 32½ N., and longitude 7° 1° in time.	- 57	8 7	ALTE	7
To compute the sun's declination, June 4th, Longitude in time 7 ^h 1 ^m D. L.	1829	0.53	408	
Prop. part to 7 ^h 1 ^m 2' 1".6 P. L.	100			00
	Drue.	176.5	1 -10	
Correct prop. part 2 4 .0 Declination at noon G. 22° 24 41 .0	diin	ess a	do	
Sun's true dec. 22 26 45 .0 N.	HAR.			-
See explanation of Table XXV.	THE OWNER.	MINERAL	Mar.	

[†] Tables XIII. and XIV. have been computed, expressly for this purpose at sca, combining the whole in one.

	. 1° 10′ log. •	0.0755
THEE OF TAIL		
Bar. 29.75 Ther. 86°	• •	9.9963 9. 99 84
r 1".1 Parallax 0".2 (table 16	er er er fyr mei er	0.0388
Fa	ice of the circle west	*
Readings $\left\{ egin{array}{ll} ext{lst Vernier} \ ext{2d} \end{array} ight.$		88° 56′ 0′′ 50 10
Obs. merid. alt. sun's l	!. !	88 50 5
Sun's semidiameter		+ 15 47.9
Refraction Parallax		+ 0.2
True alt. sun's centre		89 6 51 5 con.
entert in the second	,	
Zenith dist. Declination		0 54 8.7 B. 22 26 56.6 N.
Latitude with face wes	.+	21 32 36.3 N.
•		ret
	sun's declination, June	
Longitude in time	7 ^h 1 ^m D. L. 6 9" P. L.	. 0.5 3408 . 1.46649
Prop. part to 7 ^h 1 ^m , Eq. to sec. diff.—24" and	1′ 48″ P. L d 7° + 2. 5	2.00048
Correct man ment	+ 1 50.5	per en la
	+ 1 50.5	
	22 38 10.0	19 3 84 3
Dec. at noon G.		no esta e la esta esta
Dec. at noon G. True dec. at S. B.	22 40 0.5 N.	and A
True dec. at S. B. To compute the refract thermometer 85° Fab	22 40 0.5 N. ion, the barometer being, the meridian Z. D. be	g 29.8 inches, an
Dec. at noon G. True dec. at S. B. Pe compute the refract thermometer 85° Fab. Z/D7 (1987 at 12 28:5)	22 40 0.5 N. ion, the barometer bein , the meridian Z. D. beine de	g 29.8 inches, an
Dec. at noon G. Crue dec. at S. B. Fo compute the refract themsometer 85° Fab. Z/D/1 10 12 28 5 Ther. 85°	22 40 0.5 N. ion, the barometer bein , the meridian Z. D. be log. 1 0.1926 log. 9.9694	g 29.8 inches, an ing 1° 23'.5 nearly
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	True mer. Z. D. Declination	22	7 40	39.3 0.5	S. N.
1	Latitude, face east	21	32	21.2	N.
	Saface west	21	32	36.3	
	Mean latitude by sum	21	32	28.7	THE STATE OF

When the latitude is determined by an astronomical circle, an observation is not supposed to be complete, till the observer has reversed the circle, by this means combining two sets of observations, with the face or graduated limb of the instrument alternately, as in this example, towards the east and west.

San Blas, 20th May, 1822, the barometer being at 29.78 inches, Fahrenheit's thermometer 83°, the chronometer too fast for mean time 4^h 4^m 45°, Polaris on the meridian below the pole by chronometer at 1^h 8^m 41° and its true apparent N. P. D. 1° 38′ 28″.46.

d d	Face of instru- ment.	Chronometer.	Time from the Merid.	Reduction to Merid.	Obs. Z. D. and Alts.	Altitudes.
3	n bywo	1 6 5	2 36	13″.27	70 3 34.5	19 56 25.5
D D	or East	1 8 41	0 50	1 .36	3 34.0	56 26.0
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To compute the correction of altitude on account of the distance of the star from the meridian.

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Examples for Exercise.

4. Ch the 1st of September, 1824, in longitude 54° W., the meridisn altitude of the sun's lower limb was 79° 44' 15" S., the height of the eye being 24 feet; what was the latitude?

^{2.} On the 1st of January, 1826, the meridian altitude of the star Arctarus was 60° 41' S., the height of the eye being 24 feet; what was the latitude? Ans. 49° 29'.8.

^{3.} On the 14th September, 1827, in longitude 103° 18' E., let the meridian altitude of the moon's lower limb be 51° 4' N., and the height of the eye 20 feet; required the latitude?

4. On the 29th September, 1827, in longitude 20° 40' W., if the observed meridian altitude of the moon's upper limb be 83° 6' N., and the height of the eye 16 feet; required the latitude?

more described Ans. 1-21° 25'.7 S. beautiful anti- safaritan harrowing

As the meridian altitude may, by the interposition of clouds, or other causes, be lost at sea when a knowledge of the latitude is necessary for the safety of the ship, recourse must be had to other methods, particularly to that of H double altitudes, and the time between them, as being the most practicable.* This method requires solutions in three spherical triangles. In the triangle ZPS there are given



PS the sun's polar distance at the time of the first observation, PS' that at the second, and the angle S'PS measured by the the elapsed time; to find the side S'S and the angle PS'S.+ Again in the triangle ZS'S there are given the zenith distance ZS at the time of the first observation, ZS' that at the second, and the side S'S already found to determine the angle ZS'S. But PS'S being already computed, ZS'P may be obtained. Whence there are in the triangle ZS'P, the sides ZS', and PS', and the contained angle ZS'P; to find the side ZP the colatitude. This is the regular method by spherical trigonometry; but if the polar distance PS be supposed to remain the same, that at the middle time, between the observations, or, as Professor Lax seems to think preferable, the same as at the time of the greater altitude, and, by combining the solutions of the several triangles in one, the operation becomes more simple. In order to render this method still more easy to practical seamen, Douwes proposed an approximate method by introducing the latitude by account, which, when properly restricted according to the rules of Maskelyne or the tables of Lax, will generally give the desired result sufficiently correct for nautical purposes, and the computations may be very readily performed by the tables of Lynn.

When the common tables are used, Mr Ivory's solution is the best, particularly in the form that Mr Riddle has given it, which we shall

adopt here.

Find the sun's declination for the time of the greater altitude, and the true altitudes, reducing the less if necessary for the ship's run to what it would have been had it been taken at the same place with the greater. This is accomplished by observing the sun's bearing by compass, at the time of taking the less altitude, and, finding the angle contained between that and the ship's course by compass, corrected for leeway if she makes any, in the interval between the observations. With this angle as a course enter a traverse table, and the difference of latitude, answering to the distance run during the elapsed time, will be the reduction of altitude.

If the less altitude be observed in the forenoon, the reduction of altitude must be added to it, if the angle between the ship's course and the sun's bearing be less than eight points; but if that angle be greater than eight points, the reduction is to be subtracted from the less altitude. If the less altitude be observed in the afternoon, the orne wit no true sloy dear

On the authority of a very distinguished practical navigator, I am informed, that double altitudes are not of such importance as is generally supposed.

+ A circle is supposed to pass through PS' P' similar to PSP'.

reduction is to be subtracted from it, if the angle between the ship's course and the sun's bearing is less than eight points; but if greater, the reduction is to be added to the less altitude. With the corrected altitudes, the elapsed time, and the declination, the latitude at the time of the observation of the greatest altitude will be found, which may be reduced to noon by means of the dead reckoning.

1. Take half the interval between the observations, and call it

the half clapsed time.

2. To the sine of the half elapsed time add the sine of the sun's polar distance, the sum, rejecting always ten in the index, will be arc first.

3. To the secant of arc first add the cosine of the polar distance, the sum will be the cosine of arc second, which will be of the same

affection or character as the polar distance.

4. To the corecant of arc first, add the cosine of half the sum of the true altitudes, and the sine of half their difference, the sum will be the sine of arc third.

5. Add together the secont of arc first, the sine of half the sum of the true altitudes, the cosine of half their difference, and the secont

of arc third, the sum will be the cosine of arc fourth.

6. The difference of arc second and arc fourth is arc fifth, when the senith and the elevated pole are on the same side of the great circle, passing through the places of the sun at the times of observation, otherwise their sum is arc fifth.

7. To the cosine of arc third add the cosine of arc fifth, and the

sum will be the size of the latitude.

Ex. 1.—On the 6th of June, 1828, in latitude 58° N., and longitude 48° W., by account, at 10° 53° 20° A. M. per watch, the altitude of the sun's lower limb was 52° 20°, and at 1° 17° 8°, the altitude of the same limb was 52° 54′, and the bearing per compass S. W. by W. The ship's course during the elapsed time was S., the wind E.S.E., and hourly rate of sailing 8 knots, and the ship making 1½ pts of lee-way. Required the true latitude at the time of observation of the greatest altitude, the height of the eye being 16 feet?

Ship's apparent course S. or 0^{pts}
Lee-way 1½

Ship's true course S. by W. $\frac{1}{3}$ W. = $\frac{1}{3}$ pts S. W. Sun's bearing at 2d obs. S. W. by W. = 5 pts S. W.

Contained angle $\frac{3!}{1!}$ Interval between the observations $= 2^n \cdot 23^m \cdot 48^n = 2^n \cdot 4$ Distance run $= = 2^n \cdot 4 \times 8 = 19.2$ miles.

Now to course 31 points and distance 19.2, the difference of latitude is 14.84, and since the least altitude was observed in the afternoon, and the angle between the ship's course and sun's bearing is less than eight points, this reduction is subtractive.

[•] Should there be any doubt whether the zenith and elevated pole are on the same side of the great circle, passing through the places of the sun, the latitude may be computed on both suppositions, which, being compared with that by account, the true latitude will, in general, be readily discovered with little additional trouble, for it is only are fourth and its classes that will require alteration.

First observed alt. 53° 20′ Second observed alt. 51° 54′ Cor. table XIII. 30° + 11°.2
1. True alt. 53 31 2 m Reduction 1 and at 12 14 18
2. True alt
2. 52 50 4 Sum 106 21 6 half 53° 10′ 8 = 53° 10′ 48″
Difference . 0 40.8 half 0 20.4 = 0 20 24 Times 10 ^h 53 ^m 20 ^l Time . 10 ^h 53 ^m 20 ^l A. M.
Elapsedt. 2 23 48
and the state of the second state of the secon
Prop. part 0. 31 2.54350 Dec. at noon or 6th 22° 41′ 17″ N.
Reduced dec. 22 41 48 N. Polar dist. 67 18 12
9,489404 sin. 1 ^h 11 ^m 54 ^p H. E. T. 9.465055 sin. 67, 12 12 pol. dist. cos. 9.586422
9.454459 sin. 16 32 37 arc 1st sec. 0.018362 cosec. 0.545624 66 15 52 arc 2d cos. 9.604784
0 018362 sec. arc 1 9,903374 sin. 53° 10′ 48″ cos. 9.777646 9,999993 cos. 0 20 24 sin. 7.773187
0.000634 sec.3d 0 42 56 sin. 3.096467
33 22 8 arc 4. cos. 9.921763 3d cos. 9.99966 32 52 44 arc 5. cos. 9.924104 Latitude 57 5 51 N. arc 6. sine 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
In this example the computation is carried to seconds, but such a degree of accuracy is unnecessary at sea.
2. On the 6th of March, 1827, in latitude 60° N. by account, and

2. On the 6th of March, 1827, in latitude 60° N. by account, and longitude 105° E., the altitude of the sm's lower limb was observed to be 19° 42′ at 40^h 4^m 20′ in the forenoon, his centre bearing S. S. E. by compass, and at 1^h 32^m 36° afternoon it was 21° 8′. The ship's course during the elapsed time was N. W. by N., sailing at the rate of 9 knots per hour, and the height of the eye 16 feet. Required the ship's latitude at the time of taking the greater altitude?

 ing at the same time N. W. & W. During the elapsed time the ship was sailing S. W. by W. at the rate of 4 knots per hour, and the height of the observer's eye was 28 feet. Required the latitude at the time of taking the first altitude?

474 11° 37' 8.

PROBLEM VI.

On finding the Longitude.

I. BY LUNARS.

Since the rotation of the earth about its axis is performed in a day, the sun appears to pass over 360° in 24 hours, and, consequently, over 15° in one hour; therefore, it is obvious, that the difference of time between any two places will give the difference of longitude between those places.

A variety of methods have been proposed for determining the longitude of a place, but almost all of them depend upon one general principle, the comparison of the relative times under two different meridians; so that, if the time on two different meridians be known, the difference of these times turned into degrees, at the rate of 15° to an hour, will give the difference of longitude between these

meridians.

As the sun apparently moves from the east towards the west, it is evident, that all places lying to the eastward of any meridian will have noon, or any other hour, sooner, or if westward, later, by the precise time the sun takes to pass from the meridian of the one place to that of the other. Hence, if the time on the meridian of Greenwich, the place from which our longitude is reckoned, and that of any other place at the same instant be known, the longitude of the latter place from Greenwich is also known, by turning the difference of time into degrees, at the rate of 15° to an hour.

Among the heavenly bodies which frequently present themselves for observation, there is none whose apparent velocity is so rapid with regard to the sun, planets, and fixed stars near the ecliptic, as that of the moon; the diurnal motion of that object being at a mean rate about 13° 11'. Hence, her distance from these bodies is continually changing in proportion to the time, and an error of 2" in the distance between the moon and any of these bodies will produce an error of about 1' only of longitude. Of all the various modes, then, which have been proposed to determine the longitude at sea, it is probable the method by lunar observations will continue to be the most practicable. It appears also from the numerous observations lately made by several of our most distinguished navigators, that a series of lunars taken at land with good instruments, will, when great nicety in the requisite observations and calculations is attended to, give the longitude with singular accuracy.

The instruments generally employed are a good chronometer for connecting observations taken at different times with one another, two good quadrants for obtaining the altitudes, and a sextant or reflecting circle for taking the distance. These instruments are all described in our usual treatises on navigation and nautical astro-

nomv.

If the sun or star he at a sufficient distance from the merklism at the sine of taking the distance, the true altitude of either of these chiects will serve to compute the apparent time at the ship, and this compared with the Greenwich time, derived from the lunar distance,

will give the longitude. The same thing may be obtained from the moon's altitude, but less readily, as her right ascension and declination must be very accurately computed by applying the equation of second difference.

This method will be rendered familiar by the following examples.* Ex. 1.—September 24, 1827, in latitude 48° 50′ south, and longitude by account 120° west, at 8^h 18^m 30° A. M., the following observations were made to obtain the true longitude; the height of the eyes of the observers being 30 feet above the surface of the sea, the angular instruments being perfectly adjusted when the English ba-

rometer stood at 29.4 inches, and Fahrenheit's thermometer at 60°. The mean of five distances between the moon and sun's nearest
limbs was 44° 33′ 45", the altitude of the sun's lower limb 22° 4′ 15",
and the altitude of the moon's upper limb 6° 6′ 0".
Time at ship 23 ^d 20 ^h 18 ^m 30 To this time by estimation.
Longitude in time 8 0 0 the sun's semidiameter is 15' 59"
Ext. Green time 24 4 18 30 augmentation 2
Ext. Green. time 24 4 18 30 augmentation 2
Obs. dist. n. l. 44° 33′ 45″ hor. parallax 58′ 49′
Sun's semidia. + 15 59 reduction to lat. 49° S. — 7
Moon's semidia. + 16 2 reduced parallax 58 42
Augmentation + 112 2 CE 14 IL CAIGAGE
App. cent. dist. 45 5 48
Alt. sun's l. l. 22° 4′ 15" alt. moon's u. l. 6° 6′
White the same of
Z. D. 67 55 45 log. # 2.15567 83 54 1. # 2.70124
Thermometer 66°.0 F. 9.99104
Barometer 29.4 E. 9.99123
The mometer of of a
The A S william of the Control of th
r=137".25 . 9.98184 9.98184
Or 2' 17".25 2.13751 $r' = 482''.3$ 2.68308
For the sun $or = 8' 2''.3$
$-0.104 \times (60-50) = \cdot 104 \times 10 = -1.04$
$+0.15 \times (30-29.4) = .15 \times .6 = +0.09$
COORE OF THE PROPERTY OF THE P
True refraction for the moon = 8 1 .35
Alt. sun's l. l. 22° 4' 15" Alt. moon's n. l. 6° 6' 0"
Dip to 30 feet — 5 27
1 Dist 20 21 51
21 58 48 6 0 33
Semidiameter + 15 59 Semidiameter augm. — 16 4
True dist
Semidiameter + 15 59 Semidiameter augm. — 16 4 App. alt. 22 14 47 App. altitude 5 44 29 40

[•] The necessary computations are readily and very accurately performed, according to the rules of spherical trigonometry from the tables contained in this work. There are several collections of tables, such as those of Mendoza Rios, Lax, Lynn, and Thomson, which, for general practice at sea, by abating something of rigorous accuracy, render the calculations more simple. Some of them, however, are rather bulky and expensive.

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Appuald assume the formation of the sections of the section of the s	9-17-1	Refrection	56-44'90."
Parallax +	3	Parallax in alt.	5 36 28 + 58 22
Sun's T. alt. 22 Alt. moon's a l. Red. par	12 33 6° 6′ 8′	Moon's true alt.	6 34 50 Secant 0.60247 P. L. 0.48663
Par in alt.			P. L. 0.48910

The reduction of the apparent to the true distance is effected by the solution of two spherical triangles. First the angle at the zenith is found from the triangle formed by the apparent senith distances and apparent distance. Next the true distance is computed from the angle at the zenith and the true zenith distances, and these two may be combined in the following manner.

App. alt.) 5 44 29 secant 0.0 Sum . 73 5 4 Half . 36 32 32 cosine 9.9 Difference 8 33 16 cosine 9.9 True alt.) 6 34 50 cosine 9.9 Sum . 28 47 23 cosine 9.9 Half . 14 23 42 Arc . 27 1 55 cosine 9.9 Sum . 41 25 37 sine 9.8 Difference 12 38 13 sine 9.3 True dist 44 43 30 Distingt 3 44 1 21 cosine 9.5 True dist 44 43 30 Distingt 3 44 1 21 cosine 9.5 True dist 44 3 30 Distingt 3 1 18 1 P. L. 0. Time past 3 1 18 1 P. L. 0. Time past 3 1 18 1 P. L. 0. Preced. time 3 animos a corong to guildenose gata in a cosine section, refine to the company to the section in a cosine section and the cosine section and the cosine section in a cosine section and the cosine section and th	A			
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True dist 44 43 30 Distinct 3 44 1 21 100 42′ 9″ P. L. O. 6 45 38 36 1 37 15 P. L. O. Time past 3 1 1 18 1 P. L. Time past 3 1 1 18 1 P. L. Time past 3 1 1 18 1 P. L. Time past 3 1 1 18 1 P. L. Time past 3 1 1 18 1 P. L. Time past 3 1 1 1 18 1 P. L. Time past 3 1 1 1 18 1 P. L. T		22 21 54	sino	9.580316
True dist	3		Sinc	3.000010
True dist		_		3.00
District 3 44 1 21 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1				
Time past 3 ^h 1 ^h 18 ^m 1 ^s P. L. 0. Time past 3 ^h 1 ^h 18 ^m 1 ^s P. L. 0. Preced. time 3 ambrova a barra training of the control of t			00.404.044	.
Time past 36 1h 18m 1 P. L. O. Preced. time 3 gailbread of substance of the control of the cont				0.000
Preced. time 3 animonal processors are constant or the constant of the constan	Ø	45 38 36	1 37 15 P. L.	0.26738
Preced. time 3 or recutsury connections are conducted from the content of the search according to according to the search of the	m······	· 15 10- 1.		-
e recussive properties as a count control of the rest ened, according these spectral energy and the second of the			P. L.	0.36310
··· tena	ericed, according as rock. There is rock. There is received accura-	to the second of	or definition of the second of the second temperal reported to a second temperal reported by the second second to the second of the second temperal reported by the second temperal reported by the second second temperal reported by the second temperal rep	are several context:

Difference

dmil rewel s'noom et Diet et lower limb	G 321 that of the	faw do2d Diff.	a'mus Means
Dist. at noon 42° 2° 44° 44° 45° 3° 9° 47° 18°	1 21 37	80.297nches, a'81	meter being
9 47 1	5 58 1 37	22 de guisy sys of	Time per w
AND ADDRESS OF THE PARTY OF THE	06 1 +	ound ut . As . 97	Longitude :
(1 ^h 18 ^m 1 ^s) × 4 = 5 get (from table XXX) seconds of time.	VII.) 1" of motion	n, that at a mean	rate gives 2
seconds of time. This, from the exp		CONTRACTOR OF THE PARTY OF THE	COLUMN TO SERVICE STATE OF THE
ences are all increasing	ng, must be sub	tracted from the	approximate
distance, and consequence To the approximate	time 4 ^h 18 ^m 1 ^s	ne approximate th	Augmentati
Add cor. from sec. d	iff. + 83 2*	and deleter	True semili
True T. at Greenwich	1 24 4 18 3	TET JA	Alt of sun
Computation of t	he time derived	from the figure in	page 70, X
9.98020	02088.8		ge 78.
Sun's T. alt. Sun's pol. dist.	22° 12′ 33″ 0 0 89 40 33 cc	secant 08	0.000007
datitude .	48 50 000 86	ecant: \$ 1270 13	0.181608
	160 43866		mys
35" 35' securit OffsH 7		INIE D	×9.223941
4 247 P. L. 0.和图7	58 9 0 0 si	ne 0 3 3 82	9.929129
4'14 P. L. 0.00944	parallas in alt. &	8, 38, 5	19.334685
Time from noon	1h 50m 48°.6 si	0 00 TE 0 1	9.667343
ELIBROS.	2	- (2 Th SU	oz median.
Time from noon	3 41 37.2	U SE IV	
35 45 0	24	ter + 15 56	nome (filters to
8App. time 23d	20 18 23.0	- 101-101-111	THE WILLIAM
App. T. Green. 24	COLUMN TOTAL		App. alt. Refraction
Lon. in time Lynn gives	7 59 40.0 = 1	19° 55′ 0″ West. 20 4 45″ W. ∫ ir	Parallax
Dynn gives		O AF	autical tables.

Ex. 2.—On September 12th, 1823, in latitude 26° 30' N., longitude by account 24° 30' W. at 5^h 34^m P. M. by watch, the altitude

9 45

[•] The equation of second difference happens to be small in this example. It may amount to 6 seconds of distance, 12 seconds of time, or 3' of longitude in some cases. The correction of second difference is taken from the usual table, and its effects estimated according to the moon's mean motion. It is performed more correctly, however, by means of Tables 3d and 4th immediately following this article, which have been computed by the author expressly for this purpose.

was 35° 35′, the distance meter being 30.28 inches	o was 7° 37', that of the rece of their nearest limbs 95's, and the thermometer 72 25 feet; what was the lon 5° 34° me + 1 36	19'58",, the hage- A Fahrenheit, the
Batimated Greenwich t Mooff's semidiameter at Correction for Greenwi	: noon 14'52'' paral	lax 54 37 c. for 7 10 11 5
Augmentation .	+ B reduce	orial par. 54.96
True semidiameter Alt. of sun's l. l. 7° 37'	14 58 red. 1 Moon's 35°	35' Tour't
434 · · · · · · · · · · · · · · · · · ·	log. 4 2.61318 Z.D. 454 P.P.3 260	P.P. 5' 133
Thermometer 73 4 Barometer 30 28	log. 0.00289	9.98020 T0.00289
Thermometer 72 4	log. 9.99902	9.60002
0r 6'	98".1 2.59898 778".3 38".1 or 1' 18".3 1 .3 alt. moon's l. l. 35° 0 .0 red. hor. par. 54' 2	log. 1.89428 35' secant 0.6997 4'' P. L. 0.51867
	36.8 parallax in alt. 44 1	4 P. L. 0.00944
Alt. sun's l. l. 7° 37' Dip to 25 ft. 4		25° 35′ 0′ 25° 41′ 38
7 32	2 semidiameter	88 30 4
Semidiameter + 15	- refraction .	35 45 0
App. alt. 7 47 Refraction — 6 Parallax	37 9 moon's true alt.	
Binfictionally 7-41	30	Definition
Observed distance Suh's senddiameter hom's semidiameter		95° 19′ 58″ + 131 58
App. central dist.		95 50 52
and it was a contract	iana ta	

^{*} The equetion of second and with the control of the compile in may mount to be second; if the control of the c

94	SPHER. MOLT SUDORTAMETE	
App. dista	95° 50′ 52″ Conji meringa shou	Нерви прресо
Sun's app. alt.	7 47 58 secant wan room	0.004036
Moon's app. alt.	35 45 1 secant	
Sum :	139 23 50 Astweet Date south to	aredde sees
observation	and the second second section in the last	a all
U.le	60 41 55 cosine	9.540277
	26 8 57 homocosine markets be	9,953107
Sun's true alt.	7 41 30 \ cosine	9.996075 9.905372
Moon's true alt.	36 27 56 cosine	Homaniotal
Sum	44 9 26	19.489539
The same of the sa	88 81 8	Zenith duch
Half .	22 4 43	Comment of Management
Arc	56 14 50 cosine	9.744770
Sum 20.0	78 19 33 Sine and TRA	9.990922
Difference	34 10 7 sine	9.749450
19,617080	075 7.7.9	-
(SWEETERS)	Opening a special of the second	19.740372
9.823540	45 TO 10 10 10 10 10 10 10 10 10 10 10 10 10	0.070106
Half dist	47 52 13 sine	9.870186
COORDINA	Exports Halle II ->	App. time
True dist.	95 44 20	Greenwich ti
	95° 44′ 26″	0.69716
THE RESERVE OF THE PARTY OF THE	95 8 17 1 21 56 P.L. 6 30 13	0.34181
CONSTRUCTION OF THE PARTY OF TH	The low of the Tax	0.35535
Time of first distan	ice and salvail for other than out h	
	The second secon	miltenemon:
Approximate app.	time at Green. 7 19 25	0 - 6 -
and of the distance	d the corection for second difference.	Mean and
Dist. at 3h 93° 46'	1st Diff. 2d Diff.	when the mile
6 95 8	17 A PERSON NOT THE SECOND THE PARTY OF THE	THE PERSON NAMED IN THE PERSON NAMED IN COLUMN
9 96 30	10 - 10 10 abidipated by Derill	then Tribit No
12 97 52	Z . Thermomonor of the	BUSINES DATE
To the approxim	nate time (1h 20m) × 4, or 5h 20m, an	d the mean
second difference -	- 7", the equation from Table XXV	II. 18 0'.9 or
added to the propo	nce the second difference is negative, ortional part of the distance compu	ted by even
proportion for the	approximate time, and consequently	it must be
subtracted from the	e approximate time, or in general th	is correction
for the time must l	be applied with a contrary sign to t	hat which is
	errecting an arc, or with the same sig	n as that of
Now 1° 21' 56"	1":: 3h: 2 of time nearly.	Alt of mn'e
	n may be performed by proportional	l logarithms,

Or this operation may be performed by proportional logarithms, Cr this operation may be performed by proportional logarithms, thus, Equation of sec. diff. 1"

Variation in 3^h, 1° 21′ 56"

Equation of 2d diff. 2 P.L. 2.69161

From approximate a		San San G	•	19** <u>95</u> ***q46
True apparent time	at Greenwick	ı .	7	19 23
To find the	apparent time	at the plac	e of observa	tion.
The reduced decl	ination is fou	nd as in th	e explanati	on of Table
IX. and XXVII., the Latitude 26° 30' Declination 4 17	nen 0'' N.	secant	•	0.048209 0.001214
Difference 22 12 Zenith dist. 82 18			~	.61
Sum 104 31 Difference 60 5	 23 half 52 37 half 30	15 42 2 48	sine sine .	9.898075 9.69958 2
- A. A. (1) (4) - A. (1) (4)				19.647080
\$50.450 Pr	2 ^h 47 ^m 4 ^s 2		sine	9.823540
App. time Greenwich time	5 34 8 7 19 23			. !
Longitude in time	1 45 15 V	V. = 26° 18	' 45" West.	
Or about two mittee on navigation, tice, a method too rinstruction. Ex. 3.—On the and longitude: 144 between the sun at the altitude of the the moon's upper lice of the grand Fahrenheit's the sun and Fahrenheit's the sun	nuch neglect 14th of June W. by accord nd moon was sun's lower list imb was 35° 3 the longitude,	work, coming of the party of th	oning theororesent plan atitude 28° at 20° 32°, o be 97° 22 36′ 40″, th height of the	y with pract of nautical 31' 10" N., the distance '40"; when, e altitude of he eye being
Estimated time, Ju Longitude 144° W	ne 14th, . in time	•		20° 32° ' 9 36
Approximate Greet To this time moon's Augmentation to 3	eemidiamete: 69 alt	r is 15′ 37″	hor. par. red. to lat. S	5 8 57' 18'' 281° — 2
Correct semidiame Alt. of sun's l.l. 44	° 36′.7	moon's	cor. hor. pa: u.l. 35° 38'.	7. 57 16 3
Thermometer 68 Eddineter 29 Thermometer 68	23 .3 lo. #1.7/ 9.9 .7 9.9 9.9	8401 95 63 9922	10 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	
r 56″.3	1.7	'5084, r 1'	17".4	1.88873

Sun's semidiameter 15' 4 Parallax in alt.	6		alt. 35° 39' r. 57′ 16″	sec. 0.09004 P.L. 0.49737
Alt. sun's l. l. 44° 36' Dip. to 20 feet — 4		par. in moon's	alt. 46 32 alt. u. l.	P.L. 0.58741 35° 38′ 20″ — 4 26 — 15 46
App. alt. 44 48 Refraction 4 44 48 Parallax	56 6	app. al refract paralla	ion .	35 18 8 - 1 18 + 46 32
True alt. 44 47 Observed distance of nea Sun's semidiameter Moon's semidiameter		true al	10 21 21 166 31 23 166	36 3 22 97° 22′ 40″ + 15 46 + 15 46
Apparent central distance Now to compute the c	orrectio		e oblique sen	97 54 12
Dr Young's method, then $d = 97^{\circ} \text{ which by to}$ $* = 45$ $*' = 36$	able I.	gives A	o time is de l	O To 15" and 2 for a variation i whence the tru-
an Workley	は対象の方	t stropped t stropped t stropped t stropped	OF LEAD	therists work
$\begin{array}{c} h - s = 0.44 \\ h - s' = 0.53 \end{array}$	THE T	100 1 TO 10	84	ohuning 90
As these give in Table 2" in all, it is necessary true distance when they	to subt	ract ther	sun and 1" fo n from the ap	or the moon, or parent or even
Apparent distance Sun's app. altitude Moon's app. altitude	44 4	54′ 12 ″ 18 0 18 8	secant secant	0.149004 0.088248
Sum	2000	0 10	cosine	8.240647
Difference Sun's true alt. Moon's true-altitude	44 4	17 10 3 22	cosine cosine cosine	9.994739 9.851100 9.907648
Half	40 0	5 16	te beside plus	18.231386
Arc Sum Difference	122 5	5 16 4 44	sine sine	9.923979
Carried and Street	I - 1	BEET	of the eye as	19.750153

Marie a	ENT TO HE	~ · n to plas			10.750166
Half dist.	. 4	8° 35′ 33 ₀	l″ sin		9.875076
स्त्रा १५ व्या संद्राह्म	!!; - - 9'	7 11 7	int.	*i :	A
Cor. for oblique	e semidia	-i, 2 	.41		
True dist. Dist. at Dist. at	. 6°.9°	7 11 5 7 18 52 5 47 0			P.L. 0.30311
P. 1			⊕ h	15- 1 5- 1	P.L. 1.07500
• • <u>•</u> • • • • • • • • • • • • • • • •		•			11
Dist. at 3 98°	51' 7"	00/ 1-//		15 15	
> 1.6 .97 - 24 7	18 52 1 47 0 1	32′ 15″ 31 52 31 29	— 23 — 23	" Mea — 2	3" "
n To 15 ^m and 2 for a variation of whence the true after the noon of	3" the equat of 1° 32' near e time is 6° 13	ion of se	cond, d 2° of the 15th	ifference in time to be of June,	s 1,", which, e subtracted, or 30° 15° 12°
	To co	mpute th			
True altitude Polar distance Latitude	• •	44° 47 66 41 28 31	10	cosecant secant	0.036999 0.056193
Sym .	•	139 59	40		• •
Helf Difference	•	69 59 25 12		esine sine	9.534111 9.629 36 4
			,	1	19.256000
	• .;	1° 40	° 85•.3	sine .	9.628339
Time from noon	•	1 3 21 24	10 .6		991 199
Apply time 14th	eenwich	20 38 30 15		•	29
Longitude 4. On the 29t tade by account has son the mora mean of five secretary 16'; the land the height of the secretary 16'; th	97° W. at abon's nearest lits of observat wer limb was parometer bei	1826, in 1 out 7° 20° mb and t ions, 61° 32° 4′; ng 29.2° ir	atitude P. M., he star 56′ 30″ the obs	the obser Fomalhau ; the obse served alt ne thermore	, and longi- ved distance, it, was, from rved altitude itude of the neter 42° F.

DE

Est. time 7 ^h 2 ^m Long. in time 6 28	moon's equatorial hor. par. 58' 14" sun's 9" reduction for lat. 56° S. — 8
The state of the s	Olion's opp alt 32 16 35 secant
Est. G. time 13 30	reduced hor. par. 58 6 moon's semidiameter 001 15 52
9.805067	augmentation to 32° 00 + 9 MaH
008066'6	augm semidiameter 1 16 1
Now to correct the of from Tables I. and II.	blique semidiameter by Dr Young's method
dana = 62° gives A =	5 in Table I.
\$ = 6	Camping Se charge II o
s' = 32	Half 19 33 22 U
789598.0	Arc 38 5 49 coine 6
100	
15 15 03 9998786	Sam 57 39 11 10 sinc 6
000±20== 50 h—s== 44	81 72 56 M A
19.429166	THE RESERVE OF THE PERSON OF T
Sum	170 give Cor. = 0 in table II.
Observed distance	61° 56′ 30″
Moon's aug. semidiamet	er + 16 1
White the stant to	60 10 91
App. central distance	dt. of moon's l. l. 32° 4′ 62 12 31
12808.0	AZ DE LE COLLEGE
Z. D. 83 44 log.	2.69110, Z. D. 57 56 log. # 1.96844
Thermometer 42° F.	0.00730
D	0.00000
Barometer 29.2 in	9.98826
Thermometer 42°	0.06034
CONTRACTOR OF THE PROPERTY OF	0.06034
Thermometer 42°	9.99590 9.99590 9.99590
Thermometer 42°	9.99590 9.99590 9.99590
Thermometer 42° 1 1 1 1 2 2 486". Or = 8' 6 .	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
Thermometer 42° 2 486". Or = 8' 6 . -0''.1 x -8 = + 0 .5	9.99590 9.99590 9.99590 4 2.68700
Thermometer 42° = 486". Or = 8' 6 . -0'.1 x -8 = + 0 . 0'.14 x ·8 = + 0 .	9.99590 9.99590 9.99590 4 2.68700 $r = 1' 32'' \log$ 1.96434 8 Moon's alt. 32° 4' secant 0.07190
Thermometer 42° = 486". Or = 8' 6 . -0''.1 x -8 = + 0 .3 0'.14 x .8 = + 0 .3	9.99590 9.99590 9.99590 1 2.68700
Thermometer 42° Or = 8' 6 . O'.1 x -8 = + 0 . O'.14 x .8 = + 0 . Thermometer 42°	0.06034 9.99590 9.99590 9.99590 9.99590 1 2.68700 r = 1' 32" log. 1.96434 Moon's alt. 32° 4' secant 0.07190 Hor. par. 58' 6" P.L. 0.49110 Par. in alt. 49' 14" P.L. 0.56300
Thermometer 42° Or = 8' 6 . O'.1 x -8 = + 0 . O'.14 x 8 = + 0 . Alt. of star Alt. of star	0.06034 9.99590 9.99590 9.99590 9.99590 9.99590 1.96434 Moon's alt. 32° 4' secant 0.07190 Hor. par. 58' 6" P.L. 0.49110 Par. in alt. 49' 14" P.L. 0.56300 0" alt. of moon's l. l. 32° 4' 0
Thermometer 42° Or = 8′ 6 . O'.14 × 8 = + 0 . Alt. of star 6° 16′ Dip. to 20 feet — 4 2°	0.06034 9.99590 9.99590 9.99590 9.99590 9.99590 1.96434 Moon's alt. 32° 4' secant 0.07190 Hor. par. 58' 6" P.L. 0.49110 Par. in alt. 49' 14" P.L. 0.56300 0" alt. of moon's l. l. 32° 4' 0 dip. to 20 feet — 4 26
Thermometer 42° Or = 8′ 6 Or = 8′ 6 O'.1 x -8 = + 0 O'.14 x ·8 = + 0 Alt. of star 6° 16′ Dip. to 20 feet - 4 App. alt. 6 11 :	0.06034 9.99590 9.99590 9.99590 9.99590 9.99590 1.96434 3 Moon's alt. 32° 4′ secant 0.07190 Hor. par. 58′ 6″ P.L. 0.49110 0″ alt. of moon's l. l. 32° 4′ 0′ dip. to 20 feet 4 26 34 31 59 34
Thermometer 42° Or = 8′ 6 . O'.14 × .8 = + 0 . Alt. of star 6° 16′ Dip. to 20 feet — 4 2°	0.06034 9.99590 9.99590 9.99590 9.99590 9.99590 1.96434 Moon's alt. 32° 4' secant 0.07190 Hor. par. 58' 6" P.L. 0.49110 Par. in alt. 49' 14" P.L. 0.56300 alt. of moon's l. l. 32° 4' 0 dip. to 20 feet 4 26
Thermometer 42° or = 8' 6 . or = 8' 6 . o'.1 x - 8 = + 0 . o'.14 x · 8 = + 0 . Alt. of star 6° 16' Dip. to 20 feet - 4 2 App. alt. 6 11 3 Refraction - 8	0.06034 9.99590 9.99590 9.99590 9.99590 9.99590 1 2.68700 r = 1' 32" log. 1.96434 3
Thermometer 42° Or = 8′ 6 Or = 8′ 6 O'.1 x -8 = + 0 O'.14 x ·8 = + 0 Alt. of star 6° 16′ Dip. to 20 feet - 4 App. alt. 6 11 :	0.06034 9.99590 9.99590 9.99590 9.99590 9.99590 9.99590 1.96434 3
Thermometer 42° Or = 8' 6 . Or = 8' 6 . O'.1 x - 8 = + 0 . O'.14 x · 8 = + 0 . Alt. of star 6° 16' Dip. to 20 feet - 4 . App. alt. 6 11 3 Refraction - 8 True alt. of star 6 3 .	0.06034 9.99590 9.99590 9.99590 9.99590 9.99590 9.99590 1.96434 3
Thermometer 42° or = 8' 6 . or = 8' 6 . o'.1 x - 8 = + 0 . o'.14 x · 8 = + 0 . Alt. of star 6° 16' Dip. to 20 feet - 4 2 App. alt. 6 11 3 Refraction - 8	0.06034 9.99590 9.99590 9.99590 9.99590 9.99590 9.99590 1.96434 3 Moon's alt. 32° 4' secant 0.07190 Hor. par. 58' 6" P.L. 0.49110 9 Par. in alt. 49' 14" P.L. 0.56300 alt. of moon's l. l. 32° 4' 0 dip. to 20 feet 31 59 34 7 semidiameter 4 16 1 9 app. alt. centre 32 15 35 refraction 7 1 32 par. in alt. 49 14
Thermometer 42° Or = 8' 6 . Or = 8' 6 . O'.1 x - 8 = + 0 . O'.14 x · 8 = + 0 . Alt. of star 6° 16' Dip. to 20 feet - 4 . App. alt. 6 11 . Refraction - 8 True alt. of star 6 3 .	0.06034 9.99590 9.99590 9.99590 9.99590 9.99590 9.99590 9.99590 1.96434 3
Thermometer 42° Or = 8′ 6 . Or = 8′ 6 . O'.1 x - 8 = + 0 . O'.14 x · 8 = + 0 . Alt. of star 6° 16′ Dip. to 20 feet - 4 . App. alt. 6 11 . Refraction - 8 True alt. of star 6 3 .	9.99590 9.99590 9.99590 4 2.68700 $r = 1' 32'' \log$ 1.96434 3 Moon's alt. 32° 4' secant 0.07190 Hor. par. 58' 6'' P.L. 0.56300 alt. of moon's l. l. 32° 4' 0' dip. to 20 feet 24 26 34 semidiameter 4 26 37 app. alt. centre 32 15 35 refraction 9ar. in alt. 49 14 true alt. centre 33 3 3 17
Thermometer 42° Or = 8′ 6 . O'.1 x -8 = + 0 . O'.14 x ·8 = + 0 . Alt. of star 6° 16′ Dip. to 20 feet — 4 2 App. alt. 6 11 3 Refraction — 8 True alt. of star 6 3 2	9.99590 9.99590 9.99590 2.68700 $r = 1' 32'' \log. 1.96434$ Moon's alt. 32° 4' secant 0.07190 Hor. par. 58' 6'' P.L. 0.49110 Par. in alt. 49' 14" P.L. 0.56300 o'' alt. of moon's l. l. 32° 4' 0' dip. to 20 feet 4 26 31 59 34 7 semidiameter 4 16 1 27 app. alt. centre 32 15 35 refraction 9 1 32 15 35 refraction 9 1 32 14 49 14 true alt. centre 33 3 3 17
Thermometer 42° Or = 8′ 6 Or = 8′ 6 O'.1 x -8 = + 0 O'.14 x ·8 = + 0 Alt. of star 6° 16′. Dip. to 20 feet — 4 App. alt. 6 11 Refraction — 8 True alt. of star 6 3 True alt. of star 6 3 Alt. of star 6 App. alt. 6 Refraction — 8	9.99590 9.99590 9.99590 4 2.68700 $r = 1' 32'' \log$ 1.96434 3 Moon's alt. 32° 4' secant 0.07190 Hor. par. 58' 6'' P.L. 0.56300 alt. of moon's l. l. 32° 4' 0' dip. to 20 feet 32° 4' 0' 4 26 34 semidiameter 4 26 37 app. alt. centre 32 15 35 refraction 9 1 32
Thermometer 42° Or = 8′ 6 . O'.1 x -8 = + 0 . O'.14 x ·8 = + 0 . Alt. of star 6° 16′ Dip. to 20 feet — 4 2 App. alt. 6 11 3 Refraction — 8 True alt. of star 6 3 2	9.99590 9.99590 9.99590 4 2.68700 $r = 1' 32'' \log$ 1.96434 3 Moon's alt. 32° 4' secant 0.07190 Hor. par. 58' 6'' P.L. 0.56300 alt. of moon's l. l. 32° 4' 0' dip. to 20 feet 32° 4' 0' 4 26 34 semidiameter 4 26 37 app. alt. centre 32 15 35 refraction 9 1 32

Star's merid dist E R 45 31

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		men a serio abre de MOORI		
Star's app. al	t 6-11	noon s equatel his ed terms ter to k	h h h	
Moon's app.	Mt. 32 19	30 secant		U.U/201U
रो स	·	edicos kar ganda geomico extensi	or seeding	क्षेत्र के अ
Sum &	100 39	🔐 was en est a est	•	
Half :.	50 19	50: gostae	•	9.805067
Diff.	11 58	50: notine: 41: cosine: 27 desine:		9.990000
Omes true at	. 0 8	¥7 desine	ng tinto in the ent ropy een	9,997,508
Moon's t. alt.	, 83 3	17 cosine	•	9,923322
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Sum .	39 0	77	, , , , , , , , , , , , , , , , , , , ,	10./21250
Half .	19 33	 00	• .	
Arc .	38 5			0.905057
	50 5	- Coeille	3()	3.050007
Sum .	57 39	11 sine		9.920766
Diff.	18 32	27 sine) <i>i</i> .	9.502400
	10 00	-,	*4	d
		•		19.429166
14 11 14 14 15 18 14 14 16		•		
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-		2	0 - 1196 126	Alega B
£ 6, 3,				
True dist.	62 26	13	ل در وال الانتخار . در مطالعه و . مواهد	10 00004
Dist. at	12 ^h 63 10			0.60724
### 6 C	15 01 41	45 1 28 5	66 P.L.	0.30621
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Preceding hot	nise	12		ot etal and
I recearing no	•	24		Therener
			3, 144	
Approximate	Appi, time	13 80 0 at G		
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Approximate 64 40 19	1, 33, 90.		reenwich.	
61 41 45	1 28 56		reenwich.	4" nearly
61 41 45	1 28 56 1 28 11	42" 45	reenwich 48#.5 or 4	4' nearly
61 41 45	1 28 56 1 28 11	42" 45	reenwich 48#.5 or 4	4' nearly
61 41 45 660 13 35 01 Now to an	1 28 56 1 28 11 proximate t	- 42" - 45 ime 1 30", and s	reenwich. 437.5 or — 4 erond difference	" nearly "() " 44"; the
61 41 45 60 13 35 00 13 35 equation of a	1 28 56 1 28 11 proximate t	- 42" - 45 ime 1" 30", and s enter is 5".5, to	econd difference which and variations when 112	"nearly "O "10"; the
61 41 45 60 13 35 01 Now to any equation of a coverly in 3 ho tracted. Wh	1 28 56 1 28 11 proximate to cond differ ours, the fir ence from 1	— 42" — 45 ime 1" 30", and s ence is 5".5, to al equation in ti 3":35" this equat	reenwich. 43".5 or — 4 econd difference which and varia mg is about 11' ion of 11' being	nearly 10 10 20 20 20 20 20 20 20 20
61 41 45 60 13 35 01 Now to any equation of a coverly in 3 ho tracted. Wh	1 28 56 1 28 11 proximate to cond differ ours, the fir ence from 1	— 42" — 45 ime 1" 30", and s ence is 5".5, to al equation in ti 3":35" this equat	reenwich. 43".5 or — 4 econd difference which and varia mg is about 11' ion of 11' being	nearly 10 10 20 20 20 20 20 20 20 20
61 41 45 60 13 35 01 Now to any equation of a consarly in 3 had tracted. Who	1 28 56 1 28 11 proximate to econd differ ours, the fir ence from 1 rent time is	— 42" — 45 ime 1" 30", and sence is 5".5, to all equation in ti 3" 35" this equat 13" 35" 40" at 6	reenwich. 43".5 or — 4 econd difference which and varia mg is about 11' ion of 11' being	nearly 10 10 20 20 20 20 20 20 20 20
61 41 45 60 13 35 01 Now to any equation of a consarly in 3 ho tracted. Who other true apparents	1 28 56 1 28 11 proximate to cond differ ence from 1 rent time is To compu	— 42" — 45 ime 1" 30", and sence is 5".5, to al equation in ti 3" 30" this equat 13" 30" 49" at G to this apparent t	even wich. 43".5 or — 4 evend difference which and varia me is about 11' ion of kl' being freen with.	1" nearly 10 4 140; the sión 10 29 the substracted, to the substracted, the substracted substr
61 41 45 60 13 35 01 Now to any equation of a consarly in 3 ho tracted. Who other true apparents	1 28 56 1 28 11 proximate to cond differ ours, the fir ence from 1 rent time is To comput 6 8 2 59 27	— 42" — 45 ime 1° 30°, and sence is 5° 5, to all equation in the 3° 30° this equat 13° 30° 49° at G to this apparent to 6°	even wich. 43".5 or — 4 evend difference which and varia me is about 11' ion of kl' being freen with. ime at ship.	# nearly # 420, the side # 29' to be sub- stubtracted, the first A. 2 0.064653
61 41 45 60 13 35 01 Now to an equation of a conserly in 3 ho offacted. Wh the true appar Stars the alt Polar dist. Latitude	1 28 56 1 28 11 proximate to cond differ ours, the fir ence from 1 rent time is To comput 6 8 2 59 27	— 42" — 45 ime 1" 30", and sence is 5".5, to al equation in ti 3" 30" this equat 13" 30" 49" at G to this apparent t	even wich. 43".5 or — 4 evend difference which and varia me is about 11' ion of kl' being freen with. ime at ship.	1" nearly 10 4 140; the sión 10 29 the substracted, to the substracted, the substracted substr
61 41 45 60 13 35 Off Now to any equation of a copearly in 3 he tracted. Whi othe true appar Star's true alt Polar dist. Latitude	1 28 56 1 28 11 proximate to econd differ ours, the fir ence from 1 rent time is To compute 6° 8′ 5 59 27 4 56 13°	- 42" - 45 ime 1 30", and sented is 5",5, to all equation in the 30" 40° at G at the apparent to 60".	even wich. 43".5 or — 4 evend difference which and varia me is about 11' ion of kl' being freen with. ime at ship.	#" nearly #-14%; the 1506 # 29' to be sub- subtracted, 15 15 15 15 15 15 15 15 15 15 15 15 15
60 13 35 011 Now to any equation of a conservy in 3 h officeted. Wh other true apparent point dist. Latitude 25 21 28	1 28 56 1 28 11 proximate record difference from 1 rent time is To compute 6° 8′ 5 59 27 4 56 12°	42" 45 ime 1 30", and sence is 5",5, to all equation in the 3" 30" this equation in the this apparent to 6" 13 20" 49" at 6" 16 49" 16 49" 16 49"	even wich. 43".5 or — 4 evend difference which and varia ms is about 11' ion of k1' being freen with. hame at ship. cosecant secant	#" nearly #-14%; the 1506 # 29' to be sub- subtracted, 15 15 15 15 15 15 15 15 15 15 15 15 15
of 1 41 45 060 13 35 011 Now to any equation of a coparty in 3 h corrected. Who the true appar bear true appar bear true 1 Polar dist. 1 Latitude 36 31 28	1 28 56 1 28 11 proximate record difference from 1 rent time is To compute 6° 8′ 5 59 27 4 56 12°	42" 45 ime 1 30", and sence is 5",5, to all equation in the 3" 30" this equation in the this apparent to 6" 13 20" 49" at 6" 16 49" 16 49" 16 49"	even wich. 43".5 or — 4 evend difference which and varia ms is about 11' ion of k1' being freen with. hame at ship. cosecant secant	#" nearly 10 10 10 10 10 10 10 10 10 1
61 41 45 660 13 36 600 13	1 28 56 1 28 11 proximate record difference from 1 rent time is To compute 6° 8′ 5 59 27 4 56 12°	42" 45 ime 1 30", and sence is 5",5, to all equation in the 3" 30" this equation in the this apparent to 6" 13 20" 49" at 6" 16 49" 16 49" 16 49"	econd difference which and variants is about 11 ion of 11 being freenwith. cosecant secant	#" nearly #
61 41 45 660 13 36 600 13	1 28 56 1 28 11 proximate to econd differ ours, the fir ence from 1 rent time is To compute 6° 8′ 5 59 27 4 56 13°	42" 45 ime 1 30", and sence is 5",5, to all equation in the 3" 30" this equation in the this apparent to 6" 13 20" 49" at 6" 16 49" 16 49" 16 49"	econd difference which and variation of kl' being freenwith.	#" nearly 10 4 14 15 the side # 29 the substracted, 15 15 16 16 16 16 16 16 16 16 16 16 16 16 16
of 41 45 of 41 45 of 41 45 of 13 35 of Now to any equation of a conservy in 3 hy of tracted. Who othe true appara othe true appara 1 Post dist. Latitude	1 28 56 1 28 11 proximate record difference from 1 rent time is To compute 6° 8′ 5 59 27 4 56 12°	42" 45 ime 1 30", and sence is 5",5, to all equation in the 3" 30" this equation in the this apparent to 6" 13 20" 49" at 6" 16 49" 16 49" 16 49"	econd difference which and variants is about 11 ion of 11 being freenwith. cosecant secant	#" nearly #
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61 41 45 660 13 36 600 13	1 28 56 1 28 11 proximate record difference from 1 rent time is To compute 6° 8′ 5 59 27 4 56 12°	42" 45 ime 1 30", and sence is 5",5, to all equation in the 3" 30" this equation in the this apparent to 6" 13 20" 49" at 6" 16 49" 16 49" 16 49"	econd difference which and variants is about 11 ion of 11 being freenwith. cosecant secant	4" nearly
61 41 45 660 13 36 600 13	1 28 56 1 28 11 proximate record difference from 1 rent time is To compute 6° 8′ 5 59 27 4 56 12°	— 42" — 45 ime 1° 30°, and sence is 5°,5, to all equation in till 3° 30° 40° at G to the the apparent to 6° 6° 6° 6° 6° 6° 6° 6° 6° 6° 6° 6° 6°	econd difference which and varies which and varies is about 11 ion of k1 being breenwith. Sime at ship. cosecant secant cosine sine	4" nearly
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Star's merid. distance E. Star's R. A.		45 ^m 48					
R. A of merid. Sun's R. A.		33 32		_			
App. time at ship App. time at Green.		. 1 29					
Long. in time Without Eq. 2d diff.	6	28 28	43 54	= 97° = 97	10′ 13	45″ 30	W. W.
Error .					2	45	w.

TABLE I.

CORRECTION FOR THE OBLIQUE SEMI-DIAMETER.

For Argument A.

					For	Argu	ımen	t A	•			
•	For	h h	s	d	For	h h-	-s	d	For	h h-	-5	d
1			_	.		_		L	_ 1	_	<u> </u>	
1	•	Ā	<u> </u>	A	•	Ā	<u> </u>	$\overline{\mathbf{A}}$	٥	Ā	~	A
	89	924	1	176	59	71	31	29	29	94	61	6
	88	954	2	146	58	72	32	28	28	95	62	5
	87	972	3	128	57	74	33	26	27	95	63	5
	86	984	4	116	56	75	34	25	26	95	54	5
	85	994	5	106	55	76	35	24	25	96	65	4
	٠.				54	77	36	23	24	96	66	4
	84	2	6	98	53	78	37	22	23	96	67	4
	83	9	7	91	52	79	38	21	22	97	68	3
1	82	14	8	86	51	80	39	20	21	97	69	3
1	81	19	9	81	50	81	40	19	20	97	70	3
	80	24	10	7 6						•	•	
	79	28	11	72	49	82	41	18	19	98	71	2
	78	32	12	68	48	83	42	17	18	98	72	. 2
	77	3 5	13	65	47	83	43	17	17	98	73	2
	76	38	14	62	46	84	44	16	16	98	74	2
	75	41	15	59	45	85	45	15	15	98	75	2
	74	44	16	56	44	86	46	14	14.	99	76	1
- 1	73	47	17	53	43	86	47	14	13	99	77	1
	72	49	18	51	42	87	48	13	12	99	78	1
	71	51	19	49	41	88	49	19	11	99	79	1
•	70	5 3	20	47	40	88	50	19	10	99	80	1
	69		21	45	39	89	51	11	9	99	81	1
	68	57	22	43	38	90	52	10		100	· 82	0
	67	59	23	41	37	90	53	10	7	100	83	0
	66	61	24	39	36	91	54	9	1 -	100	84	. 0
	65	63	25	37	35	91	55	9	5	100	85	0
	64	64	26	36	34	92	56	8		100	46	0
-	63	66	27	34	33	92	57	7		100	87	0
	62	67	28	33	32	93	58	7	2	100	88	0
	61	69	29	31	31	93	59	7	1	100	89	0
	60	70	30	30	30	94	6 0	6	0	100	90	0

TABLE II.

CORRECTION FOR THE OBLIQUE SEMI-DIAMETER.

DIMINUTION OF THE SEMI-DIAMETER.

Argument A(h) + A(h-s) + A(d).

					A	ltitud	le.				5			
Sum of A	5°	6°	70	80	90	10°	11°	12°	140	16°	180	20°	30°	45
0"	25"	19"	14"	11"	9"	8"	6"	5"	4"	3"	3''	2"	1"	1"
20	24	18	14	11	9	7	6	5	4	3	2	2	1	0
40	23	17	13	10	8	7	6	5	4	3	2	2	ī	0
60	21	16	12	9	8	6	5	5	3	3	2	2	1	0
70	20	15	12	9	8	6	5	5	3	3	2	2	1	0
80	19	14 -	11	8	7	6	5	4	3	2 -	-2	9	1	0
90	17	13	10 -	- 8	7	6	5	4	3	2 2	2	2	1	0
100	16	12	9	7	6	5	4	4	3	2	2	1	1	0
110	14	10	8	6	5	4	3	3	2	2	1	1	1	0
120	11	9	7	5	4	3	2	3 2 2	2	10	1	-1	0	0
130	9	7	5	4	3	3	2	2	1	15	1	11	0	0
135	7	6	4	3	2	2	2	1	1	11	1	0	0	0
140	16	5	4	3	2	2	1	1	1	1:	1	0	0	0
145	-5	4	3	2	2	1	1	1	1	0	0	0	0	0
150	3	3	3 2 2	2	1	1	1	1	0	0	0	0	0	0
155	3	2		1	1	1	1	0	0	0	0	0	0	0
160	1	1	1	0	0	0	0	0	0	0	0	0	0	0
170	0	0	0	0	0	0	0	0	0	0	0	0	0	0
178	1	1	1	0	0	0	0	0	0	0	0	0	0	0
180	2	1	1	1	1	1	0	0	0	0	0	0,	0	0
182	:3	2	2	1	1	1	1	0	0	0	0	0	0	0
184	4	3	2	2	1	1	1	1	1	1	0	0	0	0
186	5	4	3	2	2	2	1	1	1	1	1	1	0	-
188	7	6	4	3	2	2	2	1	1	1	1	1	1	_
190	9	7	5	4	3	3.	2	2	1	1	1	1	1	_
191	10	8	6.	4	4	3	3	2	2	1	1	1	1	_
192	11	9	7	5	4	4	3	3	2	2 2 2	1	1	1	_
193	12	. 9	7	5	5	4	3	3	2	2	2	1.	1	_
194	14	10	8:	6	5	4	4	3	2	2	2	2	1	-
195	15	11	9	6	6	5	4	4	3	2	2	2	-	-
196	17_	13	10	7	6	6	5	4	3	3	2	2	-	-
197	19	14	11	8	7	6	5	5	3	3	2	2	-	_
198	21	.16	12:	9	8	7	6	5	3	3	3	-	-	_
199	23	170	13	10	8	8	6	5	4	-	-	+	-	_
200	25	19	14	11	9	-44	-	-	-	-	-	+	-	-
Alt	5°	60	70:	30	90	100	110	19	140	160	180	20°	309	45

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Equations of Second Difference for Three Hours.

One	EQUAT	EVIDEDO	SECOND	DIFFE	RENCE FO	RIHREE	Hours.
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-sth	Time,	10 20 30 4	0 50 60 70	80 90 10	0 1 2 3	4 5 6 7	S 9 M.
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In sol	6 54 9 51		0.6 0.8 1.0 1.1			0.1 0.1 0.1 0.1 0 0.1 0.1 0.1 0 2 0	
Lagran	12 48 15 45	0.3 0.6 0.9 1	.2 1.6 1.9 2.2			0.10.20.20.20 $0.20.20.30$	2 0.3 4 56
JA.	18 42	0.5 0.9 1.4 1	.8 2.3 2.7 3.2	3.6 4.1 4 4.1 4.6 5	5 0,0 0.1 0.1	$0.2 \ 0.2 \ 0.3 \ 0.3 \ 0.3 \ 0.4 \ 0$	4 0.4 6 54
ri un	21 39 24 36	0.6 1.2 1.7 2	3293540	4.6 5.2 5	80.10.102	0.2 0.3 0.3 0.4 0	5 0.5 8 52
-	97 33 0 30 2 30	Market Street, Street, by	The second secon	State of the last	The second second	$0.3 \ 0.3 \ 0.4 \ 0.4 \ 0.5 \ 0.3 \ 0.4 \ 0.5 \ 0.5 \ 0.4 \ 0.5 \ 0.5 \ 0.4 \ 0.5 $	The second second second
AL STE	33 27	0.7 1.5 2.2 3	103.7445.2	6.0 6.7 7		$0.3 \ 0.4 \ 0.4 \ 0.5 \ 0$ $0.3 \ 0.4 \ 0.5 \ 0.6 \ 0$	
Killines	39 21	0.8 1.7 2.5 3	44.25.15.9	6.8 7.6 8	.5 0.1 0.2 0.3 0	0.4 0.4 0.5 0.6 0	7 0.8 13 47 7 100
-m s	45 15	0.9 1.9 2.8 3	18 4.7 5.6 6.6	7.5 8.4 9	.4 0.1 0.2 0.3 (0.4 0.5 0.6 0.7 0	8 0.8 15 45
130	51 9	1.0 2.0 3.0 4	.1 5.1 6.1 7.1	8,1 9,1 10	20.10.20.30	$0.4 \ 0.5 \ 0.6 \ 0.7 \ 0.4 \ 0.5 \ 0.6 \ 0.7 \ 0.7 \ 0.4 \ 0.5 \ 0.6 \ 0.7 \ 0.7 \ 0.8 \ 0.7 \ 0.8 $.8 0.9 17 43
ateria	54 6 57 3					$0.4 \ 0.5 \ 0.6 \ 0.7 \ 0.4 \ 0.5 \ 0.6 \ 0.8 $	
RE JUI	1 02 0					0.4 0.6 0.7 0.8 0	
Manda	6 54	1.2 2.3 3.5 4	6 5.8 7.0 8.1	9.3 10.5 11	6 0.1 0.2 0.3 6	5 0.6 0.7 0.8 0	9 1.0 22 38
RIGHE	9 51 12 48	1.224 3.64		9.6 10.8 12	0 0.1 0.2 0.4 0	0.5 0.6 0.7 0.8 0.5 0.6 0.7 0.8 1	0 1.1 24 30
of the	15 45 18 42	1.2 2 5 3.7	96.17.48.6	9,8 11.1 12	3 0.1 0.2 0.4 0	$0.5 \ 0.6 \ 0.7 \ 0.9 \ 1$ $0.5 \ 0.6 \ 0.7 \ 0.9 \ 1$	0 1.1 26 34
	21 39 24 36	1.2 2,5 3,7	5.0 6.2 7.5 8.7 1	0.0 11.2 12	4 0.1 0-2 0.4 (0.5 0.6 0.7 0.9 1 0.5 0.6 0.7 0.9 1	.0 1.1 28 32
Kapla	27 33	1.2 2.5 3.7 5	0 6.2 7.5 8.7 1	0.0 11.2 12	.5 0.1 0.2 0.4 0	$0.5 \ 0.6 \ 0.7 \ 0.9 \ 1$ $0.5 \ 0.6 \ 0.8 \ 0.9 \ 1$	0 1.1 29 31
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т	2		5,8		11.6	14.5	17.4	20.3	23,2	26.1	29.0	0.3	0.6	0.9	1.2	1.5	1.7	2.0	2.3	2,6
н	4	2.8		8.4		14-1	16.9	19.7	22,5	25,3	28.1	0.3	0.6	0,8	101	1.4	1.7	2.0	2,2	2.5
и	6 8	2.7		8.2							27.3							1.9	2,2	2-5
	10	2.6		7.7	10.0	13.5	15.4	18.0	21.2	23.8	26.5	0.3	0.5	0.8	1.0	1.3	1.5	1.9	2.1	2 9
т	12			7.5							25.0								2.0	23
и	14		4-9	7.3	9.7	15.5	14.6	17.0	19.5	21.9	24.3	0.2	0.5	0.7	1.0	1.2	1.5	1.7	2.0	2,2
м	16			7.1							23.7									2.1
ш	18			6.9	9-2						23.1									2,1
8	99	-	-	100	1	Printed Street	1	200			21.9			CONTRACT	2000	1000		1	200	2.0
ď	94			6.6							21.4									nin.
а	26			6.3		10.5	12,6	14.7	16.7	18.8	20.9	0.2	0-1	0.6	0.8	2,1	1.3			16
н	28	2.0	4.1	6.1	8.2	10.2	12.3	14.3	16,4	18.4	20.5	0,2	0.4	0.6	0.8	1.0	1,2		1.6	1.8
11	30			6.0		10-0	12.0	14.0	16.0	18.0	20.0	8.0	0.4	0.6	0.8	1.0	1.2	1.4	1.6	1.8
н	32			5.7	7.8						19.5									100
Ζi	36			5.6		9.4	11.2	13 1	15.0	16.9	18.7	0.2	0.4	0.6	0.8	0.9	1.1			1.7
и	38	1,8	2.7	5.5	7.3	9.2	11.0	12.9	14.7	16.5	18.4	0.2	0.4	0,6	0.7	0.9	1.1	1.3	1.5	1.7
4	40	1,8	3.6	5.4	7.2	9.0	10.8	12.6	14.4	16.2	18.0	_	-	_	-		_	1.3	1-4	11.0
1	42	1.8		5.3		8.8	10.6	12.4	14-1	15,9	17.6	0.2	0,4	0.5	0.7	0.9	14	1.2		1.0
и	46	110		5.1	6.9	8.7	10.4	12.1	13.8	15.6	17.3	0.2	0.4	0.5	0.7	0.9	1.0	1,2	1.2	16
п	46	16		5.0		8.9	10.0	11.7	13.0	15.0		0.2	0.3	0.5	0.7	0-8	1.0	1.2	1.3	H
п	50	1,6			6.5	8,2	9.8	11.5	13.1	14.7	16,4	0.2	0.3	0,5	0.7	0.8	1.0	1.2		1-5
и	52			4.8	6-4				12.9		16.1								1.3	1.4
1	54			4.7	6.3	7.9			12.6		15.8								1,3	1
ш	56			4.6	6.2	7.6	9.3				15.2								1.2	154
2	0	1,5	3.0	4.5	6.0	7.5					15,0								1.2	1.3

In the practice of lunars four persons are frequently employed in making the observations, the first to take the distance, the second to take the altitude of the sun or star, the third to take the altitude of the moon, and the fourth to write down the observations. One person, however, may make the whole himself, according to the following method, which was obligingly communicated by that distinguished practical navigator Captain Basil Hall. Speaking of his own practice, he says,—" I always take all my altitudes and distances with the same instrument. First the altitudes of the sun, then those of the moon, then several distances; next the altitudes of the moon, then those of the sun, and interpolating by proportional logarithms for the altitudes at the mean time of the distances. At night I never take an altitude, unless it be about twilight, when it can be done with accuracy and ease."

"The method which I use to connect lunars and chronometers is not very general, but infinitely the best, and ought to be universally adopted, as it renders all allowance for the distance run in the in-

terval of little or no consequence."

"The use of lunars at sea I conceive is, in a great degree, to check the chronometers: the method by lunars being infallible, though not very nice; that by chronometers being fallible, but as nice as possible. So that a number of lunars are necessary to check a chronometer, and the object is to bring the whole of such lunars to bear rigorously on the chronometer without making use of the

logboard.

"This will be best illustrated by an example. At noon, or any other hour during the day most convenient for taking a lunar, I observe a set, or half dozen sets of lunars with the sun, carefully noting what the chronometer shows, but without taking any account of the actual time. At any other hour when the sun is near the prime vertical, or most suitable for determining the time, I take altitudes expressly with this view, from which I discover the error of the same chronometer used for the lunars. Again, during the night I take lunar distances with the stars, on both sides of the moon if possible, at the moments most favourable, but never mind the exact time, only carefully recording what the chronometer shows. Now by the sights for absolute time I ascertain what was the error of the chronometer on apparent time at that meridian, and this same error, corrected for rate during the interval, I apply to each of the different times by the chronometer when the lunars were taken. By this means I get the apparent times due to the meridian, on which the absolute time sights were taken, with as much accuracy as if the whole, lunars and all, had been taken at that fixed meridian. The distances give the several times at Greenwich, and thus they all concur in settling the difference of time, between the first meridian and that chosen for taking the time, with a view of seeing what longitude the chronometer gives. Hence, if there had been an unpossibly be taken, still the result would not be vitiated thereby, but all the lunars would be found to contribute to the same end, thus making, according to Dr Wollaston's simile, the moon serve the purpose of a great Greenwich clock in the heavens. After having

This is always to the method given in Norie's Navigation.

9.99460

determined the true longitude and error of the chronometers when within a few days sail of the land, I run the remainder of the voyage, in a great degree, by the chronometers alone."

On finding the Longitude.

The foregoing method of finding the longitude by lunars is very valuable at sea, on account of the frequent opportunities which occur for observation. About the time of new moon, and in unsteady weather, the necessary observations for the practice of this method cannot be obtained, and the dead reckoning is not to be depended on for any length of time, therefore recourse must be had to other methods.

On account of the very high degree of perfection to which chronometers have been brought, the longitude determined by a mean of three or four of these delicate machines merits great confidence. If the rate of a chronometer be determined on shore, or rather perhaps on board in the situation it is intended to occupy during the voyage, where the various causes which act upon it, and are likely to alter its rate, are in operation, it is likely this rate will remain pretty uniform for some time, and the amount of the gain or loss, being allowed for on the time indicated by it at any future period, the true time may be obtained at the meridian of the place where its rate and original error was determined, with as much accuracy as if it had been adjusted to go accurately to mean solar time on that meridian. Hence, it is obvious, that if the original error. and the gain or loss in 24 hours, called the daily rate, of a chronometer, be known, on any meridian, such for example as that of Greenwich; by making proper allowance for these, the mean time at Greenwich may be readily known to such a degree of accuracy as the going of the chronometer will warrant.

It is now only necessary to find the apparent time at ship, by an altitude of any celestial body properly situated, by some of the methods already given; to which the equation of time being taken from the Nautical Almanac and properly applied, the result will be the mean time to be compared with that at the given meridian to

show the longitude of the ship.

The rate of a chronometer is readily obtained, by observing daily, if possible, the altitude of one or more celestial objects near the prime vertical, from which the mean time may be accurately determined, and, being compared with that shown by the chronometer, its gain or loss in 24 hours, and also its error on the day of the last observation, called the original error, will become known.*

Ex. 1.—Near Falmouth, in latitude 50° 8′ 48″ N., and longitude 20th 10 W., at about 18th 47th 20°, the following altitudes of the sun's lower limb were taken, with an artificial horizon, in order to ascertain the daily rate of a chronometer previously set to Greenwich time. The observations were made with a sextant of which the index error was + 1′ 30″, the barometer 29.6 inches, and the thermometer 56° Fahrenheit.

[•] These would be more accurately performed on shore by using an artificial horizon and the method of equal altitudes. In this case a pocket chronometer should be employed, to be compared with those on board, which ought to be as numerous as possible.

Times by: Chronometer.			44. j. i	alt.	190. 3	1
19° 10° 35° 12° 45 14 58 3 8 18 3 Messas 19 12 46 I. E.	38 4	3 45 30 15 30 30 30 18		ther bar. ther r 16 = 2 sun'	29.6 log 29.6 log 56° log 56° log 3″.4 443″.4 e paralla	9.99974 2.21282
Greenwich time Bally variation	٠.	-	7 8 17' 58	- 0	D. L. P. L.	0.09861 1.00080
Prop. part to 19 ^h 7½ ^m Dec. at noon, May 1st		15	14 19 8 49		P. L.	1.09941
Sun's reduced declination Observed alt. sun's l. l. Semidiameter Refraction Parallax	on	15	23 8	· ·	•	19° 3′ 0′ + 15 53 .3 - 2 48 .4 + 8 .1
True altitude					•	19 16 18
Sun's true dec. 15° 2° Latitude 50	3′8″: 8 4 8	N. N.	sec:		•	0.015850 0.1 93260
Difference 34 44 Zenith dist. 70 45		٠			•	
Sum . 105 2: Difference 35 5:						sine 9.900884 sine 9.489599
· · ·						19.599593
Mercon a -	24	36**	23.8 2		. si	ne 9.799796
Time from noon	5 24	12	47 .6			
Apparent time at Falm Equation of time	. 18	47 3	12 .4 10 .9			. •
Mean time at Falm. Time by chronemeter		44 12	1 .5 46 .0	1		i di j
Chronometer for Falm.	• •••	28	44 .5	far		(0)

106	YETAMINTRODUCTION. SHEEPE
limb taken with ing constant, w. 57" 56". This g	11th of May, 1824, the altitude of the sun's lower the same instruments as before, the index error beas 19° 9′ 50″, when the chronometer showed 18° ives the mean time at Falmouth 18° 30° 23°.5, and thronometer for the meridian of the place 27° 32°.5.
# Liner a Sout	1st, the error was 28 44.5 11th 27 32.5
The loss in ten of Or in one day it. Hence the daily	ays is an old to have each to abuilte 12 12 is is a set but some State is a set but do in 7 2 rate is a need but do in 7 2 erved, that the altitudes should be taken nearly at
the same time of the rate during t 1. On the 22d	the day, otherwise an allowance must be made for he interval. of May, 1824, in latitude 32° 36' N., and longitude by
account 16° 40′ 37° 24′, when the eye being 20′	W., the altitude of the sun's lower limb at sea was ne chronometer showed 5 12 24.5, the height of feet: required the longitude?
Time per. watch	7.2 On other the cases star Will Daily rate 24.5 12 16 10000 111 111 111 111 111 111 111 11
Original error !	28 44.5 Loss in 111 days {79.2 1.8
Loss in 11 days	me 4 45 1 21 m ship will de man ou 60 81 0
Alt. sun's l. l.	39° 26′ dec. 20° 26′ N. + 10 cor. for 5° + 20° 20′ N.
-True alt.	39 36 cor. dec. 20 28 N
with antibox, sum At	39° 36′ 69 32 cosecant . 0.028318 32 36 secant . 0.074455
Half Diff.	70 52 cosine 9.515566 31 16 sine 9.715186
o between the wind	100 and 100 an
the concerning of they	88 year to the constant logarithm 5.2(2)?, and half the clapsed time, the cosecant of arc first the 179 and alarance, the sine of arc second; 810 140 Et
Eq. of time	time in minutes, the logarithm of the in 04 v Euriting in seconds, the sum will be the logarithm of the control to the control of the control
Long. in time	1 7 23 = 16° 51' W.

For the usual computations at sea it is unnecessary to push the calculations farther than the nearest minute.

""Re-Ornthe Elth of Outober, 4834, as houn, on the meridian of Geography and the delly rate was 447-1914 fast, and the delly rate was 447-1914 fast, and the delly rate was 447-1915 on the Blat of October, at 6 42° 16' A. M. by the same chironometer, the observed altitude of the sun's lower limb was 427-17-20", and the height of the eye 20 feet; required the longitude?

1 . . . Ans. -33° 25' E.

હામ છત્વ હ જ સાંધાર્થ

3. On the 16th August, 1828, in latitude 38° 20' S., the mean of several altitudes of Antares west of the meridian was 14° 29', the height of the eye being 12 feet, and the mean of the times per watch 11^h 41^m 38° P. M., which had been compared with mean time at the Cape of Good Hope on the 22d of June, and was found to be 1, 10^m 28° too slow, and gaining 3°.54 a day; required the longitude of the ship?

Ans.—17° 36' E.

EQUATION TO EQUAL ALTITUDES.

In ordinary cases the error and rate of a chronometer may be determined by single altitudes; but when great accuracy is required equal altitudes are very superior, especially when a transit instrument cannot be obtained. On this account various tables have been computed to facilitate this operation, though it is believed few of them afford great advantage in actual practice. To those who would prefer such a table, that of D. Josef S. Cerquero, given in the thirteenth volume of the Journal of Science, is perhaps the most commedious and exact. By this means, however, tables would be multiplied to any extent without giving much advantage, on account of the inconvenience of taking proportional parts; and from this consideration it is often better to give an easy practical rule, sequiring the use of the ordinary tables, where neither double entries, different signs, nor proportional parts are necessary.

The equation of equal altitudes is a correction for the change of declination of the celestial body during the interval of observation, to be applied to the middle time between the instants shown by a chronometer, at which, on a given day, that body has equal altitudes; to find the true time by the chronometer when the object

was upon the meridian.

Rule.*

To the cosine of half the interval between the times of observation add the cotangent of the latitude, the sum, rejecting 10 in the index, will be the tangent of arc first, the difference between which,

Now to the constant logarithm 5.364517, add the cotangent of half the elapsed time, the cosecant of arc first, the cosecant of the qualar distance, the sine of arc second, the logarithm of the elapsed time in minutes, the logarithm of the daily variation of the declination in seconds, the sum will be the logarithm of the equation of equal altitudes in seconds of time, which, when applied to noon, is additive if the polar distance is increasing, and subtractive if it is decreasing.

See De Mackey's of Mr. Riddle's Navigation for a singler rule, analogous in principle, though perhaps in the detail somewhat less sample.

If the equation is applied to MIDNIGHT, it is additive if the polar distance is decreasing, and subtractive if the polar distance is increas-Now half the sum of any two times, answering to the same signi

Ex. 1.—On the 23d of March, 1809, at Pisa in latitude 43° 43' 11" N. equal altitudes of the planet Venus were taken before and after transit, the elapsed time between which was 8h 50m; required the equation of equal altitudes when her declination was 20° 42′ 40′ N. and her daily variation +20'5" or +1205" increasing, and consequently the polar distance decreasing?

Latitude H. E. T.	43° 43′ 4° 25°		5.364517 ot. 9.643463
Arc 1. Pol. dist.	22° 50′ 69 17	tan. 9.624494 cosecant	osec. 0.411110 0.029030
Arc 2. Elap time Daily var, dec.	46 27 8 ^h 50 ^m 20′ 5″	= 530 no loga .	. 9.860202 2.724276 3.080987
Eq. E. Alts -	_ 12:.99	30 10	1,113585

Or subtractive, because the polar distance is decreasing and is to be

applied to noon.

Ex. 2-On the afternoon of the 17th of September, 1810, altitudes of the sun were observed at Marseilles, in latitude 43° 17' 50" N. and equal altitudes were taken on the forenoon of the 18th, after an interval of 21^h 50^m, the sun's declination for the 17th at midnight being 2° 14′ 23″ N., and daily variation of declination — 23′ 14″ = —1394″; required the equation of equal altitudes?

Ans.—Equation of equal altitudes - 136.70.

Or subtractive, for the polar distance is increasing, and is to be ap-

plied to midnight.

Ex. 3.—At Florence, in latitude 43° 46' 40" N., on the 8th of April, 1809, equal altitudes of the planet Mars were taken at an interval of 8h 20m when his declination was 5° 9' 40" S., decreasing at the rate of 6' 38" daily; required the correction for the planet's superior passage? Polacities find the Ph

Ans.—Equation of equal altitudes — 5.196.

Or subtractive, because the polar distance is decreasing, and is to be applied to the superior transit. 4º 16 5 = 316° 15 log.

TO FIND THE ERROR OF A CHRONOMETER BY EQUAL ALTITUDES.

By the Sun.—The sun is in general the most convenient object for determining the error of a chronometer by equal altitudes, and the forenoon and afternoon of the same civil day are often preferred, though the evening and succeeding morning may sometimes be employed with advantage.

In the morning when the sun is more than two hours distant from the meridian, in mean latitudes, let a set of observations be taken with the corresponding times by a chronometer. In the afternoon Hence the chrusomoter was

Ea. 2.—On the 24th of July, at Pendennis castle near Falmouth,

By polar distance in the computation, is meant the distance of the object from the elevated pole, which may be either referred to the north or south pole, according to the name of the latitude.

observed the litetants when the concesses to the same altitude, write ingressib time down opposite its corresponding altitude.

Now half the sum of any two times, answering to the same altitude, will be the spproximate time of noon. Find the mean of all the times of noon in this manner from each corresponding pair of observations; to which the equation of equal altitudes being applied, the result will be the time of apparent noon, or the instant that the sum's centre is on the meridian by the chronometer. The difference between this and noon is the error of the chronometer, which will be fast or slow according as the time of noon thereby is greater or less than twelve hours.

Ex. 1.—On the 29th of January, 1826, in latitude 57° 9' N., the following equal altitudes of the sun were observed; required the er,

ror of the chronometer?

Altitudes.	Times A. M.	•	Times P. M.
	21 ^h 35 ^m 8 ^s		2º 55 • 43° · ·
8.10	36 8		54 42 1
11.11 8 115 · · · · · · · · · · · · · · · · · ·	37 9 ′		58 49 1
ao., 8, 20 .	3 8 9	• .	52 41
^{62,66} 8 . 25 .	39 10	•	51 40
ari e i - I			15.0
with piles	35 44		15 8p
Means.	21 37 8.8		2 58 41 6 to
open worlds	2 53 41.6		21 37 8.8
ent of a	-		11
Blapsed time .	5 16 32.8	Sum	
Н. Е. Т.	2 38 16.4	Half	12 15 25.2
San's declination at noon,	on merid. Green	wich	17° 59' 15" 8.
Daily variation or decreas			- 16 15 N.
	cot. 9.810025	C. L.	5.364517
H. E. T. 2º 38º	cos. 9.887406	cot.	0.083896
TE DETERMINE	·	٠٠.	
Arc 1. 26 29	tan. 9.697431	cosec	
Pol. dist. 107 59	cosecant	•	0.021753
Arc 2. 81 30	sine .		9.995203
El. time $4^h 16.5 =$			2.500374
Daily var. dec. 16' 15" = 9	975" log.	•	2.989005
			1.005.453
Eq. equal alts — 20.2	•	•	1.305471
Half sam of approximate	time of noon		12° 15° 25′.2
Esquation of equal altitude	: 8 .	,	- 20.2
Sand house be en-	to in the second		
Time of apparent noon by	chronometer	.•	12 15 5.0
Equation of time with cor	itrary sign	•	— 13 27.9
Time of mean mean by ch	ronomotor		10 1 97 1
Time of mean noon by ch Hence the chronometer	was 15m 5r fact t	for anno	12 1 37.1
37.1 fast for mean time.	Has IV V Idst I	or apparer	it moon, and 1-
Ex. 2.—On the 24th of	July at Penden	nie oostlo	near Ralmonth
in latitude 50° 8′ 48″ N.,	Dr Tierke with	h e sorton	t of ten inches
251 36 WILLIAM OV. U 30 M.,	WAW. COMMENT AND	H. G. BCAUM	r or next wirthes

Tadies by Mr Troughton, and an artificial horizon, together with a

chronometer by Morice, found the double altitude of the sun's up.
per limb to be 69° 47′ 20″, at 8h 29m 13 A. M., and 4h 25m 5.3 P. M.
required the time of apparent noon by the chronometer?*

Time after noon 23d per chronometer 308.9
Sum 87.0
Half sum, or approximate noon . 12 27 9.15
Difference, or elapsed time . 7 55 52.30
Half elapsed time about 1 a 1 57 56.15
The declination of the sun, at noon 24th, is 19° 58' nearly. Daily variation 12' 39" S., or increasing the polar distance.
Latitude 50° 9′ cot. 9.921503 C. L. 5.364517 H. E. T. 3 ^h 58 ^m cos. 9.705469 cot. 9.770148
Arc 1: 22° 57′ tan, 9.626972 cosec. r 0.409016 Pol. dist. 70 2 cosecant 0.026922
Arc 2. 47.5 sine 9.864716 Elap. time $7^h.56^m = 476^m \log$. 2.677607 Daily var. dec, $12'.39'' = 759'' \log$. 2.880242
Eq. eq. alts. + 9°.844 log
Apparent noon
midnight by the chronometer?
viament 24 to state out of monotonic and 21 49 59.7
Summer out to coming newig a to smit passer and more constraint of
Half sum, or approximate midnight 12 27 49.2
Elapsed time (1) 1 + 1 (1-1 + 18 44 21.0
Half elapsed time 9 22 10.5
Declination at midnight 19° 52' N., daily variation 12' 39" S. Or increasing the polar distance, and the equation is therefore nega-
tive for midnight.

See a Report on Chronometrical Observations to ascertain the longitude of the island of Madeira, by J. L. Tiarks, 1322.

Letitudes 150° 9' 1 bet. 9.99180811 bg. L. 1 50 01 01 01 01 01 01 01 01 01 01 01 01 01
Pol. dist. 70 8 cosecant cosec. (1.106B 7-0.26643)
Arc 2. 37 21 sine 9.782961 Elap. time 18 ^h 44 ^m = 1124 ^m log. 3.050766 Daily varia. dec. 12' 39" = 759" log. 3.050242
From approximate midnight 12 27 49.90 Subtract the equation of equal altitudes
Apparent midnight 19 27 20 66
Proceeding in this manner till a considerable number of observa- tions are made, the error of a chronometer may be determined with great accuracy. If this chronometer is compared with any given number of them, all their errors and rates may be found as has been
done by Dr Tiarks. The same thing may be done by the stars, though rather less con-
veniently. The following method of comparing a chronometer with hear
time by Dr Tiarks, communicated by Captain Basil Hall, R. W. will be found very useful.
The difference of a chronometer from the mean time et a plear being known at three different instants, to find that difference for any intermediate instant with a proper regard to the change of rate which may have taken place between the first and second, and be-
tween the second and third times.
there is a grant of the state o
t' = a + b
So that b is the difference between the first and second states of
the chronometer, and c the difference between the second and third states of the same chronometer, the state of a chronometer, (namely, its difference from the mean time of a given place), at the moment
$\frac{t}{s} \frac{dt}{dt} \frac{dt}{dt} \frac{dt}{dt} + \frac{t}{t} \frac{(t-t')}{t''(t''-t')} \right\} b + \frac{t}{t'} \frac{(t-t')}{t''} c; \text{ or } t = t$
$ \underbrace{b}_{t} \left\{ \frac{t}{t''} f(t'' + t' - t) \right\} b + \frac{t}{t''} \frac{(t - t')}{(t'' - t')} c = \text{correction} $
If Y is less than t' , $\frac{t}{t} \frac{(t-t'')}{t}$ is positive and $\frac{t}{t''} \frac{(t-t')}{t''}$ is negative, and
if his greater than thoth are positive.
Example.
The difference of a chronometer from the mean time of a certain
place was known on the following days:

Differences. Days.
August 94,5243 91 9002 Difference between let and 2d - 21 9002
4.5104 1 and 3 = 26.4007
Hence $o = 0.0$
t' = 21.8903
007000 t"= 26.4007 August 1 August 10 August 1
11 00 P+P= 48.2910 T000 L T01 1000 - 01 T001 1010 11
It is now required to find the state of the chronometer for August
17th, at 11h 7m 44' = 17d.4637. Deducting August 9d.5243 from
August 174.4637 we have the interval $t = 74.9394$. t' + t'' = 48.2910 $t' = 21.8903$ log. 1.340252
$t = 7.9394 \log. 0.899788$ $t' = 26.4007$ $\log. 1.421616$
DO DE LE GENTE L'ASSESSON LE RESELON LE L'ENVIRENT LE TOUR
$t'+t'-t = 40.3516 \log. 1.605861 t' \times t'', \log.$ 2.761868
$t \times (t'+t''-t)$, or num. log. 2.505649
t'xt" or denominator, log. 2.761868
65.0 (30,0070,0071) 7 (00,007) 7 (00,007) 7 (00,007)
$\frac{t}{t'\times t''}\times (t'+t''-t)$, log. 9.743781, or factor of b.
$t' \times t''$ = 7.9394, log. 0.899788 t'' = 26.4007 log. 1.421616
t' = 21.8903 $t' = 21.8903$
OE F BOLUDGONE UERSSINO, I TRECEISOF OF FE
t-t = 139509 log. 1.144602 $t''-t' = 4.5104$ log. 0.654215
numerator log. 2.044390 t" (t"-t") denom. log. 2.075831
denominator log. 2.075831
08 to 808 of 100 kess 3 ,000 cc10 ,005 0 ,075
$\frac{t(t-t')}{t(t')}$ log. 9.968559, or factor of c which is negative,
t''(t''-t') because t is less than t' .
art o con determ to many the tolerate Diff.
August 9th, 12 ^h 35 ^m chronometer slow 51 ^m 57 ^s .35
31st, 9 57
Sept. 4th, 22 12 54 39 .16 · · 28 .83 c
What is the difference, August 17th, 11^h 8 ^m . $b = 132^{\circ}.98$ log. 2.123782 c = $28^{\circ}.83$ log. 1.459845
b = 132.98 log. 2.123782 c $c = 28.83$ log. 1.459845 factor b log. 9.743781 factor c log. 9.968559
Table 1. contains the decimal fraction of a fig of 24" It is use
$(f) b = +73.72 \log 1.867563$ $(f) c = -2682 \log 1.428404$
and seconds are, and densequantly may be convenued as a many calculations where daily differences are very calculations where daily differences are very calculations.
cor. = + 46.90 to be applied to the error of the chronometer at
the time a. at I have be thereby pendily abuse of hours, de.
August 9th, 12 ^h 35 ^m chronometer slow for M. T. 51 ^m 57.35 correction + 46.90
Table 11. serves the same purposes when an hour is taken for
Chronometer slow for mean time monorate lapove of labor 52 144 .25
On August 17th, at 11 7 44.
bailers of alless line alder side 1000 or 501 has 500 as 401 con

For Rossel's method of correcting the error in rate of a chronometer, see Biot's Astronomie, vol. 111., or Myer's translation of this, page 95.

· 14 16 5

Dec	E Data Table	Day of 24.	Deci	Table II. imal Parts of an Hour.	To conv	pert Decimal into Degree to an Hour.	90	
T	Decimal.	T	. Decimal.	7	Decimal.	004	Arc."	1
116	0.1041667	10	h.006944	10"	1.166667	0.10	1".5	1.
	0. 083333		.013889		3333333		3.0	1.
	0. 125000		.020833		.500000		4.5	30
	0.166667		.027778		.666667		6.0	50
The second second	208333	633 PS 34	.034722		.833333		7.5	HID.
SETTING CO. C. S. S.	250000		.000694		.016667	1475, 189	9.0	d.,
(44 - 14 / 14 - 1 / 14 / 14 / 14 / 14 / 1	. 291667	2	.001389	2	.033333	C 80 10 10 1	10 .5	
Transfer of the second	. 333333	3	.002083	3	.050000		12.0	1
	. 375000	4	.002778	4	.066667		13 .5	-
	416667	5	.003472	5	.083333		0 .15	41.5
	458333	6	.004167	6	.100000		0 30	选
	. 500000	7	.004861	7	.116667		0 .45	30.
	. 541667	8	.005556	8	.133333	0.04	0 .60	
	. 583333	9	.006250	The second	150000		01.75)	be
15 0	625000			-	-	0.06	090	3 37
16 0	666667	10	.000116	10	.002778	0.07	1 .05	₩.
17 0	. 708333	20	.000232	20	.005556		I 20	1
118 0	750000 3	30	.000348		.008333	9.09	1 .35	16.7
119 0	791667	10	.000464	10	.0111110		0 .015	77
20 0	833333 5	10	.000580	0	.013889	0.002	0 .030	460
21 0	875000	1	.000012	1	.000278	.003	0 .045	619
	916667	2	.000023	2	.000556	.004	0 .060	LICEN
	958333	3	.000035	3	.000833	.005	0 .075	(his
24 1.	000060	4	.000046	4	.001111			Am
		5	.000058	5	.001389	.007	0 .105	-
	r 12h	6	.000069	6	.001667	800.	0 .120	MAG
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132	- ER	9	.000104	9	.002500	52	81 et. 9	

Explanation.

and the state of

Table I. contains the decimal fraction of a day of 24^h. It is useful for inding what part of a day any number of hours, minutes, and seconds are, and consequently may be conveniently employed in many calculations where daily differences are necessarily involved, such as the daily rate of a clock, the change of which, in any given number of hours, &c. may be thereby readily obtained. It is also very useful in the preceding method of comparing chronosacters, and other a pulposes.

Table II. serves the same purpose when an hour is taken for unit, and is useful in several astronomical operations well 12 languages.

Table III. is supplementary to the general Table V, which garrent to convert time into degrees if less than 6° or 90°. But as 6° answers to 90°, 19° to 180° and 18° to 270°, this table will easily be applied to 24° or 360°, the whole sarding of supplied to 24° or 360°.

Under (1) and

by the proportional parts at the bottom to every single second. Whence it is only necessary to convert the decimal part of the time into degrees by this table to complete the whole. plement to 24 will be the hour

III. BY OCCULTATIONS AND ECLIPSES.

The moon in her periodical revolution frequently passes between the earth and a fixed star, of which she intercepts the spectator's

view, thus, producing what is called an occultation.

Since the instant of disappearance and reappearance of the star can be ascertained without the use of any instrument liable to error, the longitude may be determined more accurately by an observation of this phenomenon, than by a lunar distance. An observer possessed of an ordinary telescope, a chronometer, and an instrument to determine its error and rate,* can readily make the observations; and the necessary calculations are far from difficult. Several rules have been proposed for this purpose independent of the method of determining the parallaxes by the nonagesimal, and comparatively much more simple. Of these, Dr Inman's of Portsmouth, which we shall in the mean time adopt with some alterations, appears to us the most convenient.

At the instant of the disappearance or reappearance of the star, the apparent right ascension and declination of the point of the moon's limb in contact with the star is the same as the right ascension and declination of the star, which can be obtained with great facility and accuracy from tables. The apparent right ascension and declination of this point being corrected for parallax, its true right ascension and declination will be determined. Now since the distance of this point from the moon's centre, which is equal to her semidiameter, and the declination of the centre for the estimated A time at Greenwich, may be found by the Nautical Almanac, the true right ascension of the moon's centre is easily computed. Should there be an uncertainty in the estimated Greenwich time amounting to about one minute, the operation must be repeated, till the estimated and computed Greenwich time be very nearly the same.

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By applying the estimated longitude in time to the observer's apparent time, the reduced Greenwich time to the nearest minute will be obtained.

To this time take from the Nautical Almanac the sun's R. A., the moon's R. A. and their declinations corrected for second differences, repeating the operation when supposed necessary; and the moon's semidiameter, and the horizontal parallax corrected for the spheroidal figure of the earth.

Take also the moon's R. A. for 3h after the first estimated time corrected as formerly.

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Find from the Nautical Almanac, or from other tables, the apparent R. A. and D. of the observed fixed star; and reduce the given latitude for the spheroidal figure of the earth.

of the first difference subtract that If the observations are made at sea, an allowance must be made for the rate of the chronometer between the disappearance and reappearance of the star and the run of the ship, as in lunars.

To the apparent time add the sun's R. A., and from the sun, increased if necessary by 24, subtract the star's R. A.; the remainder, if less than 12, will be the hour angle; if greater than 12, its com-

plement to 24h will be the hour angle.

Now write down the proportional logarithm of the reduced horizontal parallax under the numbers (1), (2), and (3). Under (1) and (2) put the secant of the reduced latitude; under (3) the cosecant of the same; under (1) the cosecant of the hour angle (a), and take the sum of these.

Below the sum of the three logarithms under (1) put the constant logarithm 1.17609, and the cosine of the star's declination; at the same time under (2) put the cosecant, and under (3) the secant of the same; the sum of these three logarithms under (1) will be the proportional logarithm of arc first, or the parallax in R. A. in time, nearly; one half of which (b) is to be subtracted from the hour an-

gle (a), giving (a-b), the corrected hour angle.

Under (2) put the secant of the hour-angle thus corrected. The sum of the logarithms under (3) will be the proportional logarithm of the first part of the parallax in declination, and that under (2) the second. The first part must be applied with such a sign as to diminish the star's distance from the elevated pole: the second must be applied with the same sign as the first, if the hour-angle and polar distance are the one greater, and the other less than 90° or 6°; otherwise with a contrary sign. The result will the true declination of the observed point of the moon's limb. Take the difference between this true declination of the observed point and the declination of the moon's centre, found from the Nautical Almanac, under which put the moon's horizontal semidiameter properly corrected; and take the sum and difference. Add together the proportional logarithm of this sum and difference, and take half the sum, to which add the cosine of the mean of the two declinations just found, the sum will be the proportional logarithm of the moon's semidiameter in R. A. nearly.

Under (4) put the constant logarithm 1.17609, the first sum under (1), and the cosine of the declination of the observed point, the sum will be the proportional logarithm of the exact parallax of R. A. in time. This being added to the star's R. A. when west of the meridian, but subtracted if east, will give the true R. A. of the point observed. To the true R. A. thus obtained add the moon's semidiameter in R. A., or subtract it therefrom, according as the reappearance or disappearance of the star has been observed, and the result will be the true R. A. of the moon's centre deduced from observa-

tion.

If this differs considerably from the R. A. taken from the Nautical Almanac, after the moon's declination by as many seconds as will make a corresponding variation in the first R. A. such as the Nautical Almanac would give for the same alteration in declination. Repeat the operation till this is the case, and the last R. A. will be that

required.

Under this put the moon's (1) R. A. taken from the Nautical Almanac for the Greenwich time, and then the moon's R. A. three hours after, or the (2) R. A. Take the difference between the first and second, and the difference between the second and third. Then from the proportional logarithm of the first difference subtract that of the second, the remainder will be the proportional logarithm of a

portion of time which must be added to the Greenwich time when the first R. A. is greater than the second; otherwise subtracted; and the result will be the Greenwich apparent time. The difference between this and the apparent time of the observer will be the longitude in time.

Ex. 1.—On the 3d of March 1823, at Bahia, in latitude 12° 57′ 17″ S., and longitude by estimation 38° 30′ W., the reappearance of Antares from the dark limb of the moon was observed at 15^h 30^m

0°.3; Required the true longitude?

Bahia, March 3d	l, 15 ^h 30 ^m 0 ^s .3	Moon's 1st R.A. 244	° 27′ 29″.75
Lon. in time	2 34	2d R.A. 246	6 16 .82
No 1 00 192	Total Control of	Dec. 25	55 15 .6 S.
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	15h 30 0.3	A TOTAL MAN TO ST	
Sun's R.A.	22 56 58.64	latitude	12° 57′ 17″ S.
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Antares R.A.	16 18 35.82	red. lat.	12 52 17
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******	22 8 23.12		And the second
	24	The state of the state of the	Mary Street
St. Com. C	Forh Pogroo	D (2)	Fa.

As it is convenient that the work should follow from beginning to end in regular order, that of the foregoing example has been transferred to the two following pages, and to avoid unnecessary waste of room, the remainder of this has been filled with the follow-

ing example for exercise :-

Ex. 3.—On the 26th of May, 1822, at San Blas in latitude 21° 32′ 25″ N., and longitude by estimation 105½° W., at 9° 22° 41°3, A.T. the immersion of a Leonis was observed by Lieutenant H. Foster, then Master's Mate of his Majesty's ship Conway; what was the true longitude?

Choose and the same of the sam

Ans.-105° 18′ 27" W.

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Moon's T. dec. 25° 52' 6".3

Ex. 2.—On the 54' 10" S., and λ Sagittarii beh 9'.2; What was	estif ind:	hate the	d lo mé	oa ngi	tudé s dar	13 *718	∀W;table o	diap	pěři	mnd	i de
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27411	24								•		
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It is hardly necessary to give the variation of the sun's R. A. and D. in 10, as it is very small, and as the true time must differ but a few seconds from the estimated, on repetition the longitude cannot vary much on this account.

Ex. 4.—On the 3d of January, 1825, at Port Bowen, in latitude 73° 13′ 40″ N., and longitude by estimation 5° 56° W, the immersion of z Geminorum of the 4th magnitude was observed at 6° 14° 23°.26 M. T., and the emersion at 7° 11° 12°.17 M. T., by Lieutenant Henry Foster, R. N.; what was the true longitude?

Ans.—By immersion the longitude is 5^h 55^m 48, and by emersion it is 5^h 55^m 35 W.

It was intended, if room would have permitted, to put the whole of the calculation on one page, and, though not done here; may readily enough be so placed by the calculator. This little attention ought not to be slighted, as a neat form, like a convenient formula, will be found of some service in accurate computations.

1.17600	0.000000000000000000000000000000000000	9.663	1.78864
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am's right ascension and declination, as if for some point on the moon extended, process, and assurous MA vatting the min of the

An eclipse of the sun depends upon the same cause as an occultation, his light being intercepted by the body of the moon passing between him and the spectator. The beginning and end of a solar eclipse is easily observed by a telescope of moderate power properly prepared, when the point of contact of the limbs being nearly known, and the rule for computing the longitude is similar to that now given for an occultation. If the semidiameter of the moon passing through that point of the sun and moon, apparently in contact, be supposed to be produced to the centre of the sun, as seen from the observer, and conceiving this centre to be at the distance of the fixed stars, so as to have no sensible parallax, then it is manifest, that the rule for an occultation must apply by substituting for the moon's semidiameter the sum of the sun and moon's semidiameters, considering the sun to be at the same distance as the moon when seen from the earth's centre,-that is, subtracting the augmentation for the sun's semidiameter as if it were the moon's from it, as found in the Nautical Almanac. In the supposition just made, the sun's centre was supposed to have no parallax; but, as it has a horizontal parallax of about 8".7, in finding the apparent place we cannot proceed exactly as for a fixed star. The sun's right ascension and declination, as seen from the centre, must be taken from the Nautical Almanac, which, corrected for parallax, will give the apparent right ascension and declination, thus reducing the case of a solar eclipse to a similarity with that of an occultation. The apparent right ascension and declination of the sun's centre must now be corrected, using the horizontal parallax of the moon in the computation. This would evidently give the same true place as if, taking the right ascension and declination of the sun's centre from the Nautical Almanac, we considered these elements as apparent, and corrected them for parallax, instead of the moon's horizontal parallax employing the difference between the horizontal parallaxes of the sun and moon.

Whence the true right ascension of the point answering to the sun's centre is obtained, and consequently, as formerly, the true right ascension of the moon's centre, from which the Greenwich apparent time is determined. The apparent time of the observer is found by means of a chronometer, whose error and rate have been determined by double altitudes if possible, if not, by altitudes both to the east and west of the meridian.

Rule.

By applying the estimated longitude in time to the observer's apparent time expressed astronomically, the Greenwich time will be obtained to the nearest minute. For this time take from the Nautical Almanac the sun's right ascension and declination, the sun's semidiameter diminished by the augmentation, the moon's right ascension and declination, semidiameter and horizontal parallax corrected for the spheroidal figure of the earth, and diminished by the sun's horizontal parallax. Take also the moon's R. A. for 3 hours after the first R. A., or estimated Greenwich time.

Find the hour angle, which, in the afternoon, is the observer's apparent time, and in the morning its complement to 24 hours.

Employing the moon's diminished horizontal parallax, correct the

sun's right ascension and declination, as if for some point on the moon extended, proceeding as formerly, only putting the sum of the sun's semidiameter, diminished by augmentation and the moon's semidiameter, instead of the moon's semidiameter alone: If the resulting Greenwich time differ from the estimated, the sun's R. A. and declination must be corrected for the difference, repeating the operation as often as necessary, till the Greenwich time by computation and setting the computation and the moon's semidiameter alone.

tation and estimation agree.

Ex.—On the 7th of September, 1820, at the Royal Naval College,
Portsmouth, in latitude 50° 48′ 3′ N., and longitude by estimation
1° W., the end of a solar eclipse was observed at 3° 12° 55°; required the true longitude?

	oon's (1) R. var. in 10°	A.	166	54′	47"		
Lon. in time 4	(2) R. A		168	13		. 4	
Est. G. T. 3 7 To this time.	dec. var. in 10°		•	21	4	.84	N.
Sun's R. A. 11h 4m 13.60	hor. S. D.				42	.7	:
Var. in 10 0.025 Dec. 5 58 22' N. Var. in 10 0.16	equa. par. red. to lat.	•		53 —	56 ·· 6		•
Var. in 10 0.16 Semidia. 15 54 . 8 Hor. par. 8 . 6 Alt. 30° nearly		•	•	53	40		
App. time $3^h 12^m 55^o = H.A.$	difference latitude . Reduction	•		53 48 11		.1	N.
A property of the second of th	Red. lat. Sun's S. D. Aug. to 30°	•	50	15	48 54 7	8.	
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(3) P. L. 0.52543 cope. 0.11188	secant 0.00236	P. L. 0.63967							O' 1" 42.2	sun's R. A. 11 4 13.64	11 6 55.84=	are. (5)	red. B. A.
(2) 0.52643 P. 0.19751 ©	8.98273 sea		. •		٠	0.17643	2 22" S. P.L. 1.88030	l. coeine		sun's R. A.	· •.	P. L. 0.58596	P: L. L09994
9 P. L.	5° 58′ 22″ cosec.	1.17609 (2) 41" 16' N.	6°39 38 N.	مم ر		•	% 82″ B.	c. 6º 37 16 N.)'s dec. 6 21 4 N.	16 12	90 90 90	46 42	14 18
(1) 0.5254 0.19751	COSEC. 0.12737 P. L. 0.85061	C. L. 1.17609	cos. 9.99763	P. L. 2.02403		secant .		T. dec.)'s dec	Diff.		Sum	diff.
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Diff. of par. Red. lat.	Hour angle Sum		Sun's dec.	Arc 1.	Half .	Diff.			Sun's S. D.	Moon's S. D.	Sum		True dec.

				SPH	erio		LHIG	onom	ETRY.				
166 54 47	106 13426	100	1 18;39	9 0 0 85.	3 17 36	3 12 55	10 7, 30,	108° 54' 47"	+ 11	5	* R		
lst R. A. 166 54 47	2d-R. A.	P. L.	P.L.	P. L. to est. time	G. T.	app. T.	log. in time		var. in 25°			,	
		2.99203 P. L.	0.35947	2.63246	•			P. L. 3.55630 P. L. 9.35657	P. L. 3.19078		i i	11. \$ \$ W.	
1.68680	C 0.84290	9.0979R	L 0.84011	166° 28′ 5 8″	25 57	166 54 55	(1)R.A.cor. 166 54 58	1 18 30	3-17-25	3 17 18	3 12 55	4 83	
uns	half	•	26′ 0′ P. L.	on R. A.	arc (5)		(1)R.A.cor	diff.	est. T.	G. T.	Ap. T.	lon, in T.	
		cosine	Arc (5)	Repetition					0.58518 1.10247	1.68765	0.84382	9.99721	8.84183
									P. L. P. L.	Sum	Half	008	P. L.
6 21 4	12 58 20	6 29 10		6° 21′ 4″	ic	6 20 59	6 37 16		46 47 14 13			6° 29′ 10′	25 57 .4
Moon's dec.	Suns		-	Moon's dec.	Var. in 25	Cor. dec.)	True dec.	Diff. Sum S. D.	Sum Diff.			Half sum	Arc (6)

21	120				A H I		PRICK	TAN	няя	Hdb			
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A 31 (C)	Appr Or Sun's Var.	To Fo in 10	this	time 7-6	18 ₋ 18 ₋ 2.5	0 43 l nearly	nout .	angl on's (. A. . A.			1 5.4 2 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7
0.97577	Ang Cor. Hor. Latit	in 10 8. I 8. 2 8. D par.	r, D. Ogalt	<u> </u>	15	6 .05 45".5 5 .5 40 .0 8 .5 32" 40	- <u>-</u>		var. 1 dec. var. i S. D. equat red. 1 red. 1 sun's	in 10 t. par to 56	r.	_ 10	55 57 1 3 3 43 5 5 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6
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`::: `) (200 16	and Termo		## \	A second	A S			· tisH	Are J	Si x max		Diff. p.u. 18cl. lst Hour angle

	lo 1' 4"	P. L. 0.46947	P. J. 9	0.46947	P.L. 0	0.46947 C. L. 0.68264	(4) 1.17609
ned. lat. Hour angle	00 40 02 6 8 54.6 (a)	secant cosec.		8 8 3 4154	1	86 700	n sellen Ind in Abo
		P. L. 0.71960 C. L. 1.17609	•	3. 1. 3.	. P. I.	58870	10.20 to 10.00 to 10.
Sun's dec.	99° 35′ 40″	cosine 9.96532	32 23 22 17		; !		ira Pa
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٠	6^{h} 7 40.2 (a - b) secant	-b) secant		1.47491		olie i olio nio	D (4)
	•		(3) 264	264 P. L. 2.60962	. 1	• (14). • • • • • • • • • • • • • • • • • • •	
	•	T. dec.	23 22 434	cosine	a.		9.96279
San's B. D.	15' 40"	moon's dec.	23 48 554	arc (4)	I	2- 29.6 P. L.	1.8\$646
Moon's S. D.	16 43	diff.	26 12	e,un,e	sun's R. A. 7 6	9.6	
Sum .	32 23		32 23		7 8	33.0 = 106	106° 53′ 16″.0
		Sum	58 35	P. L. 0.48750	arc (5)	: 	+ 20 46:0
Sun's T. dec.	23° 22′ 44″	diff.	6 11	P. L. 1,46405	ŧi.	T. R. A. DO	106 14 1:0
Moon's	23 48 56		se th	991961	Swee (1) R.A.	R.A. 196	40 40 40 40 40 40 40 40 40 40 40 40 40 4
Sum .	47 11 40		half	0.97577	8	(2) R. A. 108	16 16 .4

Half

2° 26' 45"

Bun's dec.

Cor. dec.

Cor. dec.

IV. BY THE MOON'S TRANSIT.

The method of finding the longitude by the culmination of the moon and stars, is now considered very convenient and accurate.

Since the observations require a transit instrument, and the clock used with it generally shows siderial time; the difference of the times is supposed to be siderial time. If it is not, it must be reduced to siderial time by Table XXXI. If the moon had no motion, the difference of times between her transit and that of a fixed star would be the same at both places.

The difference of the differences arises from, and is equal to the increase (I) of the moon's right ascension in time, in the interval

between the passages over the meridian at each place.

Hence, if the increase (N) of the moon's R. A. in one hour of siderial time be known N: I:: 1h: X, the angle described by the western meridian in the interval of the passages of the moon.

This is equal to the difference of longitude + I.

Hence, the difference of longitude is equal to $X-I = \frac{I}{N}-I$. By the Nautical Almanac the moon's right ascension is given at every noon and midnight; whence its increase in an hour of siderial time may be found nearly in the middle of the interval including the observations.

Assume the difference of longitude $= \mathbf{L}'$ as nearly as can be estimated, and compute the increase (E) of the moon's R. A. in the siderial time L', then

As
$$E: I:: L': X = \frac{IL'}{E}$$
, (1) and the exact difference of longitude

 $=\frac{IL'}{E}$ I (2). But this exactness is only necessary when the places differ considerably in longitude.

The moon's limb is observed by a transit instrument, and not the centre, which makes some little difference when the difference of

longitude is considerable.

When great accuracy is required, it would then be necessary to make an allowance for the moon's alteration of distance, that changes her apparent diameter, and also for change of declination, which changes her semidiameter in R. A.*

Ex.—June 13th, 1791, the following observations of the passage of the moon and a Serpentis were made at the observatories of Green-

wich and Dublin; required their difference of Longitude?

At Greenwich, R. A.)'s 1st limb 15h 5m 3,52 at 9h 36m App. T. 15 33 34.70 R. A. a serpentis

1st Difference 28 31.18 At Dublin 15h 6m 12°.49 R. A.)'s 1st limb « serpentis 15 33 36.91 2d Difference -27 24.42

^{*} For a more complets solution of this method, see Ds. Brinkley's Article in the first number of the Dublin Philosophical Journal, and Mr Baily's Memoir in the Transactions of the Astronomical Society.

These wires, gr24:42 of 27 and Difference un ni a 27 24:42 g early sent Daily rate of clock-16.88 prop. part | + 1.00.32 mont in a bings ing also a hordrontal wire bissetting them, near up upon which the

2d cor. diff. 27 24.74 more of a stranger

chiw selienion Difference of 1st and 2d differences 1 6.44 = 16'36'.6.

tength.

As the places do not differ much in longitude, it is unnecessary to reduce apparent to mean time.

This difference 16' 36".6 is the increase of the moon's R. A., in the interval of its passages of the meridians of the observations of

Greenwich and Dublin.

By the Nautical Almanac, we find the following differences of the right ascensions of the same limb of the moon, and the star at about

differences are sufficiently uniform, the mean first difference containing the interval will be sufficiently accurate for the rate of increase in 12 hours at the middle time.

Hence, by formula (1) 7° 37'.5:16' 36".6::12h: x = 1568.42,

and when the difference of longitude is not considerable $x + \frac{x}{6 \times 60} =$

 $1568^{\circ}.42 + \frac{1568^{\circ}.42}{6 \times 60} = 26^{\circ} 12^{\circ}.77$, consequently $26^{\circ} 12^{\circ}.77 - 1^{\circ} 6^{\circ}.44$ = 25° 6°.33 = 6° 16′ 35″ W.

If dr be the increase of the moon's R. A. during the interval between the transits, then $x + \frac{x}{365} - 3r$ must be used when the dif-

ference of longitude is considerable.

It would extend this article too much to give Baily's or Brinkley's methods, which are more accurate and complete, and can only be

fully treated in a work on astronomy.

In the foregoing example the difference of R. A. between the moon and star was determined at both places by observation, but for ordinary purposes that at Greenwich may be found by the Nau-tical Almanac. tical Almanac.

OF THE TRANSIT INSTRUMENT.

A transit instrument is a telescope properly placed in the meridian for the purpose of observing the times at which the celestial bodies pass this circle. If the clock or chronometer by which the time is marked be adjusted to show siderial time, then their right ascensions will be found. This is perhaps the best method of determining the rates of chronometers.

The telescope is fitted to an axis, of which the ends tapered into points turn in notches, from their shape called Vs or Ys. This axis is made hollow, opposite one of the ends of which is placed a lamp

for illuminating the wires in night observations. In dring place and me

These wires, generally five in number, are placed in the telescope equidistant from each other, and perpendicular to the horizon, having also a horizontal wire bisecting them, near or upon which the transits are observed.

When properly adjusted, the middle vertical wire coincides with the meridian, and the instant that the centre of any heavenly body passes this wire, is called its transit. The other parallel wires are intended to correct or verify the observation by taking a mean between the transits over the first and last, the SECOND and FOURTH, and comparing it with the third or meridian wire; or, what is more correct, a mean of the whole called the reduction of the wires.

There are five principal adjustments necessary in placing a transit instrument, three relative to the telescope and two to the axis.

1. The wires should be set perfectly vertical.—This is verified by observing that any distant object cut by a wire does not change its position relative to that wire, on moving the instrument up and down. If it does, the wires must be all turned till the object is kept upon them, when moved through their whole extent, and the

adjustment is then complete.

2. The telescope should have no parallax.—When any distant object is bisected by the horizontal wire, if, on moving the eye up and down a little, the object should appear to separate from the wire, the instrument is said to have a parallax. This must be corrected by placing the object and eye glasses at such a distance from each other, that their foci may meet in the point of intersection of the wires. When the object-glass has been properly fixed by the instrument-maker, the observer has only to adjust the eye-glass.

3. The line of collimation should be correct.*—This is known by bisecting any object by the meridian wire, and if, on reversing the axis, the object still remains bisected as before, the line of collimation is correct. If not, it must be adjusted by means of the small screws in the sides of the telescope. This is effected by easing the one screw and tightening the other till the error appears one half diminished, when the axis is again reversed, and the operation is repeated till the adjustment is properly effected.

4. To level the axis.—This is performed by means of a screw placed under one of the Ys or notches, which raises or depresses that end of the axis at pleasure, while the true horizontal position is

ascertained by a spirit-level.

5. To bring the telescope to the meridian.—This is accomplished by means of a horizontal screw acting on one end of the axis, by which it is moved backward or forward till its proper position is obtained.

As the problem of bringing a transit instrument into the meridian is one of considerable difficulty, it is proposed to treat it at some length.

To take a Transit.

With the latitude of the place and the declination of the object of the its meridian altitude.

When it is known to approach the meridian, elevate the telescope

The line of collimation is an imaginary straight line supposed to join the centre of the supposed to join the centre of the supposed to join the centre of the meridian and horizontal wire in the centre of the telescopes.

to the given altitude by the circle attached to the end of the axis. Now, because the telescope inverts objects, the object will appear to come into the field of view from the west and move towards the east little hear the prime vertical, or still better by equal altitles

Mark the time of transit over each wire, using a dark glass to save the eye when the sun is observed.

FROM THE GREENWICH OBSERVATIONS.

1816.	of the state	aloi li	Wires.	lesimals	rontelbime	Reduc.	Star.
Nov.	1.	II.	III	IV.	v.	Wires.	L mon
3d	1.4 22.6		21 ^h 55 ^m 38 ^s .5 0 29 27 .5				Aquarii. Cassiop.
4th	0.4	18.4	21 55 37.2	55 .7	14.1	37.16	a Aquarii.
8th		51 ^m 48.5 53 4.3	14 ^b 52 ^m 7 ^s .6 14 54 23.4		425 CHARLES 199	13U111UU-	Sun's 1 L. Sun's 2 L.

The state of the s	NA THURSDAY CHEEN
Account By taking the means as directed.	15.1003
That of the 3d will be	21h 55m 38:30
4th	0 29 27.16
8th, both limbs	14 53 15 50
By the Nautical Almanac the sun's	14 54 4.70
right ascension that day was	(militaria militaria)
The error of the clock on the 9th is along on	mated commit
The error of the clock on the 8th is slow, or Suppose the observation had been made with	49.20
middle one only, then	one wite, as the
To	14h 52m 7.6
Add semidiameter, Table XV.	+ 1 7.6
mer experied that of approach within other wires be-	14 60 15 0
Transit of centre	14 53 15.2
Mean of the whole	adr to one 10.0
Difference only	0.2
Difference only The error of the clock may readily be determined	from the stars,
if one of those whose true places are given in the Na	utical Almanacis
observed. Otherwise the corrections must be app	
priate tables. Observed transit on 3d	218 55# 38 30
Observed transit on 3d Aquarii R. A. by tables	21 56 24.35
a clock by corulated to sideral care, and when it	de del medde
Error of clock by the star slow, on the od	40.05
	- 491 20
Loss in 4.71 siderial days	arw.hemmeras
Or the daily loss is bree crosed an exactly theme	voit mes abeo 67
ontedly observing Polaric, and correcting in this may	
several ways. One of the most general methods is by	of Position and
-One leaves are west as becomes in his assistants assistant	D. Podition M.

the every the start the sentires of attent of circumpular stars are equal sup-

' '' TO ERING A TRANSIT INSTRUMENT INTO THE MERIDIAN.

To perform this problem, the time should be accurately determined by an altitude near the prime vertical, or still better by equal altitudes as already explained. Bring the telescope to any celestial object when nearly passing the meridian, and, by turning the horizontal screw, make the middle wire bisect the object at the instant of its transit, then is the instrument in the meridian.

Should the object be the sun, as it cannot be accurately bisected, either limb must be observed when on the meridian by allowing for the time his semidiameter takes to pass the meridian. This is found most accurately in the Nautical Almanac, or, if it is not at hand,

from Table XV.

たいはくようおうけい

To find the Time that any Star takes to pass from one wire to another in a Transit Instrument, that of the Equinoctial being known.

Rule.—To the cosine of the star's declination add the proportional logarithm of the time at the equinoctial, the sum is the proportional

logarithm of the time by the given star.

Ex.—On the 10th of April, 1826, by a transit telescope which gave 25.4 for the passage of a star on the equinoctial from wire to wire; what would be the time by Antares, having 26° 2° 8. declination?

Declination Time	•	26° 2′ 25°.4	cosine P. L.		9.9535 4 2.62867
				:	
Reduced time		28.26	P. L.	•	2.58221

Or this would be more readily performed by considering the seconds minutes, and converting the decimals into thirds to be estimated seconds, then the answer will come out in minutes and seconds to be estimated seconds and thirds.

Declination	. 26° 2′	cosine	•	9.9535 4
Time	25°. 4, or 25 ^m 24°	P. L.		0.85044
•	28.27, or 28 16	P. L.	•	0.80398

Hence the star's expected time of approach to the other wires becomes known after its contact with the first is observed.

One of the most convenient methods of fixing the transit telescope in the meridian in mean northern latitudes is by means of Polaris.

It is required to set a transit instrument by Polaris, on the 1st of March, 1826, at Edinburgh, in latitude 55° 57′ 21″ N. By a reference to the Nautical Almanac its altitude at its superior transit will be 57° 34′, and at its inferior 54° 21′; and its R. A. is 0° 58° 12°.20. It must therefore pass the meridian about 2° 8°, and 14° 8° at the altitudes stated above, which serve as a guide to advertise the observer to be prepared.

Now let the clock be regulated to siderial time, and when it shows 0° 58° 12.2 make the middle wire bisect Polaris, then will the instrument be in the meridian. If, however, the time first assumed was not known with sufficient accuracy, the error of the clock can now be found very nearly by the transit of the sun or a star. By repeatedly observing Polaris, and correcting in this manner, the instrument will at last be truly in the meridian. This may be verified in several ways. One of the most general methods is by observing that the semirevolutions of circumpolar stars are equal, sup-

posing that the rate of the clock is uniform. Should the observer not choose to trust to that, he may select two circumpolar stars whose right ascensions differ nearly 12°, as it requires in this case only a few minutes perfect regularity in the clock. Take the difference between the transits of circumpolar stars by the clock, which are nearly in the same azimuth, the one above the other below the pole; repeat the operation 12 hours after successively, when the stars have reversed their positions, and if there be a variation in their differences, it shows a deviation in the instrument, which may be corrected by substituting half the difference for the error, and repeating the trial by approximation till the adjustment is complete.

If some of those stars whose apparent places are given in the Nautical Almanac be selected, the operation will be comparatively easy. These in pairs are; 1, & Cassiopeiæ and & Ursæ Majoris; 2, Polaris and & Ursæ Majoris; 3, Polaris or & Arietis and & Draconis; 4, Capella and & Herculis; 5, & Tauri and & Draconis; 6, & Aurigæ and & Draconis; 7, Pollux and & Aquilæ. No doubt some of these can only be so observed in very high northern latitudes; and, therefore, recourse must be had in some instances to other tables, such

as those of Dr Pearson.*

It sometimes happens that an observer has not a command of the whole meridian, especially if he has not an observatory properly adapted to the purpose, yet may find it necessary to take transits for the regulations of clocks or chronometers. In this case recourse must be had to the sun, and to pairs of high and low stars having nearly the same right ascension. Having, by the sun and a good watch or chronometer, placed the instrument nearly in the meridian, observe the transits of two stars having nearly the same right ascension, but differing at least 30° or 40° of declination. Now if the interval between their passing the meridian in siderial time be exactly equal to their difference of right ascension, the instrument is truly placed; if not, it wants correction.

If, when the latitude is N. and the stars S. of the zenith, the highest star come first to the meridian and the interval between the transits be too great, it deviates towards the west; if too small, towards

the east.

But if the lowest star come first to the meridian, and the interval between the transit be too great, it deviates towards the east; if too small, towards the west. In either case there is required a correc-

tion, which may be computed in the following manner:-

Rule.—To the secant of the star's declination add the sine of the difference of the latitude and declination, if they are of the same name, or the sine of their sum, if they are of different names; of the sum of which find the natural numbers. To the logarithm of the sum of these add the arithmetical complement of the logarithm of their difference, and the logarithm of the difference between the excess of the right ascension of one star above that of the other, and the observed interval of time between the transits, the sum will be the logarithm of an arc in time.

Half the sum of the excess of the right ascension of the one star above the other and the foregoing arc, will be the deviation at the

^{*} Perhaps the catalogue in the Nautical Almanac might be extended and the selection more judicious. For example, the places of some of the smaller stars in Orion might be properly exchanged for either circumpolar or high and low stars.

lowest star, and half the difference between these will be the devia-

tion at the highest.

The deviation in time at each star being now known, the instrument may be easily rectified by either, or both of them on the following night, or still more readily by a third star on the same evening; or, if the telescope is sufficiently powerful to show sters in the day, all the corrections may be performed at any time in a few successive hours. For the deviation of one star being known, that

at another may be computed by the following-

Rule.—To the logarithm of the given deviation add the cosine of the corresponding star's declination, the secant of the declination of the third star, the cosecant of the sum of the latitude and declination of the first star if they are of different names, or of their difference if they are of the same name, and the sine of the sum of the latitude and declination of the third star if they are of different names, or of their difference if they are of the same name; the sum of these will be the logarithm of the deviation in seconds of time at the third star.

Ex.—On the 1st of March, 1826, at the observatory of Edinburgh, in latitude 55° 57' 21" N., I observed the transits of Capella and Rigel, on the same evening, about a quarter past 6, and found the interval between the two transits 2.5 less than the difference between their true apparent right ascensions, as given in the Nautical Almariac; required the deviation of the instrument at either star, and also at a third, as Sirius?

55° 57' N. 55° 57' N. Latitude Dec. of Capella 45 48 N. sec. 0.156664 Rig. 8 25 S. sec. 0.004703

sin. 9.246069 sum 64 22 sin. 9.955005 10 Difference

1. Nat. number 0.2528 2. Nat. number 0.9114 9.402733

1.1642 log. 0.065953 0.6586 ar. co. 1.181478 Difference Diff. of R. A. and \2.5 log. 0.397940 Obs. interval

Arc in time

4.42 log. 1.645346

Sum

6.92 half = 3.46 = the deviation at Rigel.

Difference

1.92 half = 0.96 = the deviation at Capella.

Now since the highest star comes first to the meridian, and the interval between the transits is too short, the deviations are casterly. If the stars had been between the zenith and the north pole, the

deviations would have been westerly.

Since it has been found necessary to fix the instrument as soon as possible, we shall proceed to compute the deviation at the third star, which can be easily done, as we have an hour and three quarters nearly to perform the calculations and complete the arrangements; thus:

Declination of Rigel (a)	8° 25′ S. 55 57 N.	cosine orque ton	9.995297
Latitude (b) Declination of Sirius (c)	16 00 8		0.018226
Declination of Sirius (c)	10 29 5.	elish and hardens	0.018220
-101 M. T. C.	64 22		0.044995
Second sum, or $(b+c) =$	72 26	sine .	9.979260
Deviation at Rigel	3.46	log.	0.539076
Deviation at Sirius	3.7745	log. 0 -03 -03 -03	0.576854

After having corrected the instrument by means of Sirius, I observed the transits of Castor and Procyon, and again those of Procyon and Pollux, and found the interval of time to agree with their difference in right ascension, from which I concluded, that in the space of about three hours I had placed my transit instru-

ment exactly in the meridian.

As it is rather a difficult operation to fix a transit instrument accurately in the meridian, these operations should be repeated a considerable number of times to insure the utmost possible accuracy. After the observations prove satisfactory, a meridian mark may be put up in a horizontal direction at a considerable distance, with which the central wire may be frequently examined and rectified previous to any very nice observation. This mark may be of various constructions, such as a copper-plate with a hole in it, so as a small segment of light may be seen on each side of the vertical middle wire, or a small notch in a building, or even a post at some distance. A thin slip of brass or copper painted black, with white lines or divisions at every inch, and numbered throughout, will also be found very convenient, and by knowing its distance the deviation upon it may be computed.*

The transit instrument being now properly rectified, it will be found the most accurate of all for determining the error and rate of a clock or chronometer, by taking the transit of the sun or stars daily, and marking the difference regularly in a column prepared for that purpose. If a star be observed, siderial time must be reduced

to mean solar time by Table XXXI. when necessary.

Ex. 1.—The observed times of the sun's passing the meridian of the observatory were as follows:—What was the original error on the last day of observation and the daily rate?

1826.	Obs. Time. Sun's Transit.	Mean Time. App. Noon.	Chronometer too	Daily Rate.
March 1 2 3 4 5 6	0 ^h 25 ^m 27 ^s .1 0 25 16.6 0 25 5.4 0 24 54.0 0 24 42.0 0 24 29.8	0 12 28.6 0 12 16.0 0 12 3.0 0 11 49.5	0 12 49.4 0 12 51.0 0 12 52.5	+ 1.6 + 1.4 + 1.6 + 1.5 + 1.7
	ly rate is the		the 6th of Ma 0 ^h 12 ⁿ	5\7.8 +1.56 rch, 1826, 542 fast.

^{*} Hor. deviation = sec. alt. × cos. dec. × obs. diff. of time × 15, to radius 1. On Capuan Kater's plan, by contracting the diameter of the object-glass by some contrivance for that purpose, the meridian mark may be only a few feet distant.—See his paper on the Floating Collimator.

Hence its error, supposing the rate to remain uniform, may, at any moderately distant future time, be determined.

Ex. 2.—On the same evenings the star Rigel passed the meridian as follows:—Required the daily rate and the original error on the sixth at the time of observation, about 6 o'clock in the evening?

1896.	Obs. Time. Sun's Transit.	Daily Diff. of Star's Transit.	Diff. of Mean and Siderial Time.	Dully Rate.
March 1	6 ^h 42 ^m 56 ⁿ .6 6 39 2.3	3 ^m 54'.3	3" 55'.9	+ 1.6
3 4	6 31 13.4	3 54.5	3 55.9 3 55.9	+ 1.4 + 1.5
6		3 54.2 3 54.2	3 55.9 3 55.9	‡ i.7
Rate by the s By the s			• •	5 7.9 +1.58 +1.56 2 8.14
	both noon, on the daily var., to		. 2 2	+ 1.57 3 6 21.4 55.5
Reduced R. A. Star's R. A. b	y Nautical Alı	man a c	. 9	3 7 16.9 5 6 12.5
Apparent time Equation of the			. 5	5 58 55.6 11 35.6
	transit of star it by chronome	eter on the 6	. C	
	nometer, fast b change of rate			12 53.8 12 54.6
•			_	8.4
Mean error at With a daily		•	. () 12 54.2 1.57

As opportunities may not occur daily for celestial observations, it is in that case necessary to compare a chronometer with a good clock, the rate of which can be depended on, and is occasionally ascertained by the heavenly bodies.

Ex. 3.—Given the daily difference between a chronometer and a clock, the rate of the clock being occasionally determined by celestial observations; to find the error and rate of the chronometer?

1826.	Clock before Mean Time.	Chron, differs from Clock,	Chron, before Mean Time.	Daily Rate.
May 1 2 3	+ 8.5 * + 8.9 + 9.4	+ 2.5 + 3.8 + 5.2	+ 11'.0 + 12.7 + 14.6	+ 1.7 + 1.9
4 5 6	+ 9.8 * + 10.1 + 10.5 *	+ 6.5 + 7.9 + 9.3	+ 16.3 + 18.0 + 19.8	+ 1.7 + 1.7 + 1.8

5 + 8.8

Mean daily rate + 1.76 And on the 6th at noon, the original error was fast 19'.8

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Hence the error of the chronometer may be found at any moderate distance of time, so far as its steady rate can be depended on.

The clock was examined by celestial observation, only where the asterisks are placed, or on the 1st, 4th, and 6th, and these are sufficient to ascertain, with the requisite precision, the rate of the chronometer when the clock is good. It is in a somewhat similar manner that the prize chronometers are tried at Greenwich.

Table of the variations of the sun's R. A. and dec. in 1 for every month in the year.

Month.	Var. in R. A. for 1 Second.	Var. in Dec. for 1 Second.		
January	0.0029	0".008 N.		
February	0.0027	0 .014 N.		
March	0.0025	0 .016 N.		
April	0.0026	0 .014 N.		
May	0.0028	0 .009 N.		
June	0.0029	0 .000		
July	0.0028	0 .006 S.		
August	0.0026	0 .013 S.		
Sept.	0.0025	0 .016 S.		
October	0.0026	0 .015 S.		
Novem.	0.0028	0 .010 S.		
December	0.0031	0 .002 S.		

This table will be useful when the change of the sun's R. A or D. for a few seconds only is wanted.

PART III.

mensuration, surveying, &c.

SECTION I.

Mensuration of Surfaces.

Mensuration is the application of Arithmetic to Geometry, by which the values of geometrical magnitudes are obtained in numbers.

In this case some determinate magnitude of the same kind with that to be measured is assumed, as unit, and the number of times this unit is contained in the given magnitude is the measure of that magnitude.

See Leslie's Geometry, Book V. Prop. XXV.

1. To find the area of a parallelogram, multiply the length by the

perpendicular breadth.

A . 19 . 1

2. Triangle.—Multiply the base by the perpendicular attitude; half the product is the area. Or take half the product of the two sides and the natural sine of the contained angle. Or when the three sides are given, multiply half the sum of the three sides, and the differences between that half sum and the three sides together, the square root of this product will be the area. This may be performed readily by logarithms.

3. Trapezium.—Multiply the base into half the sum of the per-

pendiculars.

4. Trapezoid.—Multiply half the sum of the parallel sides by the perpendicular distance between them.

5. Irregular Polygon.—Divide it into triangles, find their areas,

the sum of these will be the area.

- 6. Regular Polygon.—Multiply the square of the side given into the proper multiplier for areas from the table, page 142, for that purpose, and the product will be the area. Or, divide the polygon into triangles; find the area of one of them by some of the foregoing rules. Multiply this by the number in the whole polygon, the product is the area.
- 7. Circle.—The diameter is to the oircumference as 1 to 3.1415926536, or 1 to 3.141593 nearly.

The circumference is to the diameter as 1 to 0.318309.

The area is equivalent to the square of the diameter multiplied into 0.785398.

The area is equivalent to half the diameter multiplied into half

the circumference.

8. Circular Arc.—The length of a circular arc is equivalent to the radius of the circle multiplied by 0.0174533 and by the number of degrees in the arc.

Or, from eight times the chord of half the arc subtract the chord of the whole arc, one third of this remainder is the length of the

arc nearly.

9. Circular Sector.—The area is equivalent to the radius multipli-

ed into half the length of the arc.

10. Circular Segment.—Multiply the square of the radius by either half the difference of the arc of the segment and its sine, or by half their SUM, according as the segment is less or GREATER than a semicircle, and the product will be the area.

11. Parabola.—The area is equivalent to two-thirds of the pro-

duct of its base and altitude.

12. Ellipse.—The area is equivalent to the product of the transverse axis into the conjugate axis multiplied by 0.785398. Periphery.—Multiply the square root of half the sum of the squares of the two axes by 3.141593, the product will be the periphery nearly.

Examples for Exercise.

1. Required the area of a square of which the side is 5 feet 9 inches?

Ans.—33.0625 feet.

2. Required the area of a rectangle, if the length is 1375 links and

the breadth 950? Ans.—13° 0° 10°.

3. Required the area of a rhombus, of which the length of the side is 12.24 feet and height 9.16 feet?

Ans.-112.1184 square feet.

4. Required the area of a rhomboid, of which the length is 7 feet 9 inches, and height 3 feet 6 inches?

Ans. -27th. 1in. 6pa.

5. Required the area of a rhomboid, of which the adjacent sides are 2535 and 1040 links, and the contained angle 30°?

Ans .- 13ac. Or. 29p.

6. Required the area of a triangle, of which the base is 1225 links and altitude 850?

Ans .- 5 ac. 0 . 33 .

7. Required the area of a triangle, of which two of the sides are 30 and 40 and the contained angle 28° 57′ 18"?

Ans.-290.47356.

8. Required the area of a triangle, of which the three sides are 20, 30, and 40 feet?

Ans.—290.4737 square feet.

9. How many acres are there in a triangle, of which the three sides are 380, 420, and 765 yards?

Ans .- 9ac. 0r. 38p.

10. A ladder, 50 feet long, being placed in a street, reached a window 28 feet from the ground on one side; and, by turning it over, without removing the foot, it reached another window 36 feet high on the other side; required the breadth of the street?

Ans.-76.1233 feet.

11. How many acres are there in the trapezium, of which the diagonal is 475 links, and the two perpendiculars falling upon it on opposite sides, 225 and 360 links respectively.

Ans .- 13 ac. 2r. 25".

12. Required the area of a regular hexagon, one of whose equal sides is 14.6 feet and the perpendicular from the centre 12.64 feet.

Ans.—553.632 feet.

13. If the diameter of a circle be 17, what is the circumference?

Ans.-53.4072.

14. If the circumference of the earth be 24850 miles, what is the liameter?

Ans.—7910.

15. If the chord of an arc be 30, the height or versed sine 8, what is the length of the arc?

Ans.-351.

16. Required the length of an arc of 57° 17′ 44″.8; the diameter of the circle being 25 feet?

Ans.—12.5, which is equal to the radius.

- 17. Required the area of a circle, of which the diameter is 151 feet? Ans.—81.1798.
- 18. Required the radius of a circle in yards, of which the area is Ans.-39\100.
- 19. The diameters of two circles are 16 and 10; what is the area of the ring formed between these two circles, the centre being com-Ans.-122.5224.
- 20. Required the area of the sector, whose height or raised sine is 4 and the diameter of the circle 16?

Ans.—33.5103.

21. Required the area of the segment of a circle, of which the chord is 16 and the diameter of the circle 168?

Ans.--70.7083.

22. Let ABCD be a four-sided field, and from the side AB to the points C, D, let fall the perpendiculars PC and QD. Now the measure of AP is 110 links, PC is 352 links; AQ is 745 links, QD is 595 and AB is 1110 links; required the area of the field?

Ans .- 3 .. 3r. 35 p.

.10 .04088

TO FIND THE AREAS OF CIRCULAR SEGMENTS.

Rule.—Divide the height of the segment by the diameter, and find the quotient in the column of heights in the following table: Take out the corresponding area in the next column on the righthand; and multiply it by the square of the circle's diameter, for the area of the segment.

Height.	Area of the Segment.	Height.	Area of the Segment.	Height,	Area of the Segment.	Height.	Area of the Segment.	Height.	Area of the Segment,
.01	.00133	.11	.04701	.21	.11990	.31	.20738	.41	.30319
.02			.05339				.21667	.42	.31304
.03	.00687	.13	.06000	.23	.13646	.33	.22603	.43	.32293
.04				.24	.14494	.34	.23547	.44	.33284
.05	.01468	.15	.07387	.25	.15354	.35	.24498	.45	.34278
.06					.16226	.36	.25455	.46	.35274
.07						.37	.26418		
.08	.02944				.18002				
.09									

TABLE OF THE AREAS OF CIRCULAR SEGMENTS.

Ex. 1.—Taking as an example the chord 12, and the radius 10, or diameter 20.

.30 .19817

.40 .29337

.50l

.3927

.20 .11182

And having found the perpendicular from the centre upon the chord = 8; then 10-8=2 Hence, by the rule, =2+20=1the tabular height. This being sought in the first column of the table, the corresponding tabular area is found = 04088. Then $-04048 \times 20^{\circ} = -04088 \times 400 = 16.352$, the area.

The use of the following tables will be readily understood, from considering that the areas of similar figures are as the squares of their like dimensions, and their SOLIDITIES as the CUBES.

-DU Jeti

sais, and the product by substant of Hall of Table of Polygons, and the product by the fixed

No of Sides.	they are sometimes e	Multipliers for areas	Radius of circum.	Factors for sides
3	Trigon	0.4330127	0.5773503	1.732051
4	Tetragon, or Square	1.0000000	0.7071068	1.414214
- 5	Pentagon	1.7204774	0.8506508	1.175570
6	Hexagon	2,5980762	1.00000000	1.000000
7	Heptagon	3.6339124	1.1523824	0.867767
8	Octagon	4.8284271	1.3065628	
9	Nonagon	6.1818242	1.4619022	0.684040
10	Decagon	7.6942088	1.6180340	0.618034
11	Undecagon	9.3656399	1.7747324	0.563465
12	Dodecagon	11.1961524	1.9318517	0.517638

October Section II

Mensuration of Solids.

Delegacity Company of the Company of

1. Prism. (1.) Surface. Multiply the perimeter of one end by the length or height, the product will be the surface of the sides. To this add the areas of the two ends, and the sum will be the whole surface. 01888.0

(2.) Solidity or Capacity. Multiply the area of the base by the height, the product will be the solid content. The same rules de-

termine the surface and capacity of a cylinder.

2. Pyramid or Cone. (1.) Surface. Multiply half the perimeter of the base by the slant height. To this add the surface of the base, the sum is the whole surface.

(2.) Capacity. Multiply the area of the base by one-third the

perpendicular height.

3. Frustum of a Pyramid. (1.) Multiply half the sum of the perimeters of the two ends by the slant height. To this add the areas

of the two ends, the sum will be the whole surface.

(2.) Capacity. Add a diameter or side of the greater base to one of the less; from the square of the sum subtract the product of these two sides or diameter; multiply the remainder by a third of the height, and this last product by the proper number for the circle, .785398, or polygon, the last product will be the content.

4. Sphere. (1.) Surface. Multiply the square of the diameter

by 3.141593, the product is the surface. por 1 13991.02 paging and

(2.) Capacity. Multiply the cube of the diameter by 0.5236, or the cube of the circumference by 0.016887. vgoo and become a

5. Spheric Segment. (1.) Surface. Multiply the circumference

of the sphere by the height of the segment in and the segment in t

(2.) Capacity, or $c = 0.5236 h^2$ (3 d = 2 h), in which d is the diameter of the sphere and h the height; or $c = 0.5236 h^2$ (3 $r^2 +$ h2); in which r is the radius of the base of the segment and h its the base 2000 from and po-hanger 110 feet 3 A on-2122 height.

6. Paraboloid, or solid formed by the rotation of a parabola about dispersed the greater and a free time of the loss 3 feet, six at

Capacity. Multiply the base by its height, half the product is the content, younge a to minour a to windle out it mad W. Al

7. Spheroid, or solid formed by the revolution of an ellipse about one of its axes. and the helph of test? Ank 10380 cubic inches

Capacity. Multiply the square of the revolving axis by the fixed axis, and the product by 0.5236, the result will be the content.

8. Regular, or Platonic bodies, as they are sometimes called, are contained under like, equal, and regular plane figures, of which the solid angles are all equal. The names and descriptions of these bodies, together with their multipliers, the side of each being unity, are contained in the following tables:—

Surfaces and Solidities of Regular Bodies, the Side being Unity, or 1.

No of Sides.	Name.	Surface.	Solidity.
4	Tetraedron	1.7320508	0.1178513
6	Hexaedron	6.0000000	1.0000000
8	Octaedron	3.4641016	0.4714045
12	Dodecaedron	20.6457288	7.6631189
20	Icosaedron	8.6602540	2 1816950

The diam, of a sphere being 1; the side of a	That may be in- scribed in the sphere, is	That may be circum- scribed about the square, is	That is equal to the sphere, is
Tetraedron	0.816497	2.44948	1.64417
Hexaedron	0 577350	1.00000	0.88610
Octaedron	0.707107	1.22474	1.03576
Dodecaedron	0.525731	0.66158	0.62153
Icosaedron	0.356822	0.44903	0.40883

Examples for Exercise.

- 1. Required the solidity of a cube, of which the side is 5 feet 3 inches? Ans. 1447 feet.
- 2. What is the solidity of a block of marble, of which the length is 10 feet, breadth 5\frac{7}{2} feet, and depth 3\frac{1}{2} feet? Ans. 201\frac{1}{2} feet.
- 3. Required the solidity of a prism, of which the base is a hexagon, each of the equal sides being 1 foot 4 inches, and the length of the prism 15 feet? Ans. 69.282 feet.
- 4. Required the convex surface of a cylinder, of which the circumference is 8 feet 4 inches, and length 14 feet? Ans. 1163 feet.
- 5. What is the solidity of a cylinder, of which the length is 5 ft. and diameter of its base 2 feet? Ans. 15.708 feet.
- 6. The diameter of the base of a right cone is 44 feet, and the slant height 20 feet; required the convex surface? Ans. 141.372 feet.
- 7. Required the convex surface of a frustum of a right cone, the circumference of the greater end being 30 feet, that of the less 10 feet, and the slant height 20 feet? Ans. 400 feet.
- 8. What is the solidity of a triangular pyramid, of which the height is 30, and each side of its base 3? Ans. 38.97.
- 9. What is the solidity of a cone, of which the circumference of the base is 40 feet, and its height 50 feet? Ans. 2122 feet.
- 10. What is the solidity of the frustum of a cone, of which the diameter of the greater end is 5 feet, that of the less 3 feet, and the perpendicular height 9 feet? Ans. 115.454 cubic feet.
- 11. What is the solidity of a frustum of a square pyramid, one side of the greater end being 18 inches, that of the less 15 inches, and the height 5 feet? Ans. 16380 cubic inches.

12. Required the convex superficies of a sphere, of which the diameter is 17 inches? Ans. 907.92 square inches.

13. Required the solidity of the same? Ans. 1.48868 cubic feet.

14. Required the solidity of the earth, considering it as a perfect sphere, of which the diameter is 7910 miles? Ans. 259136798136 cubic miles.

15. What is the solidity of the segment of a sphere, of which the diameter of the base is 20 feet, and its height 9 feet? Ans. 1795.4244 cubic feet.

SECTION III.

Surveying.

In landsurveying, the instruments commonly employed for the ordinary purposes are-

1. Gunter's chain, and ten iron pins.

2. Cross-staff, and signal staves.

Field-book, or paper.
 Case of mathematical instruments.

5. Plotting scales.

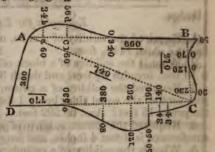
6. Parallel ruler, and beam compasses.

7. A small quadrant, if a theodolite is not at hand, to reduce the hypotenusal to their horizontal measure.

It would exceed our present limits to describe all these, as well as some others, which may however appear perhaps in a work proposed with that view.

An Example of Laying Off a Field.

Having set up poles at A, B, C, and D, so as with the different dotted lines to reduce the body of the field to a quadrilateral form, and drawn a sketch of it, into which the measures when taken may be inserted; begin at any point A, measur- D ing the successive distances A a, A c, &c., on the chainline A B, and the corre-



sponding offsets ab, cd, &c., and marking them as in the figure till a complete circuit A B C D A of the field and the diagonal A C are measured; these afford data for planning it, and computing the area. For the various portions may be considered either as trapezoids or triangles, whose contents may be ascertained by the rules given for that purpose.* The area computed in this manner will be 2.4295 acres, or 2 ac. 1 ro. 28.72 po., though it is better in general to retain it in acres and decimals. It is necessary to take an account of the roads, dikes, ponds, &c., of which the contents must all be stated distinctly by themselves when a whole estate is surveyed. In the case of the sale of crops, that in tillage only must be measured.

Required the plan and area of the field, from the following fieldbook, in which the angles were measured, with the pocket-box, sextant, and the distances with the chain, beginning the operations at the gate near the south-east corner?

Many landsurveyors first construct an accurate plan, from which, by scale and compass, the area is obtained with sufficient precision; and this is at least a good method of checking the result by computation.

Field-Book.

Left hind Offices, &c.		Stations, Distances, and Angles.	Right-hand Offices, &c.
	Links		
Hedge.	0		Remark. The chain-
,	88	143	line bears nearly west
		1 at 99° 45' 30" W.	along the north side
	73 83	200	of Bitterick Syke.
Deadriggs* or	83	940	ļ
Crosshall lands	70		Ì
on the south or left	34	400	
hand	0	490	
	0 44 42 100	510	
	44	650	
	42	726	
	100	810	
		⊙2d 85° 43′ 30″ N.	
Boundary.	0	0	The chain-line bears
	2	200	nearly north.
	5	400	
	3	600	
		800	
	10	860	_
	0	8 66	
		⊙ 3d 73° 8′ 0″ E.	
Hedge.	0 50 66 83 30	. 0	
	50	100	
Hardacres land	66	200	The chain-line bears
on the north	83	264	nearly east.
or left hand	30	360	
	66	456	
	5	5 44	·
	130	700	
	0	755	
		⊙ 4th101° 28'0" 8.	The chain-line bears
•	_0	100	almost south along
	12		the road from Green-
	38 66		law to Eccles. The
	06		diagonal from ⊙ 1st
	108	500	to O 3d, measuring
To ⊙ lst, or	143		1053 links, was also
		A 0 1450m	taken, that the area
	- 1	Area = 6.14537 ac.	might by the three
		or 6 ac. 0 ro. 23 po.	sides of the triangles
			be a check upon that
			determined from us-
1944 Ltd 2 444	4		ing the angles.

If there are dikes, ditches, or fences of any kind, they must be measured during the survey, and their amount stated. Also plantations, reads, commons, lakes, ponds, &c., must be all surveyed and classed separately from the arable land. For these we cannot here enter into detail.

This place is mentioned in Sir Walter Scott's Minstrelsy of the Scottish Border.

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in case of levelling for canal guilleved case is not different, only the

It is often necessary to ascertain the difference of elevation of one point above another, for the purpose of conveying a stream of water to drive machinery. This may be performed in several ways, but the readiest and most acurate is by means of a spirit-level of the best construction. It must be accompanied by a pole, or rod divided into feet, and at least hundredths of a foot. On this rod a sliding vane is fitted, capable of moving easily up and down, and having a dark strong line or other well-defined mark upon it, by which the telescope, or in common levels the sight, may be directed. The slider must be moved upwards or downwards on the rod, till the mark coincide with the intersections of the cross hairs in the focus of the telescope. When this is accomplished, and the level being properly adjusted, the height in feet and hundredth parts is to be carefully read off and marked in a book for the purpose. Now, by means of a chain or measuring tape, let the pole-bearer place it at equal distances, alternately on each side of the level, such as about one or two hundred yards, if convenient, if a level with a good telescope be used. If an ordinary level with a plain sight be used, the distance must be reduced to as many feet. The heights taken with the telescope turned towards the place whence the observer set out, are called the back observations; and those taken towards the place where he means to finish, are called fore observations, for the sake of distinction. Since the pole is always placed at equal distances from the level, no allowance need be made for the curvature of the earth.* solerical area, and then of

.anolimego Lenitsboug men EXAMPLE.

8	muil	EXAM	IPLE.	the	As a check upon the re-
į	Ва	ick.	For	re.	thought upgains ons
I	Dist.	Height on Pole.	Height on Pole,	Dist.	on the survey of the sales
ł	Links.	Feet.	Feet.	Links.	on he birmal - library
ı	100	2.92	4.68	100	a subte own many Al
١	100	1.56	3.79	100	about it presents by
ì	200	0.48	5.63	200	A montant wind w 111
Ä	200	1.35	4.86	200	seol for hundred and some
ı	150	1.27	3.74	150	interest outs out 92 VI
Į	150	100000000000000000000000000000000000000	2.56	150	Imigraphy and line or coming
9	100	2.36	3.94 4.36	100	must be required in it b
ı	50	3.20	4.50	50	the of the station, each
ı	1050	14.56	33 56	nn o	the running by which the
ı	2	14.00	14.56	MAIL	P is us by moustred.
ĺ		Honole	200	1314	meyed, and the distant
ĺ	2100	17 7	19.00	TERMO	quired to find Co the
k	0.1	-	THE STATE OF		Suppose A Contract

Hence the difference of level on a sloping height of 2100 links of Gunter's surveying chain, or $2100 \times 0.66 = 1386$ feet, is 19 feet. When a spirit-level exactly adapted to this purpose, is not at hand, if there is a theodolite to be had, it will perform the operation, though it is not quite so convenient.

^{*} The difference of level is about 8 inches in a mile, which increases as the square of the distance. The difference of level in feet allowing for refraction, is a of the square of the distance in English miles.

In case of levelling for canals, the process is not different, only the canal is carried on an exact level, by judiciously choosing the situation winding round rising grounds, conveying it across ravines by aqueduct bridges, and allowing it to descend at particular points, by means of locks. Roads ought to be carried along a level line as nearly as possible, and only having gentle acclivities and declivities. This may be readily obtained by following routes somewhat circuitous in uneven parts of the country, taking the advantage of ravines, water courses, and the sides of lakes; for a greater distance on a road nearly level, is productive of less expense of animal strength, than by passing over considerable elevations. All very quick turns in the road, particularly when entering upon a bridge, ought to be avoided, as the danger from centrifugal force, which may be readily estimated by the formula, Part III., Sec. IV., is considerable. The justice of these remarks may be readily appreciated by considering many parts in most of our public roads which have hitherto been constructed upon the very worst principles, having been entrusted to what are called practical men, who are frequently the mere slaves of custom.

SECTION IV.

Rules and Formulæ.

When two angles of a plane triangle are known the third may be found, consequently, for general purposes, it is unnecessary to measure the third angle. But when great accuracy is required, or when the sides on the surface of the earth are large, they become spherical arcs, and then the third angle should always be measured as a check upon the results. In conducting geodetical operations, the triangle should be so chosen, if possible, as to produce the most accurate conclusions. To diminish the probability of error, the following rules should be observed:—

I. When one side only of a triangle is to be determined, the mea-

sured base should be nearly equal to the required side.

II. When two sides of a triangle are to be determined, the triangle

should, if possible, be equilateral.

III. When the base cannot be equal to one or to both the required sides, it should be as long as possible, and the two angles at the

base equal, and not less than twenty or thirty degrees.*

IV. When the centre of the instrument cannot be placed in the vertical line occupied by the axis of a signal, the observed angles must be reduced to it by an appropriate formula. Let C be the centre of the station, such as a tower, P the place of the centre of the instrument, by which the angle subtended by A B at

P is to be measured. Let the angle A P B be observed, and the distance C P be measured, it is required to find C, the measure of the angle A C B? Suppose A P B = P, B P C = p, C P = d, A C = D and B C = D'.

Since the exterior angle of the triangle API is equal to the sum of the two interior and opposite CP angles. AIB = P+IAP, and of the triangle BIC, the exterior angle AIB = C+CBP. Making these two values of AIB equal, by transposition, we have C-P=IAP-CBP. But

^{/ •} For a demonstration of these properties, see vol. 111. of Hutton's Course of Mathematics.

the triangles C A P, C B P give sin. C A P = sin. I A P =
CP $APC = d \sin(P+p)$, $CPP = CP$
$\frac{CP}{AC}$ sin. $APC = \frac{d \sin (P+p)}{D}$; sin. $CBP = \frac{CP}{BC}$ sin. $BPC =$
$\frac{d \sin p}{D}$. And since the angles C A P, C B P, are, by hypothesis,
The same of the sa
always very small, their sines may be substituted for their arcs,
hence $C - P = \frac{d \sin (P + p)}{d \sin p}$, which in seconds becomes
hence, $C-P = \frac{d \sin (P+p)}{D} - \frac{d \sin p}{D'}$, which in seconds becomes
$\frac{d}{\sin 1'} \left\{ \frac{\sin (P+p)}{D} - \frac{\sin p}{D'} \right\}; \text{ or } R'' \text{ being the length of an arc in } D' = \frac{1}{2} \left\{ \frac{\sin (P+p)}{D} - \frac{\sin p}{D'} \right\}; \text{ or } R'' \text{ being the length of an arc in } D' = \frac{1}{2} \left\{ \frac{\sin (P+p)}{D} - \frac{\sin p}{D'} \right\}; \text{ or } R'' \text{ being the length of an arc in } D' = \frac{1}{2} \left\{ \frac{\sin (P+p)}{D} - \frac{\sin p}{D'} \right\}; \text{ or } R'' \text{ being the length of an arc in } D' = \frac{1}{2} \left\{ \frac{\sin (P+p)}{D} - \frac{\sin (P+p)}{D'} - \frac{\sin (P+p)}{D'} \right\}; \text{ or } R'' \text{ being the length of an arc in } D' = \frac{1}{2} \left\{ \frac{\sin (P+p)}{D} - \frac{\sin (P+p)}{D'} - \frac{\sin (P+p)}{D'} - \frac{\sin (P+p)}{D'} \right\}; \text{ or } R'' \text{ being the length of an arc in } D' = \frac{1}{2} \left\{ \frac{\sin (P+p)}{D'} - \frac{\sin (P+p)}{D'$
sin, If the rate of the D' be favole on any about a control of HV
seconds equal to the radius, or 200204.8, then C-P = R'ax
$\left\{\frac{\sin \cdot (P+p) - \sin \cdot p}{D}\right\}$. The use of this formula cannot be embar-
the state of the s
assing, provided the signs of sin. p , and sin. $(P+p)$ be properly
attended to, as is illustrated by the following example:—Let the observed angle P be 43° 52" 49".44, $p=264^{\circ}$ 41' 24", $d=10.706$ feet.
D = 57508 feet and D' = 66750 feet, required the reduction?
(1.) the (1.) was and do not be with and the (1.)
Log. R'house, 105.314425 low of lived to controllib out to nosing man
log. d 1.032860
109. 6
ciently accurate, by retaining the arts being thence, a = 0 x
+ 6.347285 - 6.347285
+ 6.347285 - 6.347285
$+$ 6.347285 $ 6.347285$ Sin. $(P+p)$ $ 9.893118$ sine p 264° $41'$ $24''$. $ 9.998132$
+ 6.347285 - 6.347285
$+$ 6.347285 $ 6.347285$ Sin. $(P+p)$ $ 9.893118$ sine p 264° $41'$ $24''$. $ 9.998132$
+ 6.347285 6.347285 Sin. $(P+p)$ -9.893118 sine p 264° 41′ 24″
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$
$ \begin{array}{c} + & 6.347285 \\ \text{Sin. (P+p)} \\ 308 & 34' & 14'' \end{array} \right\} -9.893118 \text{ sine } p & 264^{\circ} & 41' & 24'' \\ \text{ar. co. log. D} + 5.240272 \text{ ar. co. log. D'} \\ \text{(1.)} -30'' & 246-1.480675 \\ \text{(2.)} + & 33''.187 \\ \text{(1.)} -& 30 & .246 \\ \end{array} $ $ \begin{array}{c} + & 2.941 \\ \text{P} & . & . & . & . & . & . & . \\ \end{array} $
$\begin{array}{cccccccccccccccccccccccccccccccccccc$

When signals are circular or polygonal towers, various methods may be employed to find the true angle, from a due consideration of the nature of the case, which, to any one possessing a knowledge of the elements of geometry, will readily occur.

V. The angles measured in an inclined plane, should be reduced

to the horizontal plane.

In this case the altitudes must be also observed, and then there is formed a spherical triangle, of which the three sides are given to compute the angle at the zenith, which may be performed by the rules of spherical trigonometry.

VI. A spherical triangle being proposed, of which the three sides are very small compared with the radius of the sphere; if from each of its angles, one-third of the excess of the sum of its three angles, above two right angles be subtracted, the angles so diminished may be taken for the angles of a rectilineal triangle, whose sides are equal in length to those of the proposed triangle.

To find the spherical excess when the three sides are given in feet. 1. Rule.—To the constant logarithm 1.349380, add the logarithm of half the sum of the three sides, the logarithms of the three differences between these sides and that half sum, half the sum of these five logarithms will be the logarithm of the spherical excess in setaken for that purpose

conds.

2. To the legarithm of the area of the triangle taken as a plane one in feet, add the constant logarithm 0.674690; the sum is the logarithm of the excess above 180° in seconds.

3. If the base and perpendicular of a triangle be given. To the logarithm of the base in feet, add the logarithm of the perpendicular, and the constant logarithm 0.373660; the sum will be the logarithm of the spherical excess in seconds.

The spherical excess amounts to one second for an area of 76 English square miles, whence, if the area in square miles be known, the spherical excess may be readily obtained by dividing it by 76.
VII. To reduce a base on an elevated level to that at the surface

of the sea.

Let r represent the radius of the earth, corresponding to the base b at the level of the sea, and r+a the radius referred to the level of the measured base B; then it is obvious that r+a:r:B: $b = B \times \frac{r}{r+a}$. Hence, $B - b = B - B \frac{r}{r+a} = B \times \frac{a}{r+a} = B \times \frac{a}{r+a}$ $\left(\frac{a}{r} - \frac{a^s}{r^2} + &c\right)$. But the radius of the earth being very great in comparison of the difference of level a, we have the correction \mathbf{r} sufficiently accurate, by retaining the first term. Hence, $\delta = B \times \overline{b}$

Rule.—By logarithms. To the logarithm of the measured base in feet, add the logarithm of its height above the sea, and the constant logarithm 2.680110; the sum will be the logarithm of a number of feet which, taken from the measured base, will be that at the level of the sea required.

VIII. To determine the horizontal refraction from observation.

Rule.—From the measure of the intercepted terrestrial arc, subtract the sum of the two depressions at its extremities; half the remainder is the refraction. If by reason of the smallness of the contained arc, one of the objects has an elevation instead of a depression, then the depression must be taken from the sum of the contained arc and elevation; half the remainder is the refraction.

PORMULM.

$$R = \frac{c - d - d'}{2} = \frac{c - (d + d')}{2} \qquad (1.)$$

If -d' becomes an elevation, it changes its sign, and becomes +e, and in that case $R = \frac{e+e-d}{2}$.

The exact quantity of terrestrial refraction is very variable. It is estimated by Dr Maskelyne at one-tenth of the intercepted arc, by Delambre at one-eleventh, by General Mudge at one-twelfth, and by Liegendre at one-fourteenth at a mean state of the atmosphere. peculiar circumstances it varies very considerably from this, as from one-sixth to one-eighteenth of the contained arc.

IX. To find the angle made by a given line with the meridian.

With a good instrument measure the greatest and least angular distance of the pole star from the vertical plane in which the given line is situated; half the sum of these two measures will the angle requited.

This may also be done, though less accurately, by computing the azimuth of the sunger a star, when on the line, from an altitude taken for that purpose.

X. In addition to what has already been said relative to find-ing the latitude of the place, we may add here, that the same thing may be very accurately obtained, by observing the greatest and least altitude or zenith distance of a circumpolar star, and correcting them for the effects of refraction; half the sum of the altitudes, thus corrected, will be the latitude, or half the sum of the zenith distances will be the colatitude.

XI. To determine the ratio of the earth's axes, and their actual magnitude from the measure of a degree of the meridian in two given distant latitudes, supposing the earth a spheroid generated by

the rotation of an ellipse about its minor axis.*

Let d and d' be the measure of two degrees, d being the least, or that nearest the equator, I and I the latitudes of their middle points, t the semitransverse axis of the meridian or radius of the equator, c the semiconjugate or semipolar axis, e the excess of the equatorial radius above the polar semiaxis, and ro = 57°.2957795, the number of degrees in an arc are equal to the radius.

And
$$\frac{e}{t} = \frac{a-a}{3 \text{ d sin. } (l'+l) \times \sin. (l'-l)}$$
 . (2.)

If
$$\frac{e}{t} = i$$
, ellipticity or compression, $t = \frac{r^5 d}{1 - \frac{i}{2} - \frac{5}{5}i \cos 2t}$ (3.)

from formula (1.)
$$e = \frac{r^{\circ}(d'-d)}{3\sin^{\circ} l} . \qquad (4.)$$

Therefore, the excess of the degree in any latitude above this degree at the equator, when divided by the square of the sine of the latitude, should always give the same quotient; or the excess of the degrees of the meridian above the degree at the equator, should be

as the squares of the sines of the latitudes.

Since $e = \frac{r^{\circ}(d'-d)}{3\sin(l'+l)\sin(l'-l)}$, then $d'-d = \frac{3}{r^{\circ}}\sin(l'+l) \times \sin(l'+l)$

sin. (l'+l) is in the second of the secon $d'-d=\frac{3}{2}\frac{e}{sin}$ sin. (2 $l+1^{\circ}$) sin. 1° , and since the sine of one degree is

0.017453,
$$d'-d = \frac{3 e \times 0.017453}{r^{\circ}} \sin(2 l + 1^{\circ})$$
 (6.)+

The contiguous degrees therefore differ, by a quantity proportional to the sine of twice the middle latitude. The difference is a maximum when $2 l+1^{\circ} = 90^{\circ}$, or when the middle latitude is 45°.

From five different measures combined so as to produce the most accurate result, Mr Playfair found $\epsilon = 0.0032 = \frac{1}{312.5}$ nearly, and the equation representing the degrees of the meridian setting out from 45°, will be

 $D = 60759.472 - 290.576 \cos 2 l \pm 1$ in fathoms, or,

^{*} Playfair's Outlines of Natural Philosophy, Vol. II. Art. 59. + Using logarithms, d-d=C. L. 1.0084715 + log. sin. (2 $l+1^\circ$) in fathoms, or d-d=C. L. 1.7866228+log. sin. (2 $l+1^\circ$) in feet, where e=11158.8 fathoms, or 60952.8 feet respectively, and d = 60460 fathoms, or 362760 feet. ‡ In toises D = 57011—272.65 cos. 2 ℓ .

 \cdot D = 69.044-0.3299 cos. 21 (8.)in English miles.

Hence,
$$e = 11158.8 = 12.680$$
 $t = 3486858.8 = 3962.349$
 $c = 3475700.0 = 3949.669$

The radius of curvature for the parallel of $45^{\circ} = t - \frac{e}{2} = 2481279.4$ The circumference of the meridian is fath. = 3956.009 miles.therefore equal to the product of the mean degree at 45° by 360 = 24855.84 miles; and the circumference of the equator is 24896.16 miles, or about 40 miles more than the preceding.

A geographical mile is therefore 1012.6 fathoms, or 6075.6 feet. The semidiameter or distance from the centre to the surface, at any

latitude l, or $r = t (1-s \sin^2 l + \frac{5}{2} s^2 \sin^2 l \cos^2 l$. If d be a degree of the meridian at any point of which the latitude is l, and D a degree of the curve perpendicular to the meridian at the same point, then, $e = \frac{r^{\circ}}{2}$ (D-d) sec. 2 l.

nen,
$$e = \frac{1}{2} (D-d) \sec^2 t$$
 . . . (10.)

$$t = r^{\circ} D - \frac{r^{\circ}}{2} (D - d) \tan^{2} l. \qquad (11.)$$

$$\frac{e}{t} \text{ or } s = \frac{D - d}{2 D \cos^{2} l} = \frac{D - d}{2 D} \times \sec^{2} l. \qquad (12.)$$

For exercise the following measures of degrees of latitude are given.

Observers.	Lat.	Degrees in Toises.	Deductions.
Mason Boscovich Delambre	0° 0′ 0″ 0 0 0 12 5 0N. 35 18 0S. 39 12 0N. 43 1 0N. 46 12 0N. 52 220N: 66 20 0N.	56753 56749 56761 57037 56868 56979 57021 57069 57168	Radius of the equator 3271691 toises. Semipolar axis. 3260964 toises, \$ = \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$

Let these be solved by the foregoing theorems, and the various consequences drawn.

Ex. 1.—In the Philosophical Transactions for 1795, D the degree perpendicular to the meridian, is given equal to 61182 English fathors; d = 60851, and $l = 50^{\circ} 4'$ N. By formula. (12.)

 $\frac{10000 \text{ 331}}{2 \times 61182} \times \text{sec.}$ \$ 50° 41' = $\frac{1}{148.4}$ nearly, and much too great.

Ex. 2.—The length of a degree in latitude 52° 2′ 20" N. is 57074 taises, that in 119 0' N. is 56755 toises; required the ellipticity by formula (2.)?

The second secon

$l' = 52^{\circ} 2' 20'$ l = 11 0 0	const. log.	A real was high fallow	9.522879
$\begin{array}{c} l' + l = \overline{ 63 \ 2 \ 20 } \\ l' - l = 41 \ 22 \ 0 \end{array}$	cosecant,	The same sense	0.049969 0.182718
$d' = 57074 \\ d = 56755$	ar. co. log.	another and the contraction	5.245996
d'—d 319	log.	art with the misse of	2.503791
or $= \frac{0.003202}{10000} = \frac{32}{10000} = \frac{32}{10000}$	A COUNTY OF THE PARTY OF	mally the later of the control of th	7.505353

If L = the length of a degree of longitude, then

$$L = \frac{\cos l}{r^{\circ}} (1 + \epsilon \sin^{2} l + \frac{3}{4} \epsilon^{2} \sin^{4} l). \qquad (13.)^{\circ}$$

If the value of the degree is wanted in toises, fathoms, or feet, the second member of this equation must be multiplied by the semitransverse axis in the same measure.

Ex. 1.—Required the length of a degree of latitude at Edinburgh.

in 56° N.?

By formula (7), $D = 60759.472 + 290.576 \times \sin 22^{\circ} = 60759.427$ $+290.576 \times 0.374607 = 60868.3$ fathoms.

Ex. 2.—Required the length of a degree of longitude in latitude 56° N., the ellipticity being 300?

By formula (13), $L = \frac{0.559193}{57.2957795} \left\{ 1 + \frac{1}{300} \times 0.68694 \right\}$; or L = $0.009760 \times 1.00229 \times 20918750 = 204635$ feet, or, taking in the second term mentioned in the note, it is 204648 feet. These formulæ are useful for fixing the latitude and longitude of a particular point when referred to some object whose situation has been well determined. such as many places in Britain are by the trigonometrical survey In this case any amateur observer may verify the latitude and longitude of his observatory deduced from his own observations, by a comparison with some point well settled in that work, when properly connected by trigonometrical operations. Even by taking a few angles with great care, the situation of a particular point may be well settled by spherical trigonometry, as in the following example communicated by Captain Hall.

Ex. 2.—Given the latitude of the Staff on North Berwick Law, 56° 3′ 8″ N., longitude 2° 42′ 11″ W., and the latitude of the Isle of of May light 56° 11′ 22″ N., longitude 2° 32′ 47″ W.; the angle at North Berwick Law, between the Isle of May and Dunglass Tower. 87° 41′ 1″, that at Dunglass, between the Isle of May and North Berwick Law, being 37° 20′ 13″; required the latitude and longi-

tude of Dunglass Tower?

Ans. Lat. 55° 56′ 31″.7 N., Long. 2° 21′ 42″ W.

^{*} If great accuracy is not required, 3 4 2 sin. * 4 may be omitted in the quantity within the parenthesis.

If p be the length of a degree perpendicular to the meridian, t the equatorial radius, c the semipolar axis, t—c=d the difference of these, r^o the length of an arc in degrees equal to radius, or 57°.2957795, $t + d \sin^2 t$

and
$$l$$
 the latitude, then $p = \frac{t + d \sin^{-2} l}{r^{\circ}}$ nearly. . . (14)

Ex. 5.—If t = 3486850 fathoms, d = 11160 fathoms, and $l = 56^{\circ}$, then $p = \frac{3486850 + 11160 \times \cdot 68694}{57.29578} = 60991$ fathoms.

If p be the measure of a degree of a great circle perpendicular to a meridian at a certain point, m that of the corresponding degree on the meridian itself, and o the length of a degree on an oblique arc, making an angle a with the meridian, then

$$o = \frac{p \, m}{p - (p - m) \sin^{-2} a} = \frac{m}{1 - \frac{p - m}{p} \sin^{-2} a}$$

$$Ex \, 6 - \text{If } n = 61182 \text{ fathoms } m = 60850 \text{ fathoms and } a = 918560 \text{ fathoms}$$

Ex. 6.—If p = 61182 fathoms, m = 60850 fathoms, and $a = 81^{\circ}56'$ 53", therefore

53", therefore
$$o = \frac{60850}{1 - \frac{332}{61182} \times 0.98038} = \frac{60850}{1 - 0.00632} = \frac{60850}{0.99468} = 61175.45 \text{ the}$$

length of the oblique degree in fathoms.

For an extension of this subject, see Mr Ivory on the properties of a line of the shortest distance traced on the surface of the oblate spheroid, in the sixty-seventh volume of the Philosophical Magazine. It is rather too long and difficult to be inserted in this place.

SECTION V.

Rules and Formulæ.

SPECIFIC GRAVITY.

The difference between the absolute weight of a body, and its weight when entirely immersed in a fluid, is the same with the weight of a quantity of the fluid equal in bulk to the body.

If W be the weight of a body in vacuo, (which is nearly the same as that in air,) and W' its weight in water, then W—W' is the weight of a quantity of water equal in bulk to the body; and since the weight of any body divided by an equal bulk of water, measures the specific

gravity, S, of the body, then
$$S = \frac{W}{W - W'}$$
. (1)

The specific gravities of bodies are determined by the hydrostatic balance, the hydrometer, &c. described in books on Natural Philosophy.

To compute the specific gravity of air under given circumstances. It is shown in Playfair's Outlines, vol. I. § 333, that if the elasticity or tension at the freezing point, be denoted by unity and x, any number of degrees above that point, then the elastic force f at that point, will be $f = (1.375)^{\frac{1}{180}}$ of Fahrenheit's scale, or

$$\log f = \frac{x}{180} \times \log. (1.375) = \frac{x}{180} \times 0.138303$$
 (2)

This also gives the bulk of gas in like circumstances. But the specific gravity is reciprocally as the bulk, therefore the reciprocal of the bulk or the natural number answering to the arithmetical complement of the log. f, will be the specific gravity of permanent

elastic fluids. Thus let the bulk and specific gravity of air at 32° $F_{\cdot} = 1$, then at 52° F. they will be 1.036, and 0.9652 respectively.

From the experiments of Gay Lussac, it may be shown that 0.4545 will be the specific gravity of aqueous vapour, when compared with atmospheric air, at 32° F. Now, when the temperature is given, the specific gravity of aqueous vapour is directly as its temperature, and the tension being given, the specific gravity is reciprocally as its bulk, the specific gravity s of aqueous vapour, (that of water being 1), in saturated air at any temperature t, and elastic force f, (from Dalton's table) will be obtained from the following formula, the ba-

rometer being at 30 inches.
$$s = 0.4545 \times \frac{f}{30} \times \frac{660}{448+t} = \frac{10 f}{448+t} \qquad (3)$$

If it be not saturated, and
$$t'$$
 being the dew point $s = \frac{10 f}{448 + t} \times \frac{448 + t}{448 + t'} = \frac{10 f}{448 + t} \times \left(1 + \frac{t - t'}{448 + t'}\right)$ (4)

The quantities in this expression are all known except f which is to be taken from any good table, such as Dalton's or Ure's. See Table

II., page 48.

If, therefore, s' be the specific gravity of air fully saturated with moisture, a the specific gravity of dry air obtained from formula (2), and s the specific gravity of aqueous vapour in saturated air, derived from formulæ (3), then from the law of expansion discovered by

Dalton and Gay Lussac, that $v = \frac{p}{p - f_*}$, p being the barometric pressure, f the elastic force, and v the volume,

pressure,
$$f$$
 the elastic force, and v the volume,
$$s' = a + \left(0.4545 \times \frac{660}{448 + t} - a\right) \times \frac{f}{30}, \text{ or by simplication,}$$

$$s' = a + s - \frac{af}{30} \qquad (5)$$

If t' be the dew point, and s" be the specific gravity, according to the actual state of the atmosphere,

$$s'' = \left(a + s - \frac{af}{30}\right) \left(1 + \frac{t - t'}{448 + t'}\right) \tag{6}$$

in which a and s are got from the following table, page 165, and f from

Ex.—Required the specific gravity of air saturated with moisture,

By formula (2), $\frac{60}{180} \times 0.138303 = \frac{1}{3} \times 0.138303 = 0.046101$, ar. co. of which is 9.953899. To this the natural number is 0.89929=a.

But by formula (3),
$$s = \frac{10f}{448+i} = 0.02782$$
, and $\frac{af}{30} = 0.04502$.

Now, $s' = a + s - \frac{af}{30}$ by formula (5); therefore, s' = 0.89929 +0.02782-0.04502=0.88209 the specific gravity of air saturated with moisture, at 92° F. If the air is not saturated. Suppose 87° F. the dew point represented by t', then the factor $1 + \frac{t-t'}{448+t'}$ in formula

^{*} Daniell and Tredgold, contend that this formula should be p+f. The difference in a moderate range, however, is not great. The elasticity in the example, was not taken from Dalton. It is difficult to obtain correct formulæ for these researches.

(6), becomes $1 + \frac{92 - 87}{448 + 92} = 1 + \frac{1}{108}$, therefore, $0.88209 + \frac{0.88209}{108} = 0.88209 + 0.00817 = 0.89026$, the specific gravity of air in the given circumstances, that of dry air at 32° F. being unity.

It is shown in Playfair's Outlines, vol. I., art. 256, that if the specific gravity of air be called m, that of water being 1; if W be the weight of any body in air, and W' its weight in water, then W+m (W—W') is its weight in vacuo very nearly. In a mean state of the atmosphere at 30 inches of the barometer and 60° F. m=0.00122 nearly, which may be reduced to any other temperature by the foregoing formula (4), and to any other pressure by multiplying $\frac{p}{30}$

If s be the specific gravity of a body ascertained by weighing it in air and water, and m the specific gravity of the air at the time when the experiment was made; the correct specific gravity s', or that which would have been found if the body had been weighed in a vacuum instead of air, or

s' = s + m (1—s). (7) Where the body is heavier than water, this correction is subtrac-

tive; when lighter it is additive.

Ex.—The weight of Captain Kater's experimental pendulum was carefully determined in air, by Barton's balance from the Mint, and found to be 66904 grains. The trough, which had been previously placed under the pendulum, was then filled with distilled water, and the weight of the water displaced was 9066 grains. The small portion of iron wire which was immersed in the water was carefully noted; the weight of the wire by which the pendulum was suspended was 56 grains, and the weight of water equal in bulk to that part of the wire which was immersed was 2.5 grains. The temperature of the water was 68° F., that of the atmosphere 62' F., and the ba-

rometer 29.9 inches. Now since $s = \frac{w}{w - w'}$, w being the weight in air, and w' that in water, then

 $s = \frac{66848}{9063.5} = 7.37552$ at 29.9 bar. and 62° F., and s' = 7.37552 + 0.00120678 (1—7.37552) = 7.36783 at 68° Fahrenheit.

But the specific gravity of water oat 68° is 99936, that at 62' being 1; and, therefore

 $\frac{1}{s} \times s' = \frac{1}{0.99936} \times 7.36783 = 7.37254$ at 62° F.

2 7 may 2 2 2

Biot's experiments give at 30 inches bar., and 60° F, the specific gravity of air 0.00122, or $\frac{1}{820}$, water being 1.

Mr S. Rice, from Sir G. Shuckburgh's experiments, deduces 0.0012085, not differing much from Biot's, and generally supposed the more correct. According to Gay Lussac, the expansions of fluids from 32° to 212° F. is 0.375, whence $\frac{.375}{180} = \frac{1}{480}$ for 1° F.

Now suppose c = the first correction of the length of the pendulum, c' the second, l the measured length of the pendulum, p the barometric pressure, the standard being 30 inches; and l the difference of temperature from the standard, then

$$c = \frac{30 \times 820}{p} = \frac{24600}{p}$$

$$c' = c \times \frac{30}{480} = \frac{c}{480} = \frac{c}{480}$$

$$c' = c \times \frac{30}{480} = \frac{c}{480} = \frac{c}{480}$$

$$c' = c \times \frac{30}{480} = \frac{c}{480} = \frac{c}{480}$$

$$c' = c \times \frac{30}{480} = \frac{c}{480} = \frac{c}{480}$$

If l' = the corrected length of the pendulum l, from a mean of Captain Kater's experiments at London in air, then $l' = l + \frac{l}{s(c+c')}$ (10), s being the specific gravity of the pendulum.

Whence $e = \frac{24600}{29.786} = 826$, and $\delta t = 69^{\circ}.62 - 62^{\circ} = 7^{\circ}.62$, hence

$$c' = \frac{826 \times 7.62}{480} = 13$$
, therefore $c + c' = 839$.

 $c' = \frac{826 \times 7.62}{480} = 13$, therefore c + c' = 839.

Hence by formula (10) $l' = l + 39.13284 \times \frac{1}{839} \times \frac{1}{7.37254} = l + 0.00633$.

It is now only necessary to correct for the height above the sea, which is 92.5 feet.

The correction for this height found by the formula, which will

presently be given, is 0.00023.

Hence l'' = 39.13284 + 0.00633 + 0.00023 = 39.13940. In this case no allowance is made for the hygrometer. Now if the air were supposed half saturated with moisture, since Captain Kater does not give the state of the hygrometer, and the mean between Biot's and Rice's specific gravity of air taken, the true length would come out 39.13938, which differs from Captain Kater's result by 0.00009 in

It is shown by writers on mechanics, that when the semiare described by a pendulum is 1°, the time lost by oscillating in a circu-

lar, instead of a cycloidal or infinitely small arc, is 59594 in each se-

cond, and that in different small arcs of the same circle, the time lost varies nearly as the square of the arc; hence if a pendulum makes v vibrations in 24, when vibrating in very small circular arcs, of which the mean at the commencement and termination of each experiment is d degrees, it would, in the same time, make v+

52524 infinitely small vibrations. Hence to correct the oscillations of a pendulum for the arcs of vibration, multiply the square of the

mean arc when it makes

Daily 86000 oscillations by

1.637

1.639

1.641 -ad fliw (al.) 86200 pg 16-bus days and detrillating white 1.641 86300 86400 - 1(4 — 86500 86600

Since the force of gravity varies directly as the length of the pendulum, or inversely as the squares of the number of vibrations, and the diminution of the force of gravity, arising from the buoyancy of the atmosphere, is $\frac{1}{m}$ past; therefore if v be the number of vibra-

tion in air, and V those in a vacuum, then

$$V = \left\{ v^2 \left(1 + \frac{1}{m} \right) \right\}^{\frac{1}{2}} = v \left\{ 1 + \frac{1}{2m} - \frac{1}{8m^2} + \&c. \right\}$$
 (10)

V = v + c, and hence $c = \frac{v}{2m}$ nearly.

In Captain Kater's experiments at Unst, the specific gravity of the pendulum, to that of air, was as 7099 to 1, hence $\frac{1}{m} = \frac{1}{7000}$, and

therefore $\frac{v}{2m} = \frac{86090.77}{14198} = 6.07$ nearly.

If n' be the number of oscillations performed in 24 by the experimental pendulum, n the true number, e the expansion for a change of one degree Fahrenheit, t the standard temperature, and t' the observed, then

 $n = n' + \frac{1}{2}n' e(t' - t)$. (11) In Captain Kater's pendulum e=0.00001 of an inch nearly, whence

 $n = n' + \frac{1}{2}n' \times 0.00001$ (t' - t). Hence if v = 86058.82, $t' = 71^{\circ}.6$ and $t = 62^{\circ}$, the number of vibrations at the latter temperature are $n = 86058.72 + \frac{1}{4} \times 86058.72 \times \frac{1}{4}$

 $0.00001 \times 9.6 = 86082.77$.

To reduce the length of the pendulum from any height to the level of the sea, the true length being denoted by I, the observed by l', the height above the sea by a, and the radius of the earth by r,

$$l = l' + \frac{2 a l'}{r} \tag{12}$$

Some allow one-third for the effect of the dense strata immediate-

ly under the pendulum, in which case
$$l = l' + \frac{4 a l'}{3 r}$$
 . (13)

In a similar manner
$$v = v' + \frac{2 v' a}{3 r}$$
 . (14)

At Unst
$$\frac{2 v' a}{3 r} = 0.06$$
, therefore

1.000

170

86090.77 + 6.07 + 0.06 = 86096.90 =the number of oscillations of the pendulum in a mean solar day at the level of the sea in vacuo.

These formulæ are sufficient for most purposes. Biot has, however, demonstrated, that if c be the correction in seconds for the mean arc of vibration, n the number of oscillations. M the logarithmic modulus, a the arc of vibration at the commencement of the interval, and b that at the end, then

 $c = \frac{n' \sin (a+b) \sin (a-b)}{2}$ (15)32 M log. (+)

These arcs being small, their lengths will not differ sensibly from their sines, whence if a and b are given in degrees, the lengths of these arcs will be 0.0174533 a and 0.0174533 b, and M = 2.302585, these values being substituted for a, b, and M, equation (15) will be-

come $c = \frac{n'(a+b)(a-b)}{241886 \log. (\log. a-\log. b)}$, and adopting logarithms, we finally have $\log. c = \{\log. n' + \log. (a+b) + \log. (a-b)\} - \{C. L. 5.383611 + \log. (\log. a - \log. b).$ (16)

To apply this to practice let us assume Kater's t marked E, and we have $a=1^{\circ}.21$ and $b=1^{\circ}.09$, whence $a+b=2.30$ log. $a-b=0.12$ log. $a'=86056.47$ log.	oth experiment 0.361728 0.079181 1.934785
Sum 5.383611 Constant logarithm 5.383611 Log. $a = 1^{\circ}.21$. 0.082785 $b = 1.09$. 0.037426	1.375694
Diff. 0.045359 log. 2.656663	1.040274 (B)

 $(A - B) = \log c = 2.165.$

Hence n = n' + c = 86056.47 + 2.165 = 86058.635. Captain Kater thinking this an unnecessary refinement in practice, multiplies the square of the mean arc by 1.638 Table (A); thus $1.15 \times 1.15 \times 1.638 = 2.166$ nearly the same as before; and, by selecting the proper number, this is sufficiently correct for almost any purpose,

and much more simple.

If the length of a pendulum oscillating seconds of mean time at one place or point on the earth's surface be known, its length at another place, where the same invariable pendulum makes a different number of vibrations, may readily be found. For if l be the length at the first place, l' that at the second, v the number of vibrations at the first place in 24 hours, and v' that at the second, then as is shown by writers on mechanics,* l: l'::v2:v'2 consequently if three of these be known the fourth may be found.

As this is rather laborious, an approximate rule may be obtained sufficiently correct for most purposes where the difference of oscillations does not exceed 30 or 40, or in an arc of five or six degrees. If AL represent a small variation of the length of the pendulum, and \triangle N that in the number of oscillations, then \triangle L, $-\frac{L \triangle N}{A}$,

and
$$\Delta N = \frac{1}{2} \frac{N}{L} \Delta L$$
. (18)

Let & L be the variation of L for one degree of Fahrenheit's thermometer, and n the number of degrees of change of temperature, for this then $\Delta L = n \delta L \times L$, and $\Delta N = \frac{1}{2} N n \delta L$. Since the variation of brass from expansion is nearly 0.00001 inch

for 1° Fah,
$$\Delta N = 0.432 n$$
, and $\Delta L = \frac{n L}{100000}$ (20)

tal entol legitiminy only to Example It Captain Kater found the experimental pendulum made at London in latitude 51° 31′ 8″ N. 86061.52 oscillations at 62° Fah. in a mean solar day, while at Unst in latitude 60° 45' 28" N., it made 86096.90 oscillations in the same time; required the length of the pendulum at Unst, that at London being 39.13929 inches?

^{*} Sec Gregory's Mechanics, vol. I., section 11., for this and other formulæ and corrections more simple than those given here. or rade and entires the distance is proposed in the deal proposed and proposed and

Here $86096.90 - 86061.52 = 35.38 = \Delta N$. Now $\Delta L = \frac{L \Delta N}{\lambda N}$

formula (18) = $\frac{39.13929 \times 35.38}{43048.45}$ = 0.03217, consequently 39.13929

+ 0.03217 = 39.17146 inches, the length at Unst.

Ex. 2.—Captain Hall found an experimental pendulum, making 86235.98 oscillations at London at 62° Fah., made 86101.34 oscillations at Galapagos at the temperature of 68°. Hence from the number of oscillations at London (since 68°-62°=6°,) we must subtract (formula 20) $0.432 \times 6 = 2.59$ oscillations from that at London, which becomes 86233.39.

Now by formula (17), as the places are very distant, $v^2: v'^2::l:$ l':: 39.13929: 39.01951, the length of the pendulum at Galapagos.

Of late the figure of the earth has been determined with great accuracy by means of the pendulum. It is demonstrated by the theory of gravitation, that the length of the pendulum is augmented from the equator to the pole, proportionally to the square of the sine of the latitude, in such a manner that if the length of the equatorial pendulum be represented by z, and its absolute variation from the equator to the pole by y, then l, its length in any other latitude, L will be represented by the following equation:—

 $l=z+y\sin^2 L$ If we have two equations of this form, in which l and L are de-

termined by observation, we can obtain the values of z and y.

$$l = z + y \sin^2 L$$

$$l' = z + y \sin^2 L'$$

hence
$$y = \frac{l' - l}{\sin \cdot (L' + L) \sin \cdot (l' - L)}$$
 (2)
 $z = l - y \sin^2 L$. (3)

And
$$z = l - y \sin^2 L$$
 . (3)

Consequently $\frac{y}{z}$ represents the diminution of gravity from the pole to the equator.

Now by the doctrine of central forces if f denote the centrifugal force; * the circumference of a circle to diameter unity; r the radius of the given circle in which a body revolves; t the time of re-

volution, and g the gravitating force, then $f = \frac{4\pi}{g} \frac{s}{t^2}$. But by the theory of the pendulum, if l is its length, $g = \pi^2 l$; hence

$$f = \frac{4 r}{t^2 l} = \frac{r}{(\frac{t}{2})^2 l} \tag{4}$$

The ratio of the centrifugal force to gravity may be expressed by $\frac{f}{1+f}$, and the ellipticity of the meridian or flattening of the earth is from theory equal to §* of the ratio of the centrifugal force to gravity, diminished by the fraction obtained from dividing the difference of the lengths of the pendulum at the pole and equator by its length at the equator. Wherefore if a denote the ellipticity,

This fraction is obtained by approximation, and is not perfectly correct. By taking in the quantities of the second order, the ellipticity would vary about 18 from the first approximation. It is difficult to solve the equations involving these. Still, however, no error should be allowed, if possible, to affect the final results, but what unavoidably belongs to the observations.

$$\mathfrak{s} = \frac{5}{2} \times \frac{f}{1+f} - \frac{y}{z}$$

By substituting the value of f from equation (4)

$$\mathfrak{s} = \frac{5}{2} \times \frac{r}{r + \left(\frac{\mathfrak{t}}{2}\right)^2 l} - \frac{y}{z} \qquad (5)$$

As t in these investigations denotes the time which the earth takes to perform a rotation about its axis, or 86164.0908; $\frac{1}{2}$ $t^2 =$ 1856062632, r, the radius of the equator, is 20918750 feet, l, the length of the equatorial pendulum by numerous observations, is 39.013 inches, or 3.25108 feet, and y = 0.20712 inch.

Whence
$$s = 0.008638 - \frac{y}{z}$$
 (6)

By combining a great number of the best observations I have found $s = 0.003333 = \frac{1}{300}$ nearly.

From these we may get a formula to compute the length of the pendulum at any latitude.

Commencing at the equator $l = 39.013 + 0.20712 \sin^2 L$

Setting out from 45°, l = 39.11656 - 0.10356 cos.2 L Ex.—Required the length of the pendulum at Leith, in latitude 55° 58′ 39″ N. ?

Ans.—39.1555 inches. Since $g = \pi^2 l = 32.2$ feet.

Hence the length of the pendulum and force of gravity may be found at any latitude.

But the force of gravity may be found more readily by a particular formula for that purpose.

Since g is equal to 32.172 feet, or 9.8058 metres at 45°, then G at any other latitude will be

$$G = g (1 - 0.00268 \cos^2 L)$$

Or $G = 32.172 (1 - 0.00268 \cos^2 L)$ in feet. (7)

Let L be the length of the sexagesimal pendulum and l that of the French decimal-metrical pendulum, then

$$L = 52.74079 l . (8)$$

of Sir George Shuckburgh's scale,

Let v be the velocity of sound at 30 inches of the English barometer, 60° of Fahrenheit's thermometer and 14° of Mr Goldingham's hygrometer which he used at Madras, also let a be the change of velocity for a variation of one inch of the English barometer, & for that of one degree of Fahrenheit's thermometer, y that for one degree of Mr G's hygrometer, ω the velocity of the wind, and φ the angle which the direction of the wind makes with that of the sound,

and V the true velocity under given circumstances, then $V = v + \alpha (p' - p) + \beta (t' - t) + \gamma (h' - h) + \omega \cos \varphi$ (10) in which p = 30 inches, $t = 60^{\circ}$ Fah. $h = 14^{\circ}$ hygrometer, and p', t'and h', the observed states of the barometer, thermometer, and hygrometer, respectively.

From an examination of Mr Goldingham's experiments at Madras, I have found $\alpha=18.8$ feet, $\beta=1.14$ feet, and $\gamma=2.87$ feet. The values of ω and φ not being stated in any set of experiments which I have seen, have not been exactly verified. They must be known, however, at the time of computing the velocity as they undoubtedly affect it. Without these it becomes

 $V = 1100 + 18.8 (p' - 30) + 1.14 (t' - 60^{\circ}) + 2.87 (h' - 14^{\circ}) (11)$

Required the velocity at Port Bowen, the Bar. being at 30.398 in. Fahrenheit's Ther. — 38°.5., the state of the hygrometer, and velocity and exact direction of the wind being unknown?

Ans.—995.19, differing about 19 feet from observation from want

of the other parts of the data.

Or, if V be the velocity, t the temperature, f the elastic force of vapour by Dalton's table for the dew point, obtained by Daniell's hygrometer, or otherwise by formula, page 53, p the barometric pressure, λ the latitude of the place of observation, and ω cos. φ the same as before,

 $V = \{104.0885 + 0.10831 (i - 32^{\circ})\} \left(1 + \frac{f}{5\frac{1}{2}p - 2f}\right) (10.2738 - 0.01378 \cos. 2 \lambda) + \omega \cos. \varphi, \text{ in English feet.}$ (12)

Ex.—On the 19th of July, 1826, in mean latitude 56° N., longitude 3° 10′ W., several experiments were tried on the velocity of sound, when the guns on Edinburgh Castle were fired in honour of his Majesty's coronation. They were made on the coast of Fife at the distance of 42546 feet, the barometer standing at 29.96 inches, the thermometer at 72°, the dew point by Daniell's hygrometer, or by a thermometer, having its bulb moistened with tissue paper, (page 53) at 66°, the velocity of the wind by an anemometer was 15 miles per hour, or 22 feet in a second, making an angle of 60° with that of the sound; required the true rate per second and the difference between theory and experiment, when the arithmetical mean of a number of experiments gives 37.448 seconds for the time elapsed between seeing the flash and hearing the report?*

$$V = \{104.0885 + 4.3324\} \left(1 + \frac{0.635}{158.52}\right) (10.2738 + 0.1136) + 22 \times 0.5 = 108.4209 \times 1.004 \times 10.3874 + 11 = 1141.715$$

Experiment gives
$$\frac{42546}{37.448} = \frac{1136.189}{5.526}$$
Difference
$$\frac{42546}{37.448} = \frac{1136.189}{5.526}$$

or excess of the formula.

In a river or open canal, let v be the velocity of the stream measured by the inches it moves over in a second of time; r a constant quantity, called the radius of the section, and obtained by dividing the area of the transverse section of the stream expressed in square inches by the boundary or perimeter of that section, diminished by the superficial breadth of the stream expressed in linear inches. Also let λ be the length of an open canal or of a close pipe; δ the difference of the level of its extremities, d the diameter in the case of a pipe, h the height of the water in the reservoir above the upper orifice of the pipe, and h' the height above the lower orifice, at which the water stands in the cistern into which it is emptied.

Now let $\frac{\partial}{\partial x} = i$ or the sine of inclination and $\frac{h + \partial - h'}{\lambda} = k$.

The formula for the velocity of water in pipes, per second, will be $v = \{32806.6 \ d \ k + 0.023751\}^{\frac{1}{2}} - 0.154113$. (13)

[•] If a series of experiments are made by a gun at each end of the measured base, the geometrical means of the times should be taken. See Bulletin de Soiences for 1826.

To find the fall in a river caused by obstruction, such as the piers of a bridge, &c.

Let v be the velocity of the stream in feet per second, b the whole breadth of the channel in feet, c the contracted breadth between the

obstacles, and f the fall, then $f = \left\{ \left(\frac{25 \ b}{21 \ c} \right)^2 - 1 \right\} \frac{v^2}{64} = \frac{1.42 \ b^2 - c^2}{64 \ c^2} \times v^2 \text{ very nearly}$ Let, as is nearly the case with the old London Bridge,

 $v=3\frac{1}{6}$, b=926, c=200,

Hence $f = \frac{1.42 \ b^2 - c^2}{64 \ c^2} \times v^2 = 0.46 \times 10 \ c = 4.73$ feet, or 4 ft. $8\frac{\pi}{4}$ inches by the formula, while that by experiment was 4 feet 9 inches.

TO FIND THE TONNAGE OF A SHIP BY LOGARITHMS, ACCORDING TO THE COMMON METHOD.

Rule.—If the vessel is a ship of war, let fall a perpendicular from the fore-side of the stem, at the height of the hause holes; but if a merchantman, the perpendicular is to be let fall from that part of the fore-side of the stem which is at the same height above the keel, as the wing transom: also let fall another perpendicular from the back of the main post, at the height of the wing transom. Find the distance between these two perpendiculars, from which subtract three-fifths of the extreme breadth; and also, the product of the height of the wing transom above the upper edge of the keel, by 2½ inches, and the remainder is the length of the keel for tonnage. To the logarithm of which, add the logarithm of the breadth, and that of the half-breadth, and the constant logarithm 8.02687;* the sum, rejecting 10 from the index, will be the logarithm of the tonnage re-

Ex.-Let the length between the perpendicular at the fore-part of the stem, and the back of the post, be 100 feet: the extreme breadth 271 feet, and the height of the wing transom 15 feet. Required the tonnage?—Ans. 321 tons.

The arithmetical complement of the logarithm of 94, being the common divisor for finding the tonnage. This method is far from being correct. See papers on Naval Architecture, published by Morgan and Creuze. G. B. Whittaker, London. 1826.

TABLES OF SPECIFIC GRAVITY.

	7700						
SOLIDS.							
Platina 20.722	Marble, green Campanian	2.742					
Gold, pure, hammered 19.362	, Parian .	2.837					
Guinea of George III. 17.629	Parian Norwegian , green Egyptian	2.728					
Tungsten . 17.600	, green Egyptian	2.668					
Tungsten 17.600 Mercury, at 32° Fahren. 13.598		2.110					
Lead 11.352	Pearl	2.752					
Lead	Chalk, British .	2.784					
Rhodium 11.000	Jasper Coral Rock Crystal English Pebble Limpid Feldspar Glass, green —, white —, bottle Porcelaine, China	2.710					
Virgin Silver . 10.744	Coral	2.680					
Shilling of George III. 10.534	Rock Crystal	2.653					
Bismuth, molten . 9.822	English Pebble .	2.619					
Copper, wire-drawn 8.878	Limpid Feldspar .	2.564					
Red Copper, molten 8.788	Glass, green	2.642					
Molybdena . 8.611	——, white	2.892					
Bismuth, molten 9.822 Copper, wire-drawn 8.878 Red Copper, molten 8.788 Molybdena 8.611 Arsenic 8.308 Nickel, molten 8.279	, bottle .	2.733					
Nickel, molten . 8.279	Porcelaine, China .	2.385					
i Uranium 6.1(m) 1		2.341					
Steel from 7.769 to 7.816	Native Sulphur .	2.033					
Cobalt, molten . 7.812	Ivory	1.917					
Cobalt, molten	Native Sulphur . Ivory Alabaster,	1.874					
Pure Cornish Tin . 7.291	Alum	1.720					
Ditto hardened . 7.299 Cast Iron . 7.207	Copal, opaque	1.140					
Cast Iron . 7.207	l Sodium	973					
Pure Cornish Tin 7.291 Ditto hardened 7.299 Cast Iron 7.207 Zinc 6.862 Antimony 6.712 Tellurium 6.115 Chromium 5.900	Sodium Oak, heart of	950					
Antimony . 6.712	lce	930					
Tellurium . 6.115	Potassium	866					
Chromium 5.900	Beech	852 845					
Spar, neavy . 4.430	Ash						
Jargon of Ceylon . 4.410	Apple-1 ree	793 705					
Sembles Oriental 2004	Deer Tree	661					
Sappnire, Oriental 5.994	Pear-Tree	604					
Ditto Brazilian . 5.151	Linden-Tree	598					
Oriental Topaz . 4019	Cypress	5 6 1					
Diamond Company 2 501 to 2 521	Cedar	550					
Diamond . from 3.501 to 3.551	Popler	383					
Towardin 2 155		240					
Achaette	COPK	#1 0 ,					
Zinc 6.862 Antimony 6.712 Tellurium 6.115 Chromium 5.900 Spar, heavy 4.430 Jargon of Ceylon 4.416 Oriental Ruby 4.283 Sapphire, Oriental 3.994 Ditto Brazilian 3.131 Oriental Topaz 4.019 Oriental Beryl 3.549 Diamond from 3.501 to 3.531 English Flint Glass 3.329 Tourmalin 3.155 Asbestus 2.996	I						
Lio	UIDS.						
		991					
Sulphuric Acid . 1.841 Nitrous Acid . 1.550	Burgundy Wine .	915					
Water from the Deed Co. 1.550	Olive Oil Muriatic Ether .	874					
Water from the Dead Sea 1.240	Muriatic Etner	0/4 070					
Nitric Acid 1.218 Sea-Water 1.026 Milk 1.030 Distilled Water 1.000 Wine of Bourdeaux 944	Oil of Turpentine . Liquid Bitumen . Alcohol, absolute . Sulphuric Ether .	870 848					
Nea-water 1.020	Liquia Ditumen .	792					
Discilled 1974 1 000	Alconoi, absolute .	716					
Wing of David	Air at the Earth's sur. ab	out 14					
wine on bourdeaux 944	Aif at the Larth's sur. ad	vut 1					

^{1.} Since a cubic foot of water, at the temperature of 40° Fahrenheit, weighs 1000 ounces avoirdupois, or 62½ pounds, the numbers in the preceding tables, omitting the decimal points, exhibit very

nearly the respective weights of a cubic foot of the several substances

in avoirdupois ounces.

2. If the weight of a body be known in avoirdupois ounces, its weight in Troy ounces will be found in multiplying it into 91145. And, if the weight be given in Troy ounces, it will be found in avoirdupois by multiplying it into 1 0971.

	GA	SES.	
Atmospheric air* .	1.0000	Muriatic acid-gas .	1.2474
Vapour of hydriotic ether		Sulphuretted hydrogen	1.1912
oil of turpentine		Oxygen-gas	1.1036
Hydriotic acid-gas .		Nitrous-gas	1.0288
Fluo-silicic acid-gas .	3.5735	Olefiant-gas	0.9784
Vapour of sulph. of carbon		Azote, or nitrogen-gas	0.9691
sulphuric ether		Oxide of carbon -	0.9569
Chlorine	2.4700	Hydro-cyanic vapour	0.9476
Fluo-boric gas		Phosphuretted hydrogen	0.8700
Vapour of muriatic ether		Steam of water .	0.6235
Sulphurous acid-gas .	2.1920	Ammoniacal-gas .	0.5967
Cyanogen		Carburetted hydrogen	0.5550
Vapour of absolute alcohol			0.5290
Nitrous oxide		Hydrogen-gas	0.0732
Carbonic acid	1.5196		DARGO
THE RESERVE OF THE PARTY OF THE	30373820	1, hence Gas S. G. × 0.00122	= S. G.

Specific gravity of Distilled Water at different temperatures, that at 62° being taken as unity.

170°	0.99913	62°	1.00000	54°	1.00064	26°	46°	1.00102	340
68	0.99936	60	1.00018	52	1.00076	28	44	1.00107	36
66	0.99958	58	1.00035	50	1.00087	30	42	1 00111	38
64	0.99980	56	1.00050	48	1.00095	32	40	1.00113	40

MISCELLANEOUS COMPUTATIONS AND EXPERIMENTS.

The pendulum vibrating seconds of mean solar time at London in a vacuum, and reduced to the level of the sea, is 39 1393 inches; consequently the descent of a heavy body from rest in one second of time, in a vacuum, will be 193.145 inches. The logarithm 2 2858828.

A platina metre at the temperature of 32°, supposed to be the ten millionth part of the quadrant of the meridian, 39°3708 inches. The ratio to the imperial measure of three feet, as 1°09363 to 1, the logarithm 0°0388717.

The following standards, accurately measured, give these results:— Gen. Lambton's scale, used in the Trig. Surv. of India, 35 99934 inches.

Sir G. Shuckburgh's sca				
may be considered as	identical	with the	impe-	-35.99998
rial standard) .	The said	1816	STOP OF	STATE OF THE PARTY.
Gen. Roy's scale .	121	199		36.00088
Royal Society's standard		100	10 170	36.00135
Ramsden's bar		1	1	36.00249
Weight of a cubic inch	of distille	d water i	n a va-	Total St. Sand
cuum at the temp. 6 weights in a vacuum a	2°, as or	posed to	brass	

Consequently a cubic foot 62:3862 pounds avoir-	
Weight of a cubic inch of distilled water in air at 62° of temperature with a mean height of the	log. 2.4021857
barometer 252.456 grains Consequently a cubic foot 62.3862 pounds avoir-	log. 1.7946314
And an ounce of water 1.73298 cubic inches	log. 0.2387924
Cubic inches in the imperial gallon, 277-276 Diameter of the cylinder containing a gallon at one inch high 18-78933	log. 2·4429124
inch high, 18.78933	, , , , , , , ,

SPECIFIC GRAVITY OF DRY AND SATURATED AIR.

That at 30 in. Bar., and 32° Fahr. being 1.

			_		
Temp. Fahr,	Specific Grav. of Dry Air.	Specific Grav. of Saturat. Air.	Temp. Fahr.	Specific Grav. of Dry Air.	Specific Grav. of Saturat. Air.
32°	1.00000	0.99750	67°	0.93996	0.93164
33	0.99824	0.99568	68	0.93829	0.92968
34	0.99647	0.99385	69	0.93664	0.92772
35	0.99471	0.99203	70	0.93499	0.82576
36	0.99294	0.99021	71	0.93333	0.92380
37	0.99119	0.98839	72	0.93168	0.92184
38	0.98944	0.98654	73	0.93004	0.91988
39	0.98769	0.98470	74	0.92839	0.91792
40	0.98595	0.98286	75	0.92675	0.91596
41	0.98420	0.98101	76	0.92511	0.91400
42	0.98246	0.97917	77	0.92347	0.91203
43	0.98073	0.97731	78	0.92184	0.91005
44	0.97900	0.97545	79	0.92021	0.90811
45	0.97726	0.97358	80	0.91859	0.90609
46	0.97553	0.97172	81	0.91656	0.90411
47	0.97381	0.96986	82	0.91534	0.90213
48	0.97209	0.96798	83	0.91373	0.90013
49	0.97038	0.96610	84	0.91211	0.89814
50	0.96866	0.96421	85	0.91050	0.89615
51	0.96695	0.96233	86	0.90889	0.89415
52	0.96524	0.96045	.87	0.90728	0.89216
53	0.96354	0.95855	88	0.90567	0.89014
54	0.96183	0.95665	89	0.90408	0.88813
55	0.96013	0.95475	90	0.90248	0.88611
56	0.95843	0.95285	91	0.90089	0.88410
57	0.95674	0.95095	92	0.89929	0.88208
58	0.95504	0.94902	93	0.89770	0.88006
59	0.95336	0.94710	94	0.89612	0.87803
60	0.95168	0.94518	95	0.89453	0.87602
61	0.94999	0.94326	96	0.89295	0.87401
62	0.94831	0 94134	97	0.89137	0.87199
63	0.94664	0.93940	98	0.88979	0.86995
64	0 94496	0.93746	99	0.88821	0.86790
65	0.94329	0 93552	100	0.88664	0.86585
66	0.94162	0.93338	110	0.87110	0.84329

On this subject see Biot's Traité de Physique, vol. I., ch. xix.

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weight, and that product again by 32.

3.—Divide the latter product by the former, for the deflection sought.

Ex.—An ash batten, 3 inches square, is fixed in a wall, and projects from it 4 feet. If a weight of 200 lbs. be hung on its extremity, how much will it be deflected?—Ans. 11 inches.

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Note.—If the beam be fixed at each end, the deflection will, with equal weights, be two-thirds of that found by the above rule.

Prob. IV.—To compute the Deflection of Beams supported at each End, and loaded uniformly throughout their Length with a given Weight.

Rule.—Compute the deflection the same as in the last problem. Multiply that result by 5, and divide the product by 8, and the quotient will be the answer.

Ex.—A uniform bar of Adriatic oak, 2 inches square, is rested upon two props, distant 24 feet, how much will it be deflected by its own weight, its specific gravity being 960, or 60 lbs. to the cubic foot?—Ans. 94 inches.

To apply this to practice be marked E, and we have $a=1^\circ$. $a+b=2.30 \log$. $a-b=0.12 \log$. $n'=86056.47 \log$.	et us assume Kater's 21 and $b=1^{\circ}.09$, when	5th experiment nce 0.361728 1.079181 4.934785
Sum	5.383611	4 375694
United Monthers on duties coope sur	og. 2.656663 4 040274	4.040274 (B)

 $(A - B) = \log c = 2.165.$ 0.335420

Hence n=n'+c=86056.47+2.165=86058.635. Captain Kater thinking this an unnecessary refinement in practice, multiplies the square of the mean arc by 1.638 Table (A); thus $1.15 \times 1.15 \times 1.638=2.166$ nearly the same as before; and, by selecting the proper number, this is sufficiently correct for almost any purpose,

and much more simple.

If the length of a pendulum oscillating seconds of mean time at one place or point on the earth's surface be known, its length at another place, where the same invariable pendulum makes a different number of vibrations, may readily be found. For if l be the length at the first place, l' that at the second, v the number of vibrations at the first place in 24 hours, and v' that at the second, then as is shown by writers on mechanics,* $l:l'::v^2:v'^2$. (17) consequently if three of these be known the fourth may be found.

As this is rather laborious, an approximate rule may be obtained sufficiently correct for most purposes where the difference of oscillations does not exceed 30 or 40, or in an arc of five or six degrees. If ΔL represent a small variation of the length of the pendulum.

and \triangle N that in the number of oscillations, then \triangle L, $-\frac{L \triangle N}{\frac{1}{2}N}$,

and
$$\Delta N = \frac{\frac{1}{2} N \Delta L}{L}$$
. (18)

Let δ L be the variation of L for one degree of Fahrenheit's thermometer, and n the number of degrees of change of temperature, for this then Δ L = n δ L × L, and Δ N = $\frac{1}{2}$ N n δ L . (19) Since the variation of brass from expansion is nearly 0.00001 inch

for 1° Fah,
$$\Delta N = 0.432 n$$
, and $\Delta L = \frac{n L}{100000}$ (20)

EXAMPLE I.

Captain Kater found the experimental pendulum made at London in latitude 51° 31′ 8″ N. 86061.52 oscillations at 62° Fah. in a mean solar day, while at Unst in latitude 60° 45′ 28″ N., it made 86096.90 oscillations in the same time; required the length of the pendulum at Unst, that at London being 39.13929 inches?

to and professor land and tootte or actions it, breakle and broads sures on the

^{*} See Gregory's Mechanics, vol. I., section II., for this and other formulæ and corrections more simple than those given here.

Here $86096.90 - 86061.52 = 35.38 = \Delta N$. Now $\Delta L = \frac{L \Delta N}{\lambda N}$

formula (18) = $\frac{39.13929 \times 35.38}{43048.45}$ = 0.03217, consequently 39.13929

+ 0.03217 = 39.17146 inches, the length at Unst.

Ex. 2.—Captain Hall found an experimental pendulum, making 86235.98 oscillations at London at 62° Fah., made 86101.34 oscillations at Galapagos at the temperature of 68°. Hence from the number of oscillations at London (since 68°-62°=6°,) we must subtract (formula 20) $0.432 \times 6 = 2.59$ oscillations from that at London, which becomes 86233.39.

Now by formula (17), as the places are very distant, $v^2: v'^2::l:$ l'::39.13929:39.01951, the length of the pendulum at Galapagos.

Of late the figure of the earth has been determined with great accuracy by means of the pendulum. It is demonstrated by the theory of gravitation, that the length of the pendulum is augmented from the equator to the pole, proportionally to the square of the sine of the latitude, in such a manner that if the length of the equatorial pendulum be represented by z, and its absolute variation from the equator to the pole by y, then l, its length in any other latitude, L will be represented by the following equation:—

 $l=z+y\sin^2 L$ If we have two equations of this form, in which land L are de-

termined by observation, we can obtain the values of z and u.

$$l = z + y \sin^2 L$$

$$l' = z + y \sin^2 L'$$

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hence $y = \frac{l' - l}{\sin \cdot (L' + L) \sin \cdot (l' - L)}$ (2)
$$z = l - y \sin^2 L$$
 (3)

And
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 . . (3)

Consequently represents the diminution of gravity from the pole

Now by the doctrine of central forces if f denote the centrifugal force; * the circumference of a circle to diameter unity; r the radius of the given circle in which a body revolves; t the time of re-

volution, and g the gravitating force, then $f = \frac{4\pi}{g} \frac{g}{t^2}$. But by the

theory of the pendulum, if l is its length, $g = \pi^2 l$; hence

$$f = \frac{4 r}{t^{2} l} = \frac{r}{(\frac{1}{2})^{2} l} \qquad (4)$$

The ratio of the centrifugal force to gravity may be expressed by $\frac{f}{1+f}$, and the ellipticity of the meridian or flattening of the earth is from theory equal to §* of the ratio of the centrifugal force to gravity, diminished by the fraction obtained from dividing the difference of the lengths of the pendulum at the pole and equator by its length at the equator. Wherefore if a denote the ellipticity,

This fraction is obtained by approximation, and is not perfectly correct. By taking in the quantities of the second order, the ellipticity would vary about 100 from the first approximation. It is difficult to solve the equations involving these. Still, however, no error should be allowed, if possible, to affect the final results, but what unavoidably belongs to the observations.

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Ex.—A square beam of English oak, whose side is 6 inches, is supported on two walls, 20 feet distant, and is to be loaded at its middle point with 1000 lbs., what will it be deflected?—Ans. 18 inch.

Note.—If the beam be fixed at each end, the deflection will, with equal weights, be two-thirds of that found by the above rule.

Prob. IV.—To compute the Deflection of Beams supported at each End, and loaded uniformly throughout their Length with a given Weight.

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Ex.—A uniform bar of Adriatic oak, 2 inches square, is rested upon two props, distant 24 feet, how much will it be deflected by its own weight, its specific gravity being 960, or 60 lbs. to the cubic foot?—Ans. 9½ inches.

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Do. Spec. 4.	560	518	4210830	1149	1172	7352
Norway Spar .	577	648	5832000	1474	1492	12180

^{*} From Barlow on the Strength of Timber.

Prob. I.—To find the Strength of Direct Cohesion of a Piece of Timber of any given Dimensions.

Rule.—Multiply the area of the transverse section, in inches, by the value of C, in the preceding table of data, and the product will be the strength required.

Note.—If the specific gravity be not the same as the mean tabular specific gravity; say, as the latter is to the former, so is the above product to the correct result.

Ex.—What weight will it require to tear asunder a piece of teak 3 inches square, the specific gravity being 745?—Ans. 139-95 lbs.

Prob. II.—To compute the Deflection of Beams fixed at one End and loaded at the other with any given Weight.

Rule 1.—Multiply the tabular value of E by the breadth and cube of the depth of the given beam, both in inches.

2.—Multiply also the cube of the length in inches by the given

weight, and that product again by 32.

3.—Divide the latter product by the former, for the deflection sought.

Ex.—An ash batten, 3 inches square, is fixed in a wall, and projects from it 4 feet. If a weight of 200 lbs. be hung on its extremity, how much will it be deflected?—Ans. 1; inches.

Note.—The same rule will apply, when the weight is distributed throughout the length, by multiplying the second product by 12 instead of 32.

PROB. III.—To compute the Deflection of Beams, supported at each End, and loaded in the Middle with any given Weight.

Rule 1.—Multiply the tabular value of E by the breadth and cube

of the depth, both in inches.

2.—Multiply also the cube of the length, in inches, by the given weight in lbs.; then divide the latter product by the former for the deflection sought.

Ex.—A square beam of English oak, whose side is 6 inches, is supported on two walls, 20 feet distant, and is to be loaded at its middle point with 1000 lbs., what will it be deflected?—Ans. 1.8 inch.

Note.—If the beam be fixed at each end, the deflection will, with equal weights, be two-thirds of that found by the above rule.

Prob. IV.—To compute the Deflection of Beams supported at each End, and loaded uniformly throughout their Length with a given Weight.

Rule.—Compute the deflection the same as in the last problem. Multiply that result by 5, and divide the product by 8, and the quotient will be the answer.

Ex.—A uniform bar of Adriatic oak, 2 inches square, is rested upon two props, distant 24 feet, how much will it be deflected by its own weight, its specific gravity being 960, or 60 lbs. to the cubic foot?—Ans. 94 inches.

PROB. V.—To compute the ultimate Deflection of Beams or Rods, before their Rupture.

Note.—The beams are supposed to be supported at each end.

Rule.—Multiply the tabular value of U, in the preceding table of data, by the depth of the beam in inches, and divide the square of the length, also in inches, by that product, for the ultimate deflection sought.

Ex.—A square inch rod of ash, 6 feet long, is broken by a weight applied to its centre: how much will it be deflected before it breaks? Ans. 13:1 inches.

Prob. VI.—To find the ultimate transverse Strength of any rectangular Beam of Timber, fixed at one End and loaded at the other.

Rule I.—Multiply the value of S, in the preceding table of data, by the breadth and square of the depth, both in inches, and divide that product by the length, also in inches, and the quotient will be the weight in lbs. This is approximative.

Rule II.—1. Take the ultimate deflection 8 times that of the last problem, and divide the deflection by the length, which will give

the sine of the angle; whence, by a table find the secant.

2. Multiply the secant by the breadth and square of the depth in inches, and the product again by the value of S' in the table of data.

3. Divide this last product by the length in inches, and the quotient will be the answer in lbs.

Ex. 1.—What weight will it require to break a piece of Mar forest fir, fixed by one end in a wall, and loaded at the other; the breadth being 2 inches, depth 3 inches, and length 4 feet?—Ans. 518 lbs.

PROB. VII.—To compute the ultimate transverse Strength of any rectangular Beam, when supported at both Ends and loaded in the Centre.

Rule I.—Multiply the tabular value of S by 4 times the breadth and square of the depth in inches, and divide that product by the

length, also in inches, for the weight.

Rule II.—1. Compute the ultimate deflection by Prob. V.; square that deflection, and divide it by the square of half the length of the beam, and add the quotient to 1, for the square of the secant of deflection; which multiply by the length in ihches.

Multiply the tabular value of S' by 4 times the breadth, and the square of the depth; and divide that product by the former an-

swer in lbs.

Ex.—What weight will be necessary to break a piece of larch similar to the third specimen, the length being 8 feet 4 inches, the breadth 8 inches, and depth 10 inches; being supported at each end, and loaded in the middle?—Ans. 36676 lbs.

MATHEMATICAL TABLES.

TABLE I.

THE MILES AND PARTS OF 4 MILE IN A DEGREE OF LONGITUDE
AT EVERY DEGREE OF LATITUDE.

D.L.	Miles.	D.L.	Miles.	D. L.	Miles.	D.L.	Miles.	D.L.	Miles.	D.L.	Miles.
1	59.99	16	57.67	31	51.43	46	41.68	61	29.09	76	14.52
2	59.96	17	57.38	32	50.88	47	40.98	62	28.17	77	13.50
3	59.92	18	57.06	33	50.32	48	40.15	63	27.24	78	12.47
4	59.85	19	56.73	34	49.74	49	39.36	64	26.30	79	11.45
5	59.77	20	56.38	35	49.15	50	38.57	65	25.36	80	10.48
6	59.67	21	56.01	36	48.54	51	37.76	66	24.40	81	9.39
7	59.55	22	55.63	37	47.92	52	36.94	67	23.44	82	8 35
8	59.42	23	\$5.23	38	47.28	53	36.11	68	22.48	83	7.31
9	59.26	24	54.81	39	46.63	54	35.27	69	21.50	84	6.27
10	59.08	25	54.38	40	45.96	55	34.41	70	20.52	85	5.23
11	58.89	26	53.93	41	45.28	56	33.55	71	19.53	86	4.19
12	<i>5</i> 8.68	27	53.46	42	44.59	57	32.68	72	18.54	87	3.14
13	58.46	28	52.97	43	43.88	58	31.80	73	17.54	88	2.09
14	58.22	29	52.47	44	43.16	59	30.90	74	16.54	89	1.05
15	57.95	30	51.96	45	42.43	60	30.00	75	15.53	90	0.00

TABLE II.

LOGARITHMS OF NUMBERS.

	No. 1-		100		Log.	0.000	0005	.00000	0
No.	Log.	No.	Log.	No.	Log.	No.	Log.	No.	Log.
1	0.000000	21	1.322219	41	1.612784	61	1.785330	81	1.908485
2	0.301030	22	1.342423	42	1.623249	62	1.792392	82	1.913614
3	0.477121	23	1.361728	43	1.633468	63	1.799341	83	1.919078
4	0.602060	24	1.380211	44	1.643453	64	1.806180	84	1.924279
5	0.698970	25	1.397940	45	1.653213	65	1.812913	85'	1.929419
6	0.778151	26	1.414973	46	1.662758	66	1.819544	86	1.934498
7	0.845098	27	1.431364	47	1.672098	67	1.826075	87	1.939519
8	0.903090	28	1.447158	48	1.681241	68	1.832509	88	1.944483
g	0.954243	29	1.462398	49	1.690196	69	1.838849	89	1.949390
10	1.000000	30	1.477121	50	1.698970	70	1.845098	90	1.954243
11	1.041393	31	1.491362	51	1.707570	71	1.851258	19	1.959041
12	1.079181	32	1.505150	52	1.716003	72	1.857332	92	1.963788
13	1.113943	33	1.518514	53	1.724276	73	1.863323	93	1.968483
14	1.146128	34	1.531479	54	1.732394	74	1.869232	94	1.973128
15	1.176091	35	1.544068	55	1.740363	75	1.875061	95	1.977724
16	1.204120	36	1.556303	56	1.748188	76	1.880814	96	1.982271
17	1.230449	37	1.568202	57	1.755875	77	1.886491	97	1.986772
18	1.255273	38	1.579784	58	1.763428	78	1.892095	98	1.991226
19	1.278754	39	1.591065	59	1.770852	79	1.897627	99.	1.995635
20	1.301030	40	1.692060	60	1.778151	80	1.903090	100	2.000000

2		- 4	A Table	of Log	arithm	s of Nu	mbers	from 1	to 100,	000.		
P. P.	N.	0	1	2	3	4	5	6	7	8	9	11
	-	The last of the last of the									00389	
41	1	4321	4751	5181	5609							
82 124	2			9451			4940				661	
165	4	100000		7868	8284			9532		Name and Address of the Owner, where the Owner, which is the Own	02077	
206	5			022016								00
247	6	5306					100000000000000000000000000000000000000	7757	8164	ALC: UNKNOWN THE	a management of	
288	7 8	9384									03302	
371	9	7426	033826 7825	9550	4628 8620	- CO E E CO	5430 9414				7028	
011	1000	THE RESERVE TO SHARE	The Party of the P		Land Committee of the	-					044935	-
38	1	5323		6105	6495	100000000000000000000000000000000000000						
75	2	9218	9606	9993				051538			052694	1 3
113	-		053463		4230		4996	5378	5760			
150 188	4	6905		7666	8046		8805	9185		063709	060320	
226	6	4458	4832	5206	5580		6326	6699	7071	7443		
263	7	8186	8557	8928	9298			100 May 10 May 1	and the second	A COLUMN TO SECOND	071514	
301		071882	072250	072617	072985	073352	3718	4085	4451	4816	The second second	3
338	9	5547	5912	6276	6640	7004	7368	7731	8094	8457		
											082426	
35 69	2	6360	National Confession Co	083503 7071	3861 7426	4219	4576 8136	4934 8490	5291 8845	5647 9198	9552	м
104	3										093071	
138		093422		4122	4471	4820						
173	5	6910	7257	7604	7951	8298	8644	8990	9335		100026	
208				101059							3462	
242	7 8	3804 7210	4146 7549	7888	4828 8227	5169 8565	5510 8903	5851 9241	6191 9579	6531	6871 110253	
311				111263							3609	
		113943	-	Acres de la constante de la co	THE RESERVE AND ADDRESS OF THE PERSON NAMED IN	Section Sectio		-	_		116940	_
32	1	7271	7603	7934	8265	8595	8926	9256	9586		120245	
64			100000000000000000000000000000000000000	121231	1000	11 CT 10 CO 10 CT				123198	3525	
96	3	3852	4178	4504	4830	5156	5481	5806	6131	6456	6781	
128	4	7105	7429	7753 130977	8076	8399	8722	9045	9368		130012	
193	6	3539	3858	4177	4496	4814	5133	5451	5769	6086	6403	
225	7	6721	7037	7354	7671	7987	8303	8618	8934	9249	9564	
257	8		and the last	4 4 4 4		The second second					142702	
289		143015	3327	3639	3951	4263	4574	4885	-5196	A COLUMN TWO IS NOT THE OWNER.	5818	
				146748	147058	147367	147676	147985	148294	148603	148911	3
30 60	2	9219	9527 152594		3205	3510	3815	4120	4424	4728	151982	
90	3	the same of the same of	5640	5943	6246	6549	6852	7154	7457	7759	8061	
120	4	8362	8664	8965	9266	9567	9868			160769	161068	30
149	1000		III MANAGEMENT	161967				3161	3460	3758	4055	
179	6	4353	4650	4947	5244	5541 8497	5838	6134 9086	6430 9380	6726 9674	7022	
209	7	7317	7613	7908 170848	8203		8792 171726				9968 172895	
269	9	3186	3478	3769	4060	4351	4641	4932	5222	5512	5802	
		176091		THE RESIDENCE OF THE PERSON NAMED IN	The second second	STATE OF THE PARTY.	-	THE RESERVE	_		178689	100
28	1	8977	9264	9552	9839	180126		180699	180986	181272	181558	2
56		181844		182415		2985	3270	3555	3839	4123	4407	
84	3	4691 7521	4975			5825	6108	6391	6674	6956	7239	21
112	4		7803	8084 190892	8366	8647	8928	9209	9490	192567	190051	
167	6		3403	3681	3959	4237	4514	4792	5069	5346	5623	
195	2	5900	6176	6453	6729	7005	7281	7556	7832	8107	8352	27
223	8		8935	9206	9481	9755					201124	27
251	9	201397	201670	201943	505516	202488	2761	3033	3305	3577	3848	27
P. P.	N.	0	100	2	3	4	. 5	6	7	8	9	D

	1.		Table	of Loga							1 0	3
P.	N.	0	1	2	3	4	5	6	7	8	9	D.
	160	204120	204391	204663	204934	205204	205175	205746	206016	206286	206550	271
26	. 1		7096	7365	7634	7904	8173	8441	8710	8979		269
52	2		9783	210051						211654	211921	267
79			212454									
105	4									6957		
131	5	7484	7747	8010	8273	8536	8798	9060	9323	9585		
157	6			220631			221414	221675	221936	222196	222456	561
183	7	2716					4015					
209	8	5309	5568									
236	9	7887	8144								230193	
		230449	230704	230960	231215	231470	231724	231979		232488	232742	254
25	1	2996					4261					
50	2	5528					6789		7292			
74	3			8548			9299				240300	
99	4			241048								
124	5											
149	6			6006	6252		6745	1000000	7237	7482		
174	7	7973					9198				250176	
198				250908						1200	2610	
223	9	2853	3096	3338	3580	-	4064	1000				-
				255755							257139	24)
23	1	7679	7918	8158	8398	8637	8877	9116	9355	9594		
47	2	260071		260548					261739	261976	262214	238
70												
94												
117							8344					
140	6	100000									271609	233
164	7			272306								
187	8	4158					5311					
211	9	6462	6692	6921	7151	7380	7609	7838	8067	8296	8525	229
	190	278754	278982	279211	279439	279667	279895	280123	280351	280578		
22	1		281261	281488	281715	281942	282169	2396	2622	2849	3075	227
44	2	3301	3527	3753	3979	4205	4431	4656	4882	5107		
67	3	5557	5782	6007	6232	6456	6681	6905	7130			
89	4	7802	8026	8249	8473		8920			9589		
111	5			290480								
133	6						3363					
155	7	4466					5567		6007	6226		
178	8	6665										
200	9	8853	9071	9289	9507	9725	9943	300161	300378	300595	300813	21
0.1	200	301030	301247	301464	301681	301898	302114	302331	302547	302764	302980	217
21	1	3196	3412	3628	3844	4059	4275	4491	4706	4921	5136	216
42	2	5351	5566				6425			7068	7282	21
63	3		7710	7924	8137	8351	8564	8778	8991			
84	4		9843	310056	310268	310481	310693	310906	311118	311330	311542	219
105	5		311966	2177	2389	2600			3234	3445	3656	211
127	6	3867	4078	4289			4920		5340		5760	210
148	7	5970				6809	7018	7227	7436			209
169	8	8063			8689		9106	9314				208
190	9	320146	320354	320562	320769	320977	321184	321391	321598	321805	322012	201
	210	322219	322426	322633	322839	323046	323252	323458	323665	323871	324077	206
20	1	4282					5310			5926		
40	2			6745			7359	7563				
61	3				8991	9194	9398				330211	
81	4			330819			331427	331630	331832	2034		
101	5									4051	4253	
121	6		4655		5057		5458			6059	0.000	
141	7	6460	6660		7060		7459	7659	7858	8058		
162	8				9054		9451	9650			340246	
182				340841	341039	341237	341435	341699	341830	2028		
D	=	-	-	o rooti	9			J 1002		- 0	-	
	200								~	- 42	- (1	

3

P. P. N.

4		1	Table	of Log	arithms	of Nu	mbers f	rom 1 t	0 100,0	00.	-	
P. P.	N.	0	1	2	3	4	5	6	7	8	9	L
	550	342423	342620	342817	343014	343212	343409	343606	343802	343999	344196	1
19	1	4392	4589	4785	4981	5178	5374	5570	5766	5962	6157	1
39	2	6353	6549	6744	6939	7135	7330	7525	7720	7915	8110	
58	3	8305	8500	8694	8889	9083	9278	9472	9666	9860	350054	1
77	4	350248	350442	350636	350829	351023	351216	351410	351603	351796	1989	Œ
96	5	2183	2375	2568	2761	2954	3147	3339	3532	3724	3916	I
116	6	4108	4301	4493	4685	4876	5068	5260	5452	5643	5834	Œ
135	7	6026	6217	6408	6599	6790	6981	7172	7363	7554	7744	Œ
154	8		8125	8316		8696	8886	9076	9266	9456	9646	
174	9	9835	360025	360215	360404	360593	360783	360972	361161	361350	361539	Į
	230	361728	361917	362105	362294	362482	362671	362859	363048	363236	363424	ij
18	1	3612	3800	3988	4176		4551	4739	4926	5113		
37	2		5675	5862	6049	0.000	10000000	600000	6796	6983	100000000000000000000000000000000000000	
55	3		100000000000000000000000000000000000000	7729	7915	8101	8287	8473	8659	8845		
74	4	4 (4 (5 (5 (5 (5 (5 (5 (5 (5 (5 (5 (5 (5 (5		9587	9772						370883	
92			371253				1991	2175		2544		•
110	6		3096	3280	3464	3647	3831	4015	4198	4382		
129	7	-	17353000	5115	11-00-00-00-00-00-00-00-00-00-00-00-00-0	5481	5664		6029		4 0 2 3 3	
147	8		6759	6942	7124	7306	7488		7852	The second second	Decision in the last of the la	
166	9	1000000	8580	8761	8943	9124	9306		9668		380030	
100		0000	-		and the same of							
0.0		380211									381537	
18	1	2017	2197	2377	2557	2737	2917		3277	3456	The second second	
35	2	0010		4174	4353	1000		100000	5070	I LONG TO STATE OF	100000000000000000000000000000000000000	"
53	3		5785	5964	6142	6351	6499	10000000	6856	ALC: UNKNOWN	7212	ı
71	4	1000	7568	7746	7924	8101	8279		8634		8989	
88	5	9166	9343	9520	9698	9875	390051	390228	390405	390582	390759	Æ
106	6	390935	391112	391288	391464	391641	1817	1993	2169	2345	2521	Z
124	7	2697	2873	3048	3224	3400	3575	3751	3926	4101	4277	1
142	8	4452	4627	4802	4977	5152	5326	5501	5676			ï
159	9	6199	6374	6548	6722	6896	7071	7245	7419			F
	950	_	398114	398987	398461	398634	-	-	399154	Name of the last	Comment of the last	
17	1	9674	9847	400020	400199	400365	400538	400711	100889	401056	401228	Œ
34			401573	1745		2089						
51	3		3292				3978		4320		1 15 10 000	
68	4	100000000000000000000000000000000000000		5176			5688		6029	100000000		
85	5		the Edition	100000000000000000000000000000000000000	7051	7221	7391	7561	7731	10000000		
102	6	122000	100000	8579			10505	0000		7901	8070	
	7		8410	410001	410440		9087	9257	9426	9595	9764	ä
119											411451	
136	8			1956		2293	10000	2629	2796	200000000000000000000000000000000000000	100000000000000000000000000000000000000	
153	9	3300	3467	3635	3803	3970	4137	4305	4472	4639	4806	il.
	260	414973	415140	415307	415474	415641	415808	415974	416141	416308	416474	ĮĮ
16	1	6641	6807	6973	7139	7306	7472	7638	7804	7970	8135	¥
33	2	8301	8167	8633	8798				9460			
49	3	9956	420121	420286	120451			420945			421439	
66	4	421604		1933		2261	2426					
88	5	3246	1 2000	Mr. C. at 700	100.00.000		4065		4392			
98	6			5208		5534	0.000.00		6023	100000		
115	7	6511	6674	6836	17527	7161	7324	12000	7648	7811	7978	
131	8	10000	12220	8459	1 2222	8783	100000	1 135.00	9268	9429	9591	
148	9			430075	Duran Da	A COLOR	A SANTON AND AND AND					0
10	210		431525									
16	1	2969								757.000	The State of the S	
32	2		1000000	Transfer in			1000000					
47	3		100000000000000000000000000000000000000	6481	6640							
63	4		7909				8542		8859	9017	9175	۱
79	5			9648		9964	440122	440279			440752	I
95			441066			441538	1695	1852	2009	2166	2323	
111	7			2793	2950	3106	3263	3419	3576	3732	3889	
126	8	4045	4201	4357	4513		2000	4981	5137	5293	5449	
142	9		5760			6226			6692	6848	7003	
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106	788: 939: 46089: 46239: 589: 538: 686: 834: 982: 47129: 2756				6821	6973		7276	7428	7579	7731	
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137 9 290 15 1 290 29 2 44 3 59 4 73 5 88 6 103 7 118 8 83 6 132 9 300 14 1 128 2 43 3 57 4 77 1 5 6 85 6 10 3 11 8 128 9 7 1 14 8 128 9 14 1 28 2 41 3 55 5 4 6 69 5 83 6 69 7 7 110 8 8124 9 13 1 127 2 440 3 530 13 1 27 2 40 3 530 13 1 27 2 40 3 530 13 1 27 2 40 3 53 4 66 5 80 6 67 7 7 110 8 9 93 7 110 8 9 13 1 127 9 13 1 127 9 13 1 127 9 13 1 13 1 127 2 14 0 13 1 14 0 13 1 14 0 15 1 16 1 17 1 18 1 18 1 18 2 18 2 18 3 18 3 19 3 330	460899 462399 3893 5383 6869 8344 9823 471299 2756				9845						460748	
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93 7 106 8 120 9 330 13 1 26 2 39 3		5		2151	2284	2418	2551	2684	2818	2951	3084	
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13 1 26 2 39 3				4813	4946	5079	5211	5344	5476	5609	5741	1
330 13 1 26 2 39 3	587	8	6006	6139	6271	6403	6535	6668	6800	6932	7064	
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39 3			521269	1400		1661	1792			2183	2314	
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6			A Table	of Log	arithms	of Nu	mbers f	rom 1 t	0 100,0	000.		
P. P.	N.	0	1	2	3	4	5	6	7	8	9	D.
100	340	531479	531607	531734	531862	531990	532117	532245	532372	532500	532627	128
13	1/1					3264	3391	3518	3645		3899	
25	2	00000	Carrie la la	The San San San San	A COLUMN TO A COLU	4534	4661	4787	4914		5167	
38	3			1 2000		5800 7063	122000			6306 7567		
63	5	A PAGE	The Control of the	The second	6937 8197	8322	7189 8448		12220	1000000	7693 8951	
76	6	1000	1 10000		100000	9578	9703				540204	
88	7				540705						1454	
101	8		The second second			2078	2203				2701	12.
113	9	2825	2950	3074	3199	3323	3447	3571	3696	3820	3944	12
-	350	544068	544192	544316	514440	544564	544688	544812	544936		545183	12
12	1	1 000		5555		5802	5925	1000000			6419	
24	2	10000					7159				7652	
37	3	10000			8144	8267	8389				8881	
49	4					9494					550106	
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85	7		120000		3033	10000	3276					
98	8	1 1000	1 2222	12000	22.50	4368	4489	100000	2000	4852	4973	
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1	360		556423		The second second	556785				557267		
12	1	7507	7627			7988	8108				8589	
24	2	8709	8829	8948	9068	9188	9308	9428	9548		9787	
36	3		560026						560743	560863	560982	
48	4		1551	1340		1578	1698		1936			
59	5	10000000			2650	2769						
71 83	6 7		3600			3955 5139	4074 5257			4429 5612		200
95	8	4666 5848	W W C C C		10000	6320	6437	6555	(535)3	100,000	6909	
107	9			7262	7379	7497	7614				8084	
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12	1	9374	9491	9608		9842					570426	
23	2				570893				19 5009	10000000	1592	
35	3				2058	2174		2407	2523	2639	2755	
46	4	2872	2988	3104	3220	3336	3452	3568	3684		3915	116
58	5	4031	4147	4263		4494	4610			4957	5072	
70	6	5188	5303	5419		5650	5765				6226	
81	7	6341	6457	6572	6687	6802	6917	200,000	7147	2222	7377	
93	8 9	7492	7607	7722	7836	7951 9097	8066 9212		8295 9441	9555	8525 9669	
104	-	8639	8754	8868	8983					-	-	
11	1		579898 581039		580126		1495	1608	1722	1836	580811 1950	114
23	2	2063		1153 2291	1267 2404	1381 2518	2631	2745	2858	2972	3085	
34	3		3312	3426	3539	3652	3765	3879	3992	4105		
45	4	4331	4444	4557	4670	4783	4896	5009	5122		5348	
56	5	5461	5574	5686	5799	5912	6024	6137	6250	-2333444	6475	
68	6	6587	6700	6812	6925	7037	7149	7262	7374	7486	7599	112
79	7	7711	7823	7935	8047	8160	8272	8384	8496	8608	8720	
90	8	8832	8944	9056	9167	9279	9391	9503	9615	9126	9838	-
102	9										590953	113
	390	591065	591176	591287			591621	591732	591843		592066	111
11	1	2177		2399			2732	2843		3064	3175	
22	2			3508		3729	3840			4171	4282	
33	3	610000	4503 5606	4614 5717	4724	4834	4945 6047	5055 6157	5165 6267	5276 6377	5386 6487	
55	5		6707	6817		5937 7037	7146	7256	7366	7476	6487 7586	
66	6	7695	7805	7914	8024	8134	8243	8353	8462	8572	8681	
77	7	8791	8900	9009		9228	9337	9146	9556	9665	9774	
88	8										600864	
99	_	600973		1191	1299	1408	1517	1625	1734	1843	1951	
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21	2	3144 4226	2.00		3469		3686		3902	4010		
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43	4	5305	5413		5628	5736	5844	5951	6059	6166	6274	
53	5	6381	6489		6704	The second second second	6919	7026	7133		7348	
64	6	7455	7562		7777	7884		8098	8205	8312	8419	
75	7	8526	8633			8954	9061	9167	9274	9381	9488	107
86	8	9594	9701		9914	610021						
96	9				610979				1405		1617	
90	-	1723	1829		2042	2148	2254				2678	
. 7			612890	612996	613102	613207						
10	1	3842	3947							4686		
21	2	4897	5003						5634		5845	105
31	3	5950	6055			6370	6476	6581	6686	6790	6895	105
42	4	7000	7105	7210	7315	7420	7525	7629	7734	7839	7943	105
52	5	8048	8153		8362	8466	8571	8676	8780	8884	8989	105
63	6	9093	9198	9308	9406	9511	9615	9719	9824	9928	620032	104
73	7					620552	620656	620760	620864	620968	1072	104
84	8	1176	1280		1488	1592	1695				2110	
94	9	2214	2318		2525	2628	2732				3146	104
55	420	623249	623353	623456	623559	623663	623766	623869	623973	624076	624179	103
10	1	4282	4385	4488	4591	4695			5004		5210	
20	2	5312	5415	5518	5621	5724						
31	3	6340	6443						The state of the s			
41	4	7366	7468	7571	7673	7775	7878					
51	5	8389	8491	8593	8695	8797						
61	6	9410	9512							630224	630326	109
71	7	630428	630530			630835	630936	. 1038			1342	
88	8	1444	1545		1748	1849		2052				
98	9	2457	2559			2862			100000			10000
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10	1	4477	4578	4679	4779	4880	4981	5081	5182			
20	2	5484	5584	5685	5785	5886	5986		0.000			
30	3	6488	6588		6789	6889			6187	6287	6388	
40	4	7490	7590		7790	7890	100000000000000000000000000000000000000					
50	5	8489	8589			8888						
60	6	9486	9586	1						9287 640283	9387	100
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80	8	1474	1573			1871	1970		1177			
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10	1	4439	4537			6						
19	2	5422	5521	5619		5815		The second second	6110	10.000		
29	3	6404	6502				0.00	100		The second second	7285	
39	4	7383	7481	7579	7676				8067			
48	5	8360	8458	1777	8653						9237	
58	6	9335	9432	9530	9627	9724	9821	9919	650016	650113		
68		000308				650696						97
78	8	1278	1375		1569	1666						
87	9	2246	2343			2633					3116	97
	450	653213	653309	653405	653502	653598	653695	653791	653888	653984	654080	96
9	1	4177	4273	.4369	4465	4562	4658	4754				
19	2					5523						
28	3	6098			6386	6482						100
38	4	7056	7152		7343							1 3 3
47	5	8011	8107							8774		
57	6	8965	9060	9155	9250	9346	9441	9536	9631	9726	9821	95
66	7				660201	660296	660391	660486	660581	660676	660771	95
76	8	660865	0960	1055	1150	1245	1339	1434				
85	9	1813	1907	2002	2096	2191	2286					
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9 19 28 37 46 56 65 74 84 9 18 27 36 45 55	1 2 3 4 5 6 7	3701 4642 5581 6518	3795 4736		663041			_		_		
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56 65 74 84 9 18 27 36 45 55	6		1700000	7640	7733	7826	7920	8013	8106	8199	8293	
74 84 9 18 27 36 45 55	_	8386	8479	8572	8665	8759	8852	8945	9038	9131	9224	
9 18 27 36 45 55	8	9317	9410	9503	9596	9689	9782	, 9875	9967	670060	670153	93
9 18 27 36 45 55	_	670246	670339	670431	670524	670617		670802		0988	1080	
9 18 27 36 45 55	9	1173	1265	1358	1451	1543	1636	1728	1821	1913	2005	
18 27 36 45 55			THE RESERVE OF THE PERSON NAMED IN			The second second			The second second		672929	
27 36 45 55	1	3051	3113		3297	3390	3482	3574		3758	3850	
36 45 55	2	3942	4034	4126	4218	4310	4402	4494		4677	4769	
45 55	3 4	4861 5778	4953 5870	5045 5962	5137 6053	5228	5320	5412	5503 6419	5595 6511	5687 6602	
55	5	6694	6785	6876	6968	7059	6236 7151	6328 7242	7333	7424	7516	
	6	7607	7698	7789	7881	7972	8063	8154	8245	8336	8427	1000
	7	8518	8609	8700	8791	8882	8973	9064	10000	9246	9337	
73	8	9428	9519	9610	9700	9791	9882	9973			680245	
82	9	680336	680426	680517	680607	680698			0970	1060	1151	
	180	681241	681332	681422	681513	681603	681693	681784	681874	681964	682055	90
9	1	2145	2235	2326	2416	2506	2596		2777	2867	2957	
18	2	3047	3137	3227	3317	3407	3497	3587	3677	3767	3857	
27	3	3947	4037	4127	4217	4307	4396		4576	4666	4756	
36	4	4845	4935		5114	5204	5294		5473	5563	5652	90
45 54	5	5742 6636	5831 6726	5921	6904	120000	6189		6368 7261	6458 7351	6547 7440	89
63	7	7529	7618	6815	7796	6994 7886	7083	7172 8064		8242	8331	89
72	8	8420		8598	8687	8776	8865	200	10000	9131	9220	89
81	9	9309	9398	9486	9575	9664	9753			690019		89
- 4	490	690196	THE REAL PROPERTY.				-				690993	
9	1	1081	1170	1258	1347	1435	1524			1789	1877	Barrier .
18	2	1965	2053	2142	2230	2318	2406			2671	2759	
26	3	2847	2935	3023	3111	3199	3287	3375		3551	3639	88
35	4	3727	3815	3903	3991	4078	4166	2000		4430	4517	
44	5	4605	4693	4781	4868	4956	5044		5219	5307	5394	
53 62	6 7	5482	5569	5657	5744	5832	5919		6094	6182	6269	
70	8	6356 7229	6444 7317	6531 7404	6618 7491	6706 7578	6793 7665	6880 7752	6968 7839	7055 7926	7142 8014	87
79	9	8101	8188	8275	8362	8449	8535	8622	8709	8796	8883	
-	-	-	The second			THE REAL PROPERTY.	THE RESERVE OF THE PERSON NAMED IN			699664		87
9	1	9838									700617	87
17	2	4-12-5	700790		0963	1050	1136		1309	1395	1482	
26	3	1568	1654	1741	1827	1913	1999	2086		2258	2344	
34	4	2431	2517	2603	2689	2775	2861	2947	3033	3119	3205	
43	5	3291	3377	3463	3549	3635	3721	3807	3893	3979	4065	
52	6	4151	4236	10000	4408	4494	4579	4665		4837	4922	-
60	7 8	5008	5094	5179 6035	5265 6120	5350 6206		0000000		5693	5778	10000
77	9	5864 6718	5949 6803	725/903	6974		6291 7144	6376	6462 7315	6547 7400	6632 7485	
Street, or other Designation of the last o			1	707740				ST.	-	Name and Address of the Owner, where		
0	1	8421	8506		8676		8846		9015	708251 9100	708336	85
17	2										710033	
25				710287	710371	710456	710540	710625	710710	710794	0879	
34	4						1385				1723	
42	5	1807			2060		10000	122200	100000	2481	2566	
50	6						3070		10000000	3323	3407	84
59	7	3491			2000		100000000000000000000000000000000000000			100000	4246	
67	8	0.000	10000		-	4665	The second second	100000000000000000000000000000000000000	100000000000000000000000000000000000000	5000	5084	
76	9		5251	5335		5502	5586	5669	5753	5836	5920	84
P. P.	N.	0	1	2	3	4	5	6	7	8	9	D.

-	-		- Audio				mbers f					9
P. P.	N,	0 .	1	2	3	4	5	6	7	8	9	D.
	520	716003	716087	716170	716254	716337	716421	716504	716588	716671	716754	83
8	1	6838	6921	7004	7088	7171	7254	7338	7421	7504	7587	83
17	2	7671	7754	7837	7920	8003	8086	8169	8253	8336	8419	83
25	3	8502	8585	8668	8751	8834	8917	9000	9083	9165	9248	83
33	4	9331	9414	9497	9580	9663	9745	9828	9911	9994	720077	83
41	5	720159	720242	720325	720407	720490	720573	720655	720738	720821	0903	83
50	6	0986	1068	1151	1233	1316	1398	1481	1563	1646	1728	82
58	7	1811	1893	1975	2058	2140	2222	2305	2387	2469	2552	82
66	8	2634	2716	2798	2881	2963	3045	3127	3209	3291	3374	88
75	9	3456	3538	3620	3702	3784		3948	4030	4112	4194	
_	590	724276	_	724440	724522	724604		724767		724931	725013	_
8	1	5095	5176	5258	5340			5585		5748	5830	
16	2	5912	5993	6075	6156	20.00		6401	6483	6564	6646	
24	3	6727	6809	6890	6972	7053		7216	7297	7379	7460	
32	4	7541						8029	8110	8191	8273	
40	5	Charles A	7623	7704	7785	7866					1 2222	100
49	6	8354	8435	8516	8597	8678	8759	8841	8922 9732	9003	9084	
		9165	9246	9327	9408	9489	9570	9651		9813	9893	81
57	7		730055				730378				730702	81
65	8	730782	0863	0944	1024			1266		1428	1508	81
73	9	1589	1669	1750	1830	-	1991	2072	_	2233	2313	81
	540	732394	732474	732555	732635	732715	732796	732876	732956	733037	733117	80
8	1	3197	3278	3358	3438	3518	3598	3679	3759	3839	3919	80
16	2	3999	4079	4160	4240	4320	4400	4480	4560	4640	4720	80
24	3	4800	4880	4960	5040	5120	5200	5279	5359	5439		
32	4	5599	5679	5759	5838	5918		6078	6157			
40	5	6397	6476	6556	6635			6874				
48	6	7193	7272	7352	7431			7670				
56	7	7987	8067	8146	8225			8463		8622		75
64	8	8781	8860	8939	9018			9256		9414		75
72	9	9572	9651	9731	9810			740047			740284	75
••	_							-				-
	550	740363		740521	740600			740836		740994		75
8	1	1152	1230	1309	1388			1624			1860	75
16	2	1939	2018	2096	2175			2411	2489	2568		75
23	3	2725	2804	2882	2961	3039		3196				78
31	4	3510	3588	3667	3745			3980		4136	4215	78
39	5	4293	4371	4449	4528			4762		4919	4997	78
47	6	5075	5153		5309			5543	5621	5699	5777	78
55	7	5855	5933	6011	6089			6323	6401	6479	6556	78
62	8	6634	6712	6790	6868	6945	7023	7101	7179	7256	7334	78
70	9	7412	7489	7567	7645	7729	7800	7878	7956	8033	8110	
_	560	748188	748266	748343	748421	748498	748576	748659	748731	748909	748885	77
8	1	8963	9040		9195							
15	2	9736	9814	9891	0080	75004	750123	250900	750977	250954	9659	77
23	3		750586									77
31	4	1279	1356									77
38	5	2048	2125	1433 2202								
46	6	2816										
		100000000000000000000000000000000000000			Total Control							71
54 62	8	3583										7
		4348	4425		4578							76
69	9	5112	5189	_								76
		755875					756256	756332	756408	756484	756560	76
7	1	6636	6719	6788						7244		
15	2	7396	7472	7548	7624	The second second						
22	3	8155										
30	4											
37	5					9970	760045	760191	760196	760979	760347	7
45			760498			76079	0799	0875				
52	7					00						
60	8											
67	9											2
		2013	6104	4029	2304	2311	3003	3128	3203	3210	3333	16

7 15 22 30 37 44 52 59 67 7 15 22 29 36	N: 5800 1 2 3 4 5 6 6 7 8 9 5900 1 2 3 4 5 6 6	4176 4923 5669 6413 7156 7898 8638 9377 770115	4251 4998 5743 6487 7230 7972 8712 9451 770189 770926 1661 2395	6562	4400 5147 5892 6636 7379 8120 8860 9599 770336	4475 5221 5966 6710 7453 8194 8934 9673	4550 5296 6041 6785 7527 8268 9008	4624 5370 6115 6859 7601 8342	4699 5445 6190	4774 5520 6264 7007 7749 8490	5594 6338 7082 7823 8564	3
7 15 22 30 37 44 52 59 67 7 15 22 29 36	1 2 3 4 5 6 7 8 9 5 9 0 1 2 3 4 5 5	4176 4923 5669 6413 7156 7898 8638 9377 770115 770852 1587 2322 3055	4251 4998 5743 6487 7230 7972 8712 9451 770189 770926 1661 2395	4326 5072 5818 6562 7304 8046 8786 9525 770263	4400 5147 5892 6636 7379 8120 8860 9599 770336	4475 5221 5966 6710 7453 8194 8934 9673	4550 5296 6041 6785 7527 8268 9008	4624 5370 6115 6859 7601 8342	4699 5445 6190 6933 7675 8416	4774 5520 6264 7007 7749 8490	4848 5594 6338 7082 7823 8564	3
15 22 30 37 44 52 59 67 7 15 22 29 36	2 3 4 5 6 7 8 9 5 9 5 9 1 2 3 4 5 5	4923 5669 6413 7156 7898 8638 9377 770115 770852 1587 2322 3055	4998 5743 6487 7230 7972 8712 9451 770189 770926 1661 2395	5072 5818 6562 7304 8046 8786 9525 770263	5147 5892 6636 7379 8120 8860 9599 770336	5221 5966 6710 7453 8194 8934 9673	5296 6041 6785 7527 8268 9008	5370 6115 6859 7601 8342	5445 6190 6933 7675 8416	5520 6264 7007 7749 8490	5594 6338 7082 7823 8564	1
22 30 37 44 52 59 67 7 15 22 29 36	3 4 5 6 7 8 9 590 1 2 3 4 5	5669 6413 7156 7898 8638 9377 770115 770852 1587 2322 3055	5743 6487 7230 7972 8712 9451 770189 770926 1661 2395	5818 6562 7304 8046 8786 9525 770263	5892 6636 7379 8120 8860 9599 770336	5966 6710 7453 8194 8934 9673	6041 6785 7527 8268 9008	6115 6859 7601 8342	6190 6933 7675 8416	6264 7007 7749 8490	6338 7082 7823 8564	3
30 37 44 52 59 67 7 15 22 29 36	500 590 1 2 3 4 5	6413 7156 7898 8638 9377 770115 770852 1587 2322 3055	6487 7230 7972 8712 9451 770189 770926 1661 2395	6562 7304 8046 8786 9525 770263 770999	6636 7379 8120 8860 9599 770336	6710 7453 8194 8934 9673	6785 7527 8268 9008	6859 7601 8342	6933 7675 8416	7007 7749 8490	7082 7823 8564	
37 44 52 59 67 7 15 22 29 36	5 6 7 8 9 590 1 2 3 4 5	7156 7898 8638 9377 770115 770852 1587 2322 3055	7230 7972 8712 9451 770189 770926 1661 2395	7304 8046 8786 9525 770263 770999	7379 8120 8860 9599 770336	7453 8194 8934 9673	7527 8268 9008	7601 8342	7675 8416	7749 8490	7823 8564	400
44 52 59 67 7 15 22 29 36	6 7 8 9 590 1 2 3 4 5	7898 8638 9377 770115 770852 1587 2322 3055	7972 8712 9451 770189 770926 1661 2395	8046 8786 9525 770263 770999	8120 8860 9599 770336	8194 8934 9673	8268 9008	8342	8416	8490	8564	
52 59 67 7 15 22 29 36	7 8 9 590 1 2 3 4 5	8638 9377 770115 770852 1587 2322 3055	8712 9451 770189 770926 1661 2395	8786 9525 770263 770999	8860 9599 770336	8934 9673	9008					•
59 67 7 15 22 29 36	8 9 590 1 2 3 4 5	9377 770115 770852 1587 2322 3055	9451 770189 770926 1661 2395	9525 770263 770999	9599 770336	9673	100000000000000000000000000000000000000		9150	9230	9303	
67 7 15 22 29 36	590 1 2 3 4 5	770115 770852 1587 2322 3055	770189 770926 1661 2395	770263 770999	770336	100000000000000000000000000000000000000		10000000	9894		770042	
7 15 22 29 36	2 3 4 5	1587 2322 3055	1661 2395		271029	I I DEL	100000000000000000000000000000000000000			770705		
7 15 22 29 36	2 3 4 5	1587 2322 3055	1661 2395			771146	771220	771293	771367	771440	771514	i
22 29 36	3 4 5	2322 3055	2395		1808	1881	1955		2102			
29 36	5		The second second	2468	2542	2615	2688		2835			
36	5	3786	3128	3201	3274	3348	3421	3494	3567	3640	3713	
			3860	3933	4006	4079	4152	4225	4298	4371	4444	ч
	6	4517	4590	4663	4736	4809			5028	5100	The second second	
44		5246	5319	5392	5465	5538	5610		5756	11 12 2 2 2 2 2	5902	
51	7	5974	6047	6120	6193		6338	No. of Street, Street, or other	6483	100000000000000000000000000000000000000	6629	
58	8	6701	6774	6846	6919	6992	7064	7137	7209	12000	7354	
66	9	7427	7499	7572	7644	7717	7789	7862	7934	8006	8079	
	600	778151	778224		778368			Militaria	778658	100000000000000000000000000000000000000	Belleville State of the State o	
7	1	8874	8947	9019	9091	9163	9236	9308	9380	9452	9524	
14	2	9596	9669	9741	9813	9885				780173		
22	3	780317		780461				0749	0821	0893	0965	
29	4	1037	1109	1181	1253	1324	1396	1468	1540 2258	1612 2329	1684	
36	5	1755	1827 2544	1899	1971	2042	2114	2186	2974	3046	2401	ŀ
50	6	2473 3189	3260	2616 3332	2688 3403	2759 3475	2831 3546	2902 3618	3689	3761	3117	
58	8	3904	3975	4046	4118	4189	4261	4332	4403	4475	ACCRECATE VALUE	
65	9	4617	4689	4760	4831	4902	4974	5045	5116	5187	5259	
	_	785330	The second second							785899	785970	
7	1	6041	6112	6183	6254	6325	6396	6467	6538	6609	6680	
14	2	6751	6822	6893	6964	7035	7106	7177	7248	7319	7390	
21	3	7460	7531	7602	7673	7744	7815	7885	7956	8027	8098	
28	4	8168	8239	8310	8381	8451	8522	8593	8663	8734	8804	
35	5	8875	8946	9016	9087	9157	9228	9299	9369	9440	9510	
13	6	9581	9651	9722	9792	9863	9933		790074	790144		
50	7	790285	790356		790496	790567	790637	0707	0778	0848	0918	
57	8	0988	1059	1129	1199	1269	1340	1410	1480	1550	1620	ı
64	9	1691	1761	1831	1901	1971	2041	2111	2181	2252	2322	ı
6	520	792392	792462	792532	792602	792672	792742	792812	792882	792952	793022	i
7	1	3092	3162	3231	3301	3371	3441	3511	3581	3651	3721	E
14	2	3790	3860	3930	4000	4070	4139	4209	4279	4349	4418	E
21	3	4488	4558	4627	4697	4767	4836	4906	4976	5045	5115	
88	4	5185	5254	5324	5393	5463	5532	5602	5672	5741	5811	E
35	5	5880	5949	6019	6088	6158	6227	6297	6366	6436	6505	ľ
12	6	6574	6644	6713	6782	6852	6921	6990	7060	7129	7198	ľ
19	7	7268	7337	7406	7475	7545	7614	7683	7752	7821	7890	ľ
56	8	7960	8029	8098	8167 8858	8236 8927	8305 8996	8374	8443	8513 9203	8582	Š
STATE OF THE PERSON NAMED IN	100	8651	8720	8789	-	Mark Control	1	9065	9134	THE RESIDENCE	9272	4
7 6	30	199341	749409	799478	799517	799616	199685	799751	199823	799892	799961	4
7	1			800167					1100	1000	800648	-
14	3	0717	0786	0854	0923	0992	1061	1129	1198 1884	1966	1335	1
20	4	2089	2158	1541	1609	1678 2363	1747 2432	1815 2500	2568	2637	2021	-
34	5	2774	2842	2226	2295	3047	3116	3184	3252	3321	3389	-
200	6	3457	3525	3594	2979 3662	3730	3798	3867	3935	4003	4071	1
8	7	4139	4208	4276	4344	4412	4480	4548	4616	4685	4753	-
54	8	4821	4889	4957	5025	5093	5161	5229	5297	5365	5433	
31	9	5501	5569	5637	5705	5773	5841	5908	5976	6014		6
P. 1		0	1	2	3	4	5	6	7	8		L

P. P.	N.	0	1	2	1 3	4	5	6	7	8	9	D.
	640	806180	806248	806316	806384	806451	806519	806587	806655	806723	806790	68
7	1	6858	6926	6994	7061	7129	7197	7264	7332	7400	7467	68
13	2	7535	7603	7670	7738	7806	7873	7941	8008	8076	8143	68
20	3		8279	8346	8414	8481	8549	8616	8684	8751	8818	67
27	4	8886	8953	9021	9088	9156	9223	9290	9358	9425	9492	67
33	5	9560	9627	9694	9762	9829	9896	9964	810031	810098	810165	67
40	6	810233	810300	810367	810434	810501	810569	810636	0703	0770	0837	67
47	7	0904	0971	1039	1106	1173	1240	1307	1374	1441	1508	67
54	8	1575	1642	1709	1776	1843	1910	1977	2044	2111	2178	67
60	9	2245	2312	2379	2445	2512	2579	2646	2713	2780	2847	67
	650	812913	812980	813047	813114	813181	813247	813314	813381	813448	813514	67
-7	1	3581	3648	3714	3781	3848	3914	3981	4048	4114	4181	67
13	2	4248	4314	4381	4447	4514	4581	4647	4714	4780	4847	67
20	3	4913	4980	5046	5113	5179	5246	5312	5378	5445	5511	66
26	4	5578	5644	5711	5777	5843	5910	5976	6042	6109	6175	66
33	5	6241	6308	6374	6440	6506	6573	6639	6705	6771	6838	66
40	6	6904	6970	7036	7102	7169	7235	7301	7367	7433	7499	66
46	7	7565	7631	7698	7764	7830	7896	7962	8028	8094	8160	66
53	8	8226	8292	8358	8424	8490	8556	8622	8688	8754	8820	66
59	9	8885	8951	9017	9083	9149	9215	9281	9346	9412	9478	66
	660	819544	819610	819676	819741	819807	819873	819939	820004	820070	820136	66
6	1	820201	820267	820333	820399	820464	820530	820595	0661	0727	0792	66
13	2		0924	0989	1055	1120	1186	1251	1317	1382	1448	66
19	3		1579	1645	1710	1775	1841	1906	1972	2037	2103	65
26	4				2364	2430	2495					65
32	5			2952	3018	3083	3148	3213	3279	3344	3409	65
39	6	3474		3605	3670			3865	3930	3996	4061	65
45	7	4126		4256	4321	4386				4646		65
52	8	4776	4841	4906	4971	5036		5166	5231	5296	5361	65
58	9	5426	5491	5556	5621	5686	5751	5815	5880	5945	6010	65
1	670	826075	826140	826204	826269	826334	826399	826464	826528	826593	826658	65
6	1	6723	6787	6852		6981	7046	7111	7175			65
13	2	7369	7434	7499	7563	7628	7692	7757	7821	7886	7951	65

19 3 8015

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51 8

58 9 1870

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2 840 106 840 169 840 232 840 294 840 357 840 420 840 482 840 545 840 608

90 838849 838912 838975 839038 839101 839164 839227 839289 839352 839415

680 832509 832573 832637 832700 832764 832828 832892 832956 833020 833083

30268 8

30332 830396 8

30460 830525

8595 64

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2445 64

3721 64

4357 64

4993 64

6894 63

7525 63

5627 63

6261 63

8156 63

8786 63

0671 63

1297 63

2547 62

3170 62

4415 62

5036 62

9 D.

1922 63

9981 840043

12	E	1	Table	of Log	arithms	of Nu	nbers f	rom 1 t	0 100,0	00.		
P. P.	N.	0	1	2	3	4	5	6	7	8	9	D.
	700	845098	845160	845222	845284	845346	845408	845470	845532	845594	845656	62
6	1	5718	5780	5842	5904	5966	6028	6090	6151	6213	6275	
12	2	6337	6399	6461	6523	6585	6646	6708	6770	6832 7449	6894	
19 25	3	6955 7573	7017	7079 7696	7141	7202	7264 7881	7326 7943	7388 8004	8066	7511 8128	
31	5	8189	8251	8312	8374	8435	8497	8559	8620		8743	
37	6	8805	8866	8928	8989	9051	9112	9174		9297	9358	
43	7	9419	9481	9542	9604	9665	9726	9788	9849		9972	61
50 56	8 9										850585	
20		0646	0707	0769	0830	0891	0952	1014	100000		1197	
6	1	1870	851320 1931	1992	2053	2114	2175	2236	2297	2358	851809 2419	61
12	2	2480	2541	2602	2663	2724	2785	2846	0.200		3029	
18	3	3090	3150	3211	3272	3333	3394	3455			3637	61
24	4	3698	3759	3820		3941	4002	4063	14660	1 200	4245	
30	5	4306	4367	4428	4488	4549	4610	4670 5277	4731 5337	4792 5398	4852 5459	
43	7	4913 5519	4974 5580		5095 5701	5156 5761	5216 5822	5882	1000000		6064	III SED
49	8	6124			6306		6427	6487	(20)02	400000	6668	
55	9	6729	6789	6850	6910		7031	7091	7152		7272	
	720	857332	857393	857453	857513	857574	857634	857694			857875	60
6	1	7935	7995				8236		8357		8477	
12	2	8537	8597		8718	700 000 0000	8838	8898 9499			9078	60
24	3	9138 9739			2222	9379	9439	860098	860158	9619 860218	9679	60
30			860398			860578	0637	0697		0817	0877	60
36	6	0937	0996				10000	1295	1355	1415		60
4.2	7	1534	B. 100073	100000		1200000				5222	2072	60
48 54	8 9	2131	2191	2251	2310						2668	60
-	100	-			2906			and the second second		863799		59
6	1	3917	3977	4036							4452	
12	2	4511	4570			100000	11222	1000000	133000			
18	3	5104		1 5 5 5 5 5	1 10222	20072	5400			1 000000		1000
24	4	100000		1000000		1,000,000,000				100000	6228	
29	6	100000	1 0000000	1 2 3 3 5		1 10000	1 12 7000	-		100 000 000	150000	
41	7			2/2/2/2		0.0000		4 122	A COLUMN		7409 7998	
47	8	10000			100000	0355		2427	400000	1 (0)0000000	8586	
53	9	8644	8703	8762	8821	8879	8938			The second second		59
THE	740	869232	869290	869349	869408	869466	869525	869584	869642	869701	869760	
6	1	9818		9935							870345	
12	3		870462 1047			1000000		1339				
23	4	0.000		1690	2000					10000000	2098	
29	5	100000	1 100000		150100	1000000	1 2222	1 60 25	100000	1	2681	
35	6		1 12233	2855	2913	2979	3030			7000	3262	48
41	7		1 10000	10000						7070	1 27.50	
46 52	8	3902	77777	02707	100 100 100 100 100 100 100 100 100 100	100000					4424	1000
-00	750		-	The real Property lies		-					5003 875582	
6	1	5640										58
11	2	6218	-		1000000	THE RESIDENCE		200	12.000			58
17	3	6795	6853	6910	40.00		7083	7141	7199	7256	7314	38
23	4		The second second	200.00		1000000	1 2222	I TOWN ON A		10 0000	100 00 000	
28	6		4 4 4 4 4	72000	100000						8464	
40	6							12/2/20			9039 9612	
46	8	4 -10-10	1 1 2 2 2 2 2	10000	1			A STATE OF THE PARTY OF THE PAR	A DESCRIPTION OF THE PERSON NAMED IN		880185	
51			880299									
PP	N.	0	1	2	3	4	5	6	7	8	9	D.
	-											-

. P.	N.	0	A Table	2	3	4 1	5 1	6	7	8	9	I
=	_	880814			880985		_			_	_	-
6	1	1385	1442	1499	1556	1613	881099 1670	1727	1784	1841	1898	
11	2	1955	2012	2069	2126	2183	2240	2297	2354	2411	2468	
17	3	2525	2581	2638	2695	2752	2809	2866	2923	2980	3037	8
23	4	3093	3150	3207	3264	3321	3377	3434	3491	3548	3605	
28	5	3661	3718	3775	3832	3868	3945	4002	4059	4115	4172	
34	6	4229	4285	4342	4399	4455	4512	4569	4625	4682	4739	
40	7	4795	4852	4909	4965	5022	5078	5135	5192	5248	5305	
46	8	5361	5418	5474	5531	5587	5644	5700	5757	5813	5870	
51	9	5926	5983	6039	6096	6152	6209	6265	6321	6378	6434	
-	770	886491	886547	886604	886660	886716	886773	886829	886885	886942	886998	Ĩ.
	1	7054	7111	7167	7223	7280	7336	7392	7449	7505	7561	l
6	2	7617	7674	7730	7786	7842	7898	7955	8011	8067	8123	
17	3	8179	8236	8292	8348	8404	8460	8516	8573	8629	8685	
22	4	8741	8797	8853	8909	8965	9021	9077	9134	9190	9246	1
26	5	9302	9358	9414	9470	9526	9582	9638	9694	9750	9806	l
34	6	9862	9918	9974	890030	890086	890141	890197	890253		890365	1
		890421	890477		0589	0645	0700	0756	0812	0868	0924	
45	8	0980	1035	1091	1147	1203	1259	1314	1370	1426	1482	
50	9	1537	1593	1649	1705	1760	1816	1872	1928	1983	2039	1
	780	892095	892150	892206	892262	892317	892373	892429	892484	892540	892595	
6	1	2651	2707	2762	2818		2929	2985	3040		3151	
11	2	3207	3262	3318	3373	3429	3484	3540	3595	3651	3706	r
16	3	3762	3817	3873	3928	3984	4039	4094	4150	4205	4261	1
22	4	4316	4371	4427	4482	4538	4593	4648	4704	4759	4814	ô
27	5	4870	4925	4980		5091	5146	5201	5257	5312	5367	i
33	6	5423	5478	5533		5644	5699	5754	5809	5864		
38	7	5915	6030	6085		6195	6251	6306	6361	6416	6471	
44	8	6526	6581	6636		6747	6802	6857	6912	6967	7022	
49	9	7077	7132	7187	7242	7297	7352	7407	7462	7517	7572	
	790	897627	897682	897737	897792		897902	897957	898015	898067	898122	6
5	1	8176	8231	8286	8341	8396	8451	8506	8561	8615	8670	١,
11	2	8725	8780	8835	8890	8944	8999	9054	9109	9164	9218	
16	3	9273	9328	9383		9492	9547	9602	9656	9711	9766	
22	4	9821	9875	9930			900094					
27	5		900422			0586	0640	0695	0749	0804		
33	6	0913		1022	100000	1131	1186	1240	1295	1349	1404	
38	7	1458		1567	1622	1676	1731	1785	1840	1894	1948	
44	8	2003		2112		2221	2275	2329	2384	2438	2492	
49	9	2547		2655		2764		2873	2927	2981	3036	ν.
1			903144					903416				
5	1	3633		3741	3795		1	3958	4012	4066		
11	2	4174		4283		4391	4445	4499		100000000000000000000000000000000000000	4661	
16	3			4824			4986	5040	5094		5202	э.
22	4	5256		5364		5472	5526	5580	5634	5688	5749	
27	5	5796				6012	6066	6119	6173	6227	6281	
32 38	6	6335		6443 6981		6551 7089	6604 7143	6658 7196	6712 7250	6766 7304		
43	8	6874	7465		7035					7841	7895	ж
49	9			8056				8270	8324		8431	
20	-	-	-		-	-	-		20000		W-100-00	4
			908539									
.5	1											
11	2	9556	9610	9663	9716	9770	9823	9877		9984	910037	
16			910144									
21	4								22.47			
26	5											
32	6											
37	3											
48	8											
40	-	-	3337		3443	3490	3349				3101	1
P. P.	N.	10	1	2	3	4		6	7	8	9	

14		3	A Table	of Log	garithm	s of Nu	mbers	from 1	to 100,	000.		
P. P.	N.	0	1	2	3	4	5	6	7	8	9	1
10.7	820	913814	913867	913920	913973	914026	914079	914132	914184	914237	914290	1
5	1	4343	4396	4449	4502	4555	4608	4660	4713	4766	4819	
11	2				5030					5294		
16	3		1000000	100000000000000000000000000000000000000		5611	1000000	100000000000000000000000000000000000000	5769	5822	5875	
21	4	5927									6401	
26	5			6559	6612	6664	100000				6927	
32	6	1 FOITH			7138	7190					Laborator in	
37	7	7506	1 10000000	100000	7663	7716				100000	7978	
42	8	8030	120000	10,000	8188	8240	100000	DOM: N	2000	8450	8502	
48	9	8555		8659	8712	8764	8816		8921	8973	9026	98
	830										919549	
5	16.1	9601	9653	9706	9758	9810	9862				920071	
10	2	100000000000000000000000000000000000000	The second second	The second second	920280			The second second		0541	-0593	
16	3	0645	1 1000000000	0749	0801	0853	0906		1010	1062	1114	
21	4	1166		1270	1322	1374	1426		1530	1582	1634	
26	5	1686		1790	1842	1894	1946	1	2050	2102	2154	
31	6	2206		2310	2362	2414	2466		2570	2622	2674	
36	7	2725		2829	2881	2933	2985	95071070	3099	3140	3199	
42	8	3244	3296	3348	3399	3451	3503	10000000	3607	3658	3710	
47	9	3762	3814	3865	3917	3969	4021	4072	4124	4176	4228	47
1			924331								924744	•
5	1	4796	4848	4899	4951	5003	5054		5157	5209	5261	
10	2	5312	5364	5415	5467	5518	5570		5673	5725	5776	
15	3	5828	5879	5931	5982	6034	6085		6188	6240	6291	
20	4	6342	6394	6445	6497	6548	6600		6702	6754	6805	
25	5	685	6908	6959	7011	7062	7114		7216	7268	7319	1
31	6	7370	No.	7473	7524	7576	7627	7678	7730	7781	7832	ó
36	7	7883	7935	7986	8037	8088	8140	8191	8212	8293	8345	ā
41	8	8396	8147	8498	8549	8601	8652 9163	8703	8754	8805	8857	5
46	9		8959	9010	9061	9112			9266	9317	9368	2
15	Indiam'r		929470					929725			929879	4
5	1	9930			930083							E
10	_	930410		0542	0592	0643	0694	0745	0796	0817	0898	E
15	3	0949	1000	1051	1102	1153	1204	1254	1305	1356	1407	2
20	4	1458	1509	1560	1610	1661	1712 2220	1763 2271	1814 2322	1865 2372	1915	17.0
25	5	1966	2017	2068	2118	2169		The state of the s	100000000000000000000000000000000000000	The state of the s	2423	
31	6	2474	2524	2575	2626	2677	2727 3234	2778	2829	2879	2930	
36 41	7	2981 3487	3031	3082	3133 3639	3183 3690	3740	3285 3791	3335 3841	3386	3437	B
46	8	100000000000000000000000000000000000000	3538	3589	4145	4195	4246	4296	4347	4397	3943	
_	_	3993	4044	4094		Name and Address of the Owner, where the Owner, which is the Owner, which					4448	
					934650							200
5	1	5003	5054	5104	5154	5205	5255	5306	5356	5106	5457	å
10	2	5307	5558	5608	5658	5709	5759	5809	5960	5910	5960	8
15	3	6011	6061	6111	6162	6212	6262	6313	6363	6413	6463	5
20	4	6514	6564	6614	6665	6715	6765	6815	6865	6916	6966	5
25	5	7016	7066	7117	7167	7217	7267	7317	7367	7418	7468	3
30	6	7518	7568	7618	7668	7718 8219	7769	7819	7869	7919	7969	å
35	7	8019	8069	8119	8169	8720	8269	8320	8370	8420	8470	2
40	8	8520 9020	8570	8620	9170	9220	8770 9270	8820	8870	8920	8970	3
			9070	9120	-	And the latest the lat	A CONTRACTOR OF THE PARTY OF TH	9320	9369	9419	9469	-5
					939669			939819				5
5											940467	
10	2	0516	0566	0616	0666	0716	0765	0815	0865	0915	0964	
15	3	1014	1064	1114	1163	1213		1313	1362	1412		
20	14	1511	1561	1611	1660	1710	1760	20,00	1859	1909	1958	
25	ō	2008	2038	2107	2157	2207	2256	2306	2855	2405	2455	
30	6	2504	2554	2603	2653	2702	2752	2801	2851	2901		
35	7	3000	3049	3099	3148	3198	3247	3297	3346	3396		
40	8	3495	3544	3593	3643	3692	3742	3791	3841	3890	3939	
4.5	9	3989	4038	4088	4137	4186	4236	4285	4335	4384	4433	4
	N.1	0	1 1	2	3	-4	5	6	7 1	8	9	I

D	1 15	.0	Table 1	2	3	4	5	6	7	8	9	I
P. P.		_										=
-	880				944631				944828		944927	
5	1	4976	5025	5074	5124				5321	5370	5419	
10	2	5469	5518	5567	5616		5715			5862	5912	
15	3		6010	6059			6207	6256 6747	6305 6796	6354 6845	6403 6894	
20	4	6452	6501	6551	6600		6698		7287	7336	7385	
24	6	6943	6998	7041	7090		7189 7679	7238	7777	7826	7875	
29	7	7434	7483	7532		7630	8168	8217	8266	8315	8364	1
34	8	7924	7973	8022				8706	8755	8804	8853	
39 44	9	8413	8462 8951	8511 8999	9048	8609 9097	8657 9146	9195	9244	9292	9341	1
**		a financial backs										
	890	949390		949488	949536	949585	949634	949683	949731	949780	049829	
5	1	9878	9926	9975	950024						950316	
10	2			950462	0511	0560	0608		0706	0754	0803	
15	3	0851	0900			1046	1095	1143	1192	1240	1289	
20	4	1338	1386	1435			1580	1629	1677	1726	1775	
24	5	1823	1872	1920	1969	2017	2066	2114	2163	2211	2260	
29	6	2308	2356	2405	2453	2502	2550	2599	2647	2696	2744	1
34	.7	2792	2841	2889	2938	2986	3034	3083 3566	3131 3615	3180 3663	3228	ľ
39	8	3276	3325	3373	3421	3470	4001	4019			4194	
44		3760	3808	3856	3905	3953			4098	4146		١
50					954387		954484					
5	1	4725	4773	4821	4869		4966		5062	5110	5158	
10	2	5207	5255	5303		5399	5447	5495	5543		5640	
14	3	5688	5736	The section of			5928	5976	6024		6120	
19	4		6216				6409	6457	6505			т.
24	5	6649	6697	6745			6888	6936	6984		7080	
29	6	7128	7176				7368	7416	7464		7559	
34	7	7607	7655			7799	7847	7894	7942	7990	8038	
38	8	8086	8134	8181	8229	8277	8325	8373	8421	8468	8516	
43	9	8564	8612	8659		8755	8803	8850	8898	8946	8994	-
	910	959041			959185							1
5	1	9518	9566	9614	9661	9709	9757	9804	9852	9900	9947	
9	2										960423	
14	3	960471	0518	0566		100000000000000000000000000000000000000	0709	0756	0804		0899	
19	4	0946	0994	1041	1089	1136	1184	1231	1279	1326	1374	
23	5	1421	1469	1516	100000		1658	1706	1753	1801	1848	
28	6	1895	1943				2132	2180	2227	2275	5355	
33	7	2369	2417	2464		2559	2606	2653	2701	2748	2795	
38	8	2843	2890	2937	2985	3032	3079	3126	3174	3221	3268	
42	9	3316	3363	3410		3504	3559	3599	3646	3693	3741	1-
	920	963788	963835	963882	963929	963977	964024				964212	
5	1	4260	4307	4354		4448	4195	4542	4590	4637	4684	
9	2	4731	4778	4825		4919	4966	5013	5061	5108	5155	1
14	3	5202	5249	5296		5390	5437	5484	5531	5578	5625	
19	4	5672	5719	5766		5860	5907	5954	6001	6048	6095	
23	5	6142	6189	6236	6283	6329	6376	6423	6470	6517	6564	
28	6	6611	6658	6705		6799	6845	6892	6939	6986	7033	
33	-7	7080	7127	7173		7267	7314	7361	7408	7454	7501	1
38	8	7548	7595	7642	7688	7735	7782	7829	7875	7922	7969	
42	9	8016	8062	8109	8156	8203	8249	* 8296	8343	8390	8436	
	930	968183	968530	968576	968623	968670	968716	968763	968810	968856	968903	
5	1						9183		9276	9323		
9	2						9649			9789	9835	
14	3		0.000								970300	
18				970440					0672	0719	0765	
23	5					0997	1044	1090	1137	1183	1229	
28	6						1508			1647	1693	
32	7	1740					1971	2018	2064	2110	2157	
37	8			2295		2388	2434	2481	2527	2573	2619	1
41	9			2758			2897	2943	2989	3035	3082	14
. P.	_		1							8	9	1

16		1	Table	of Log	arithms	of Nu	mbers f	rom 1 t	o 100,0	00.		
P. P.	N.	0	1	2	3	4	5	6	7	8	9	D.
	940		THE RESERVE OF THE PERSON NAMED IN	THE RESERVE OF THE PERSON NAMED IN	INCOME AND DESCRIPTION OF	AND PROPERTY.				THE PERSON NAMED IN	973543	
5 9	2	3590 4051	3636 4097	3682 4143	3728 4189	3774 4235	3820 4281	3866 4327	3913	3959 4420	4005 4466	
14	3	4512	4558	4604	4650	4696	4749	4788	4834	4880	4926	
18	4	4972	5018	5064	5110	5156	5202	5248	5294	5340	5386	1000
23	5	5432 5891	5478 5937	5524 5933	5570 6029	5616 6075	5662 6121	5707 6167	5753 6212	5799 6258	5845 6304	
32	7	6350	6396	6442	6488	6533	6579	6625	6671	6717	6763	1000
37	8	6808	6854	6900	6946	6992	7037	7083	7129	7175	7220	46
41	9	7266	7312	7358	7403	7449	7495	7541	7586	7632	7678	
4	2000004			977815	977861 8317						978135	
9	2	8181 8637	8226 8683	8272 8728	8774	8363 8819	8409 8865	8454 8911	8500 8956		8591 9047	
13	3	9093	9138	9184	9230	9275	9321	9366	9412	9457	9503	
18	4	9548	9594	9639	9685	9730	9776	9821	9867	9912	9958	
22 27	6	980003 0458	980049 0503	980094 0549	980140 0594	980185 0640	980231 0685	980276	980322	980367 0821	980412	
31	7	0912	0957	1003	1048	1093	1139	1184	1229	1275	0867 1320	
36	8	1366	1411	1456	1501	1547	1592	1637	1683	1728	1773	
40	9	1819	1864	1909	1954	2000	2045	2090		2181	2226	
											982678	
4 9	2	2723 3175	2769 3220	2814 3265	2859 3310	2904 3356	2949 3401	2994 3446	3040	3085 3536	3130 3581	
13	3	3626	3671	3716	3762		3852	3897	3942	3987	4032	
18	4	4077	4122	4167	4212	4257	4302	4347	4392	4437	4482	
22	5	4527	4572	Branch Company	4662		4752	1000000	4842	4887	4932	
27	6	4977 5426	5022	5067 5516	5112 5561	5157 5606	5202 5651	5247 5696	5292 5741	5337 5786	5382 5830	45
36	8	5875			6010		6100	12223	Time and the	6234	2000	45
40	9	6324	6369	6413	6458	6503	6548	6593	6637	6682	6727	45
700			986817								987175	Delete C
4 9	1 2	7219 7666	100000000000000000000000000000000000000	7309 7756	7353 7800	7398 7845	7443 7890			7577	7622	
13	3	10000000	12000	8202	8247	8291	8336	10000	8425		8068 8514	
18	4	8559		8648	8693		8782	8826		8916	8960	
22	5	9005		9094	9138	9183	9227	9272	9316	9361	9405	
27	6	9450 9895	9494 9939		9583		9672	9717	9761	9806	9850 990294	
36	_		990383		0472	0516	0561	0605		0694	0738	
40	9	0783		0871	0916	1000000000	1004	1049		1137	1182	
187	980	991226	991270	991315	991359	991403					991625	44
4	1	1669		1 100 - 100	1802	1846				100000	100000	1000
9	3	2111	2156 2598	2642	2686	The state of the	2333 2774	100000	2421	2465 2907	2509 2951	
18	4	2995	100000			3172	3216			100000	3392	
22	5	3436			3568	3613		3701	3745	10000	3833	44
26	6	3877	3921	3965 4405	4009			4141	4185	1,000,000	4273	
31	7 8	4317	4361 4801	4845	4889	0.000	10000	1000000	5065	The second second	4713 5152	1100
40	9	5196	The first water		5328	5372	5416			5547	5591	
740	990										996030	
4	1	6074	10000	2000	20.00	100000				A CONTRACTOR	9 - 90	44
9	3										6906 7343	
18	4	100000				100000000000000000000000000000000000000	10000				7779	
22	5	7823	7867	7910	7954	7998	8041	8085	8129	8172	8216	
26	6	1			100000000000000000000000000000000000000				8564	The Control of the	8652	44
31	8									00,00	9087	
40	9		The second second								9957	
	1										The second second	

`**}**---

TABLE III.

THE ANGLES WHICH EVERY POINT AND QUARTER POINT OF THE COMPASS

MAKES WITH THE MERIDIAN.

No	rth	Points.	0 / //	Points.	Sou	th.
N. b. E.	N. b. W.	0 1 0 1 1 1 1 1 1	2 48 45 5 37 30 8 26 15 11 15 0 14 3 45 16 52 30 19 41 15	0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	S. b. E.	S. b. W.
N.N.B.	N.N.W.	1 2 2	22 30 0	2	S.S.E.	s.s.w.
N.E. b. N.	N.W. b. N.	2 2 2 3 3 3 3 3 3	25 18 45 28 7 30 30 56 15 33 45 0 36 33 45 39 22 30 42 11 15	112000000000000000000000000000000000000	S.E. b. S.	S.W. b. S.
N.E.	n.w.	4	45 0 0		S.E.	s.w.
N.E. b. E.	N.W. b. W.	444555556	47 48 45 50 37 30 53 26 15 56 15 0 59 3 45 61 52 30	44-55-55-56-6-14-15-14-15-14-15-14-15-14-15-14-15-14-15-14-15-14-15-14-15-14-15-14-15-14-15-14-15-14-15-14-15-14-15-14-15-15-15-15-15-15-15-15-15-15-15-15-15-	S.E. b. E.	S.W. b. W.
E.N.E.	w.n.w.	5 4 6	64 41 15 67 30 0	6	E.S.E.	w.s.w
E. b. N.	W. b. N.	6 1 6 2 7 1 7 1 7 1	70 18 45 73 7 30 75 56 15 78 45 0 81 33 45 84 22 30 87 11 15	6 6 6 7 7 1 1 7 7 7 7 7 7 7 7 7 7 7 7 7	E. b. S.	W. b. S.
East.	West.	7 2 8	90 0 0	8	East.	West.

TABLE IV.

LOGARITHMIC SINES, TANGENTS, AND SECANTS, TO EVERY POINT AND QUARTER POINT OF THE COMPASS.

Points.	Sine.	Cosine.	Tangent.	Cotang.	Secant.	Cosec.	Points.
0	0.000000	10.000000	0.000000	Infinite.	10.000000	Infinite.	8
0 4	8.690796	9.999477	8.691319	11.308681	10.000523	11.309204	7 4
0 1	8.991302	9.997904	8.993398	11.006602	10,002096	11.008698	7 1
0 4	9.166520	9.995274	9.171247	10.828753	10.004726	10.833480	7
1	9.290236	9.991574	9.298662	10.701338	10.008426	10.709764	7
1 1	9,385571	9.986786	9.398785	10.601215	10.013214	10.614429	6 3
1 4	9.462824	9.980885	9.481939	10.518061	10.019115	10.537176	6 1
1 3	9.527488	9.973841	9.553647	10.446353	10.026159	10.472512	6 1
2	9.582840	9.965615	9.617224	10.382776	10.034385	10.417160	6
2 1	9.630992	9.956163	9.674829	10.325171	10.043837	10.369008	5 1
2 1	9.673387	9.945430	9.727957	10.272043	10.054570	10.326613	
2 4	9.711050	9.933350	9.777700	10.222300	10.066650	10.288950	5 1
3	9.744739	9.919846	9.824893	10.175107	10.080154	10.255261	5
3 1	9.775027	9.904828	9.870199	10.129801	10.095172	10.224973	4 3
3 1	9.802359	9.888185	9.914173	10.085827	10.111815	10.197641	4 1
3 4	9.827084	9.869790	9.957295	10.042705	10.130210	10.172916	4 1
4	9.849485	9.849485	10.000000	10.000000	10.150515	10.150515	4
	Cosine.	Sine.	Cotang.	Tangent.	Cosec.	Secant.	1

1	8		TABLE	The state of the s	Logarit	hmic Si	ines, Tang	ents,					I
m.	8.	1	0 Ho	ur,	Tang.	D. S. T.	Cotang.	Sécant	D.	Degree.	1	m.	1
O	0	=	0.000000		0.000000	LA DE A	Infinite.	10.000000	=	10.000000	50	-	0
ľ	4			13.536274		501717		000000	00	000000		30	50
п	8				200000	293484	The state of the s	000000	00	000000			52
п	12					208231	059153	000000	00	000000		-	48
п	20	5			Market State of the Control of the C	131969	THE RESERVE OF THE PARTY OF THE	000000	00	000000	DOM:		40
ш	24	6		758123		111577		000001	01	9.999999		2	36
п	28	7 8	308824 366816	691176 633184	308825 366817	99653 85254	The second second	000001	01	999999	Total Control		90
п	36	9	417968		Principle of the last	The second second	THE PERSON	000001	01	999999	District of		28 24
п	40	10	463725	536275	- P. C. C. C. C.	68988	200000000	000002	01	999998	100		20
	44		505118 542906	494882 457094	505120 542909	62981 57934	1 1000000000	000002	01	999998 999997		3	16
ш		13		422332	577672	53642	700000	000003	01	999997	1000	и	8
	56	14	609853	390147	609857	49939	390143	000004	01	999996	46		4
1				12.360184	7.639820	The state of the state of	12.360180	10.000004	01	9.999996	1000	59	0
п	_	16 17	667845 694173	332156 305827	667849 694179	43882		000005	01	999995		78	56
	12		718997	281003	719003			000006	01	999995 999994	200.0		45
1	16	19	742477	257523	742484	37128	257516	000007	01	999993	41	4 3	52 48 44 40 36 32 28 24 20
			764754	235246	764761	35136		000007	01	999993	-	3	40
	24	21	785943 806146	214057 193854	785951 806155	33673 32176		000008	01	999992 999991	39		30
ш		23	825451	174549	825460		12222	000010	01	999990		1	28
п		24	843934	156066	843944			000011	02	999989			Z
ш	_	25 26	861662 878695	138338 121305	861674 878708		\$1900 CONTRACTOR	000012	02	999988 999988	35		16
	_	27	895085	104915	895099	100.0000	- THE RESERVE THE PARTY NAMED IN COLUMN TWO IS NOT THE PARTY NAMED IN COLUMN TWO IS N	000012	10000	999987	33		12
		28	910879	089121	910894	2000	100000	000014	02	999986	32		8
	56		926119	073881	926134	STATE OF THE PERSON NAMED IN	THE RESERVE OF THE PERSON NAMED IN	000015	05	999985	31		L
2		30	7.940842 955082	12.059158 044918	7.940858 955100		12.059142 044900	000017	02	9.999983 999982	100		0
ii.		32	968870	031130	968889	100000000000000000000000000000000000000		000019	02	999981	29		56 52 18 14 10 36 38
ш	12	33	982233	017767	982253		555555	000020	02	999980		ĸ	8
ш	16		995198	004802 11.992213	995219	20982	THE COMPOSITION	000021	02	999979	26	w	*
п		36	020021	979979	020045	20391 19832		000023	02	999977 999976	24		ŧ
100	28	37	031919	968081	031945		550000	000025		999975	23		Ö
ш	32		043501	956499	043527	18802	100 To 10	000027	02	999973	22	.	ā
ш		39 40	054781 065776	945219 934224	054809 065806	18326 17873	THE RESERVE TO SERVE	000028	02	999972 999971	-		÷
100	44	41	076500	923500	076531	17443		000031	02	999969		æ	16
п		42	086965	913035	086997	17033		000032	02	999968	-	æ	2
ш	56		097183 107167	902817 892833	097217	16640 16267	902783 892797	000034 000036	02	999966 999964			H
3	-	_		11.883074		Elizabeth field	11.883037		03	9.999963		57	C
1	-	46	126471	873529	126510	15567	873490	000039	03	999961			6
		47	135810	864190	135851	15240	864149	000041	03	999959		1	9100
1	12	48	144953 153907	855047 846093	144996 153952	14926	855004 846048	000042	03	999958 999956	801		ñ
16	20		162681	837319		14334	10000000	000044		999954	_		N
	24	51	171280	828720	171328	14056	828672	000048	03	999952	9	1 3	16
	28 32		179713 187985		179763	13788 13530	820237 811964	000050		999950	8	1	E
11	36	54	196102	812015 803898	188036 196156	13282	803844	000052 000054		999948 999946	6	1	ñ
1	40		204070	795930	201126	13043	795874	000056	03	999944	5	1	0
	44		211895		211953	12812	788047	000058		999942	4	1	6
	48		219581 227134	780419 772866	219641 227195	12509 12374	780359 772805	000060		999940 999938	3 2		9
1	56		234557	765443	234621	12166	765379	000064		999936	1		60004060040
4	=	60	241855	758145	241921	11965	758079	000066	04	999934	0 5	6	0
m	8.		Cosine.	Secant.	Cotang.	THE REAL PROPERTY.	Tang.	Cosec.		Sine.	1 1	n.	Ē
		-	5 Ho		100,000	or	_			egrees.			
P. 1		0/		3560	Is I	15"	3560	14	15"	0	P. 1	P. te	اه
8 0	r "	1	3 30		3	30 45	10681	3 3	45	101		or "	
		-	- 30	10000		_	-	-	-		-	-	4

						and Se	cants.		TA	BLE V.		19
		_	Q Ho	ur,		or			1 De	gree.		
n.	8.	7	Sine.	Cosec.	Tang.	D. S. T.	Cotang.	Secant.	D.	Cosine.	' m	. :
4	0	7	8.241835	11.758145	8.241921	11965	11.768079	10.000066	01	9.9999316	05	-:== 6
•	4	ĭ	249033		249102		750898	000068	04	999938 5		5
	8	2	256094		256165		743835	000071	04	9999295		5
	12	3	263042	736958	263115		736885	000073	04	999927 5	7	4
	16	4	269881	730119	269956		730044	000075	04	999925	6	4
	20	5	276614	723386	276691	11052	723309	000078	04	999922	5	4
	24	6	283243	716757	283323	10885	716677	000080		999920/3	4	3
	28	7	2 89773	710227	289856	10724	710144	000088	01	999918.5	3;	3
	32	8	296 207	703793	296292	10568	703708			999915 5		2
	36	9	302546	697454	302634	10416	697366			999913.5		2
		10	308794				691116			9999105		2
		11	314954				684954			999907		1
	48		321027		321122		678878			999905		1
	52		327016	1			67 288 6	000098		999902'4		
	56	14	332924	667076	383025	9716	666975	000101	05	999899	1-	
8	0	15	8.338753	11.661247	8.338856	9588	11.661144	10.000103	05	9.999897	5 5	Ĵ
	4	16	344504	655496	344610	9463	655390	000106	05	999894	11	
		17	3 50181	649819	350289	9340	649711	000109	05	999891 4		å
	12	18	355783	644217	355895	9222	644105	000112	05	999888		4
	16		36 131 <i>5</i>	638685	361430	9106	638570	000115	05	999885		4
	20		366777				633105			999882		4
	24		372171				627708			999879		:
	28		377499				622378			999876		:
	32		382762				617111	000127		999873		:
	36						611908			999870		:
	40						606766			999867		:
	44		398179				601685			999864 999861		
		27	403199				596662					
	52		408161				591696			999858		
	56	_	413068			I	586787	000146		999851		
6				11.582081				10.000149		9.999851		
		31	422717				577131	000152		999848		
		35	427462				572382			999844		•
	12		432156				567685			999841		•
	16		436800				563038			999838		•
	20 24		441394				558440			999834		;
	28		445941 450440	1			553890 549387			999827		
	32						544930			999823		
	36 36						540519			999820		
		40								999816		
		41					531828			999812		
		42					527546		1	999809		
		43					523301			999805		
		44				1	519108			999801		
7				11.515158				10.000203		9.999797		E-12
•		46					4 .			999793		,,
		47					510830			999790		
		48								999786		
		49								1		
		50									in	
		51										
l		52										
		53										
		54										
l		55									5	
		56										
		51										
Ī		58										
Ì		59									1	
8		60								l	0	52
=		=		Secant.	Cotang.		-		-	Sine.	7	== m.
m.	. 8	1	1 0000000		I couring.		Tang.	Cosec.	<u> </u>	egrees.	لـــا	• • • • • • • • • • • • • • • • • • • •
_				ours, 15" 1200	1.	15//			אָל <u>ו פ</u> ייל <i>ו</i>	~	_	
P	P. P. 5 or	to		15" 1200 30 2400	2 2	15" 30	1200	1, J.	30		1	7.5 8
			1 45 1	: £1:UU	- E		24(N)					

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18	-	TABLE	v.	Logarit	hmic Si	nes, Tang	ents,		
		0 Но			. 0		-	_	Degree
m. s.	-	Sine.	Cosec.	Tang.	D. S. T.	Cotang.	Sécant.	D.	Cos
0 0		0.000000	Infinite.	0.000000		Infinite.	10.000000	-	10.00
8	1 2	764756	13.536274 235244	200000000000000000000000000000000000000		13.536274 235244	000000	00	00
12	3	940847	059153		208231	059153	000000	00	00
16		7.065786				12.934214	000000	00	00
20	5	162696	837304		131969	837304	000000	100	00
24	6	241877 308824	758123 691176	100000000000000000000000000000000000000	111577 99653	758122 691175	000001	01	9.99
32	8	366816	633184	THE RESERVE AND ADDRESS.	85254	633183	000001	01	99
36	9	417968	582032	The second second		582030	000001	01	99
40		463725	536275 494882	1 4 7 7 7 7 7 7 7	68988 62981	536273 494880	000002	01	99
44	11	505118 542906	457094	542909	57934	457091	000002	10000	99
52		577668	422332	The state of the s	53642	422328	000003		99
56	14	609853	390147	609857	49939	390143	000004	01	99
		The second second	12.360184				10.000004	01	9.99
0.00	16 17	667845	332156 305827	667849 694179	43882	332151	000005	01	99
12	10000	694173	281003		41373 39136	305821 280997	000005 000006	0.00	99
	19	742477	257523	7.000.7000	37128	257516	000007	01	99
20	200	764754	235246	7 (00) 2, 5 (07) 24	35136	235239	000007	01	99
1000	21	785943	214057		33673	The second second	000008	01	99
32	22	806146 825451	193854 174549		32176	193845 174540	000009	01	99
36		843934	156066	The same of the last	DESCRIPTION OF THE PERSON OF T	156056	000011	02	99
40	25	861662	138338			138326	000012	02	99
200	26	878695	121305	100000	27318	121292	000012	02	99
	27	895085 910879	104915 089121	895099 910894	26324 25400	104901 089106	000013	02	99
	29	926119	073881	926134	24539	073866	000015	02	99
	30	7.940842	12.059158	7.940858	23734	12.059142	10.000017	02	9.99
. 4	31	955082	044918	955100	22981	044900	000018	02	99
	32	968870	031130	968889	200000	031111	000019	02	99
-	33	982233 995198	017767	982253 995219	21609 20982	017747 004781	000020	02	99
-	100	CONTRACTOR OF THE PARTY.	11.992213		100000000000000000000000000000000000000	11.992191	000023		99
24		020021	979979	Commence of the second	The state of the	979955	000024	02	91
	37	031919	968081	031945	19304	968055	000025	02	99
32	38	043501	956499 945219	100000000000000000000000000000000000000	18802 18326	956473 945191	000027 000028	02	99
40		065776	934224	065806	17873	934194	000029	02	99
44		076500	923500	076531	17443	923469	000031	02	99
48		086965	913035		17033	913003	000032	02	99
52		097183 107167	902817 892833	097217 107202	16640 16267	902783 892797	000034 000036	02	99
		and the second	11.883074			11.883037		03	9.99
	46	126471	873529	126510		873490	000039	03	99
8	47	135810	864190	135851	15240	864149	000041	03	99
	48	144953	855047	144996	14926	855004	000042	Berlei II	99
16	49	153907 162681	846093 837319		14624		000044		99
24		171280	828720		14056	828672	000048		99
28		179713	820287	179763	13788	820237	000050	03	99
32		187985	812015		13530	811964	000052	03	99
36		196102 204070	803898 795930		13282	803844 795874	000054 000056	03	99
44	200	211895	788105		12812	788047	000058	04	99
48		219581	780419	219641	12509	780359	000060	04	99
52		227134	772866	STATE OF THE PARTY OF	12374	772805	000062	04	99
86	59	234557 241855	765443 758145		12166 11965	765379 758079	000064 000066	04	99
		-			11900			-	99
		5 Ho	Secant	Cotang.	Hale.	Tang.	Cosec.	0.0	Sin
			o" 3560	10	15"	3560 (15"	cgrees
			Street, Square, Square	-			200		
		30	7120	2	30	1150	5/	30	1

		- 5	and Se	cants.		TAB	11 V.	19
Quito	dt,		br	19 2		1 Des	Tree.	
Sec.	Cosec.	Thing.	D.S.T.	Cotang.	Secant.	-	(wine.	° ga •
11855	11.758145	_	-	11.789079	-		99994 55	
49033	750967	249109		750499	DOINGS		99993	
56094	743906	256165		143435			95491211	
63042	736958	263113	11400	734445				4-
69881	730119	269956	11223	730014	CHRRISTS	04		2: 4:
76614	723386	276691		723309	OHHHIT -	64	All as	35 34
53243	716757	283323		716677	(4HHmi)	(1)	9999:	14
59773	710227	289956		710114	(Anno)	HE.	99991=	
96207	703793	296292				118		12 37
02546 08794	697454	302634		697366	(איא)ט~;			21 21
14954	691206 685046	309994	10264		and the state of the state of			
21021	675973	315046		681934	100000000000000000000000000000000000000		Griffing 7	
27016	672984	327114			(DINKIN)		000000	
32924	667076	383025	9715	666975		113	garan-2	
	11.661247	9.338H46						
44304	653496	344610	9385		10,000103		909-97	and the second second
0181	649819	350289	9340		Control		900-91	
55783	644217	355895	9222				bidger	
5131 5	638685	361430	9106					
66777	633223	366895	5993	633103	(mull-			
78171	627829	377297	P983	6277114	(80121		200	10
77459	622501	371622	×775	622374	000121		Million .	*
82762	617238	382889	5670	617111	0.00152	115	mine.	17
187962		388092	5367	611904	000130	11%	911447	
393101	6009899	393234	5467	606766	Oca)1.73	43	inition.	
399175	601821	398315	5369		000136	15		51
03199	. 596501	403339	×274	596662	O(4)136			y
13068	391839	408304	5180	591696			999= }=	
military in	586932	413213	8099	546747	(840) 16	-		11
17919		8.4F9068		11.5-19 12	70.000 (0.000 0.000			St of 2
2717 27462	577293	422809	7912	577131	000125		trisin !-	
32156	572536 561644	427618 432315	7826	172392	000136		Goden !!	
36900	563200	436962	7743 7660	567643 563038			Odne!	
41394	358606	441560	7590	556 140	(MA)199		991-11	
45941	554039	446110	7502		(00)[60.		999-53	
150440	549360	450613	7425		0.0173		gane :	
454893	545107	455070	7349				40042	
459301	540699	459481	7276	540519			0004	
463665	536335	463849	7203	536151	(while4	10,	44041	21.
467985		468172	7132	531428	0001==	14	govel:	1.
672263		472454	7063	527546	United	111	agen o	
476498		476693	6995	523307		101	General,	
488693		480892	6924	519109	tention	1-11	ann I	1
	8 11.515152	8.485050	6862		10.000203	07. 9	4997-17	1:00
48890		489170	6798	I CONTRACTOR OF		17	F116.1.1	
49301	100	493250	6735	506750			uen	
50109		497293	6673	502707				12 4
50504	A SERVICE AND	501298 505267	6612	49-702			9447-1	
30897	17 20.000	500900	6552	494733			040114	
51286	AT MARKET	513099	6435	486902			69.774	5 9
5167	483974	516961	6379	483039			946763	
15	519149	520790	6323	479210			604:-1	
13	43 415657			475414			994757	9 2
	102 ST1898	529349	6215	471651			099753	1 1
	828 MINTS	532080	6162	467920	A CONTRACTOR OF THE PARTY OF TH		66571-	
	523 MU	435779	6110	464221		. 71	666:44	2
	186 46085 2819 45118	589447	6059	460553	then fine		0.9:1	3
_		543084	6008	456916	100.25	71	69973.	29
' Cos	THE RESERVE	Cotang.		Tang.	Tires .	== =	Size. L	_3
4	5 Hours,	ang,		rang.		Degre		1
W 1000		All lines	or		7.7	The Park		- 400

TO BERRY

-	3		TABLE		Logariu	ALCOHOL: NAME OF TAXABLE PARTY.	nes, Tang	CH 603	0.	Dames		
4	-	,	O Ho	Cosec.	Tang.	D. S. T.		Sécant.	D.	Cosine.	-	m.
n.	8.					17. 5. 1.			=			
0	0		0.000000	Infinite.	0.000000	501717	Infinite. 13.536274	000000	00	10.000000	100	60
	8	2		235244	764756		235244	000000	00	000000		8
	12	3		059153	940847		059153	000000	00	000000	100	8
	16						12.934214	000000	00	000000	100	*
	20	5		837304		131969	837304	000000	00	000000	_	8
	21	6	241877	758123	241878	111577	758122	000001	01	9.999999	54	•
	28	7	308824	691176	308825	99653	691175	000001	01	999999	53	•
	32	8	366816	633184	366817	85254	633183	000001	01	999999		•
	36	9	417968	582032	417970		582030	000001	01	999999	200	
	40			536275	463727	68988	536273	000002	01	999998		77
	44	11	505118	494882	505120		494880	000005	01	999998	-	16
	48		542906	457094	542909	57934	457091	000003		999997		
	52			422332 390147	577672	53642	422328 390143	000003	01	999997	1	
	56		609853		609857	49939		000004	Bridge St.	999996	-	-
1				12.360184				10.000004	01	9.999996		59
	- 4	16	667845	332156 305827	667849	43882	332151	000005	01	999995	1000	
	_	17	694173	281003	694179 719003	41373	305821 280997	000005		999995		
	12 16		718997	257523	742484	39136 37128	257516	000006 000007	01	999994		
	20		764754	235246	764761	35136	235239	000007	01	999993		
	24		785943	214057	785951	33673		000008		999999		
	28		806146	193854	806155		193845	000009		999991		
		23	825451	174549	825460		174540	000010		999990		ж
	36		843934	156066	843944	29548	156056	000011	02	999989		я
	40		861662	138338	861674	28389	138326	000012	02	999988	35	
	44	26	878695	121305	878708	27318	121292	000012	02	999988	34	
		27	895085	104915	895099	26324	104901	000013	02	999987	33	
	52		910879	089121	910894	25400	089106	000014	02	999986		
	56		926119	073881	926134	24539	073866	000015	05	999985	31	
2				12.059158			12.059142		02	9.999983	30	58
		31	955082	044918	955100	100000000000000000000000000000000000000	044900	000018	02	999982	29	
		32	968870	031130	968889	The second second	200000000000000000000000000000000000000	000019	02	999981		
	12			017767	982253	The second second	4 10 CO CV 200	000020	02	999980		
	16		995198	004802 11.992213	995219		004781 11.992191	000021	02	999979		
	20		020021	979979	020045	14 14 M 40 40 C	979955	000023 000024	02	999977 999976		
		37	031919	968081	031945	10 to 10 to 10 to	968055	000024	02	999975		я
	32			956499	043527	18802	956473	000027	02	999973		•
	36		054781	945219	054809	18326	945191	000028	02	999972		
	40		065776	934224	065806	The second second	10000000	000029	02	999971	20	
		41	076500	923500	076531	17443		000031	02	999969	19	я
	48	42	086965	913035	086997	17033	913003	000032	02	999968		
	52	43	097183	902817	097217	16640	902783	000034	02	999966	17	
	56		107167	892833	107202	16267	892797	000036	03	999964	16	
3	0	45	8.116926	11.883074	8.116963	15909	11.883037	10.000037	03	9.999963	15	57
1	4	46	126471	873529	126510	15567	873490	000039	03	999961		
	8	47	135810	864190	135851	15240	864149	000041	03	999959		
	12		144953	855047	144996	14926	855004	000042	03	999958	-	
	16		153907	846093	and the second second	14624	846048	000044	03	999956		
	20	100	162681	837319	162727	14334	837273	000046	03	999954	100	
	24			828720	The second second	19799		000048		999952		
	28			820287 812015	179763 188036		820237 811964	000050		999950 999948		
	36			803898	196156		803844	000054		999946	7 6	
	40			795930	204126	Eller Control of the	795874	000056		999944		
		56		788105	211953	12812	788047	000058		999942	à	
	48	BOOM	200000000	780419	219641	12509	780359	000060		999940	3	
		58		772866		The second second	772805	000062		999938	3 2	
	56	59	234557	765443	234621	1	5979	000064	04	999936	1	
4	0	60	241855	758145	241921		79	000066	04	999934	0	56
-		=	Cosine.	Secant.	Cotan		=	Cosec.		Sine.	=	n.
			- The state of the		Cotali		-	The second second	O.D	The second second	100	-
			5 Ho		-		-		15'	egrees.	-	
			THE REAL PROPERTY.		10		10		10		P.	P. 1
			2 / 30	7120			U	2				or "

		-		-	and	Seca	nts.		TA	BLE V.	Ξ	2
		0 Ho	ur,		_	or		- 1	De	grees.	=	J.S.
3.	1	Sine.	D.	Cosec.	Tang.	D.	Cotang.	Secant.	D.	Cosine.	1	m.
0	0	8 040906	9403	11.059704	8.941952	9491	11.058048	10.001656	19	9.998344	60	10
4	ĭ	941738					056596	001667		998333		N.
- 8	2	943174		056826	2000		055148	001678	19	998322	58	11.3
12	9	944606		055394		2397	053705			998311		
16	4	946034		053966			052266			998300		
20	5	947456		052544			050832		19	998289		
24	6	948874		051126		12000	049403			998277 998266		
28	7 8	950287					047979 046559			998255		1
32	9	951696 953100		048304 046900	The second second		045144	100 000 000	V 20	998243		
	10	954499			Christian Street, Stre		043733		1000	998232		200
	11	955894		044106			042326	001780		998220		
	12	957284			11 to 10 to 12 to		040925			998209		late:
	13	958670			960473		039527	001803		998197		
56	14	960052					038134	001814		998186		
1 0	15	8.961429	2288	11.038571	8.963255	2307	11.036745	10.001826				
4	16	962801	2280	037199	964639	2300	035361	001837		998163		
	17	964170					033981	001849		998151		
12		965534					032606	and the second	50	998139 998128		1
16		966893					031234 029867			998116		10
24		968249					028504	The second second second		998104		
28		970947					027145			998092		
32	23	972289			The Barrier	2251	025791	001920		998080		HE:
36		973628				2244	024440			998068		
	25	974962	2217	025038			023094			998056		
	26	976293			the second second second second second		021752			998044		
	27	977619				1000202	020414			998032 998020	33	
52	28	978941			The second second second		019079			998008		1
	200	980259					017749		12736	9.997996		90
55 0	31			11.018427			015101	10.002004		997984	29	30
4	35	982883 984189					013783			997972	28	4
12	33	985491	2163	014509			012468		100	997959	27	16.6
16	34	986789			988842	2178	011158	and the second		997947	26	10
20	35	988083				2171	009851	002065		997935		
24	36	989374					008549			997922	24	
28	37	990660			992750		007250			997910	23	
32	38	991943					005955	002103		997897 997885		
36		993222					004663 003376			997872		
44	40	994497 995768					002092		1000	997860		
	42	997036			All the second of the second of		000812			997847		
52		998299					10.999535			997835		
56		999560		000441	001738		998262		21	997822	16	-
				10.999184			10.996993	10.002191	21	9.997809		37
	46	002069			004272	2103	995728	002203		997797		
8	47	003318	2076	996682	005534	2097	994466	005516		997784		
12	48	004563					993208			997771		1
	49	005805	1 1000							997758		
	50											
	51	008278										
32	52	009510										-
36		011962										2.3
	55	013182		986818			984498					
	56	014400	2023	985600			983268	002333		997667	4	1
48	57	015613			017959							
52	58	016824	2012	983176							2	
THE STATE OF THE S	59	018031								997628	1	90
24 0	60	019235	2000	980765	021620	2023	978380	002386	55	997614	U	36
m. s.	1	Cosine.		Secant.	Cotang.	-	Tang.	Cosec.		Sine.	1	w.
1	-	5 Ho				or	-2007			grees.		
P.P		18	15"		1.	15"	330	The second second	15"	3	ľ	4
P. P.	ro	2	30	655	2	30	661	2	30			

			0 Но			0				Degree.		
n.	S.	_	Sine.	Cosec.	Tang.	D. S. T.	Cotang.	Secant.	D.		鮅	m,
0	0		0.000000	Infinite.	0.000000		Infinite.	10.000000	00	10.000000		60
	4	_	Contract Con	DATE OF THE PARTY	THE RESIDENCE OF THE PARTY OF T	1030213 700	13.536274 235244	000000	00	000000		
	12	3	764756 940847	235244 059153	940847	293484	059153	000000	00	000000	8000	
	16			12.934214			What I was a street of	000000	00	000000	-	
	20	5		837304		131969	837304	000000	00	000000	-	
	24	6	241877	758123	241878	111577	758122	000001	01	9.999999	54	
	28	7	308824	691176	308825	The state of the s	691175	000001	01	999999	-	
	32	8	366816	633184	366817	85254	633183	000001	01	999999	100	
	36	9	417968	582032	417970	76263 68988	582030	000001	01	999999		
	40	10	463725 505118	536275 494882	463727 505120		536273 494880	000002	01	999998 999998	1000	
	48	-	542906	457094	542909	57934	457091	000003	01	999997		
	52		577668	422332	577672	53642	422328	000003	01	999997	-	
	56		609853	390147	609857	49939	390143	000004	01	999996	1000	
1		_		12.360184	7.639820	46715	12.360180	The state of the s	01	9.999996	45	59
ì	4	16	667845	332156	667849	43882	332151	000005		999995		
	8	17	694173	305827	694179	41373	305821	000005	01	999995	43	
	12		718997	281003	719003		280997	000006		999994		1
		19	742477	257523	742484		257516	000007	01	999993		
	20		764754	235246	764761	35136	235239	000007	01	999993	100	
	24	22	785943 806146	214057 193854	785951 806155	33673 32176	214049 193845	000008	01	999999 999991		
	28 32		825451	174549	825460		174540	000010	01	999990		
	36		843934	156066	843944		156056	000011	02	999989	130	
	40		861662	138338	861674	III CONTROL TO STATE OF	138326	000012	02	999988	100	
	44		878695	121305	878708		121292	000012	02	999988	1000	
	48		895085	104915	895099	26324	104901	000013	02	999987	33	
	52		910879	089121	910894		089106	000014	02	999986		
	56	_	926119	073881	926134	THE RESIDENCE OF	073866	000015	05	999985	_	
2	-	_		12.059158	DOMESTIC OF THE PARTY OF THE PA		12.059142		02	9.999983		58
*		31	955082	044918	955100		044900	000018		999982		
	12	32	968870 982233	031130 017767	968889 982253	22274 21609	031111	000019	02	999981	100	
		34	995198	004802	995219		004781	000020	02	999980 999979		
				11.992213			11.992191	000023	Mark I	999977		
	24		020021	979979	020045	100000000000000000000000000000000000000	979955	000024	02	999976	100	
	28	37	031919	968081	031945	19304	968055	000025	02	999975	23	
	32		043501	956499	043527	18802	956473	000027	02	999973		
	36		054781	945219	054809		945191	000028	02	999972	21	
	40		065776	934224	065806	-	934194	000029	02	999971	20	
	44		076500 086965	923500 913035	076531 086997	17443	923469 913003	000031	02	999969 999968	19	
	52		097183	902817	097217	16640	902783	000032	02	999966		
	56		107167	892833	107202	16267	892797	000036	03	999964	Digital Associated	
3			Section Section Section 5.	11.883074	The second second			10.000037	03	9.999963		57
-		46	126471	873529	126510	The second second	873490	000039	03	999961		-
		47	135810	864190	135851	15240	864149	000041	03	999959		
	12	-	144953	855047	144996	14926	855004	000042	03	999958	12	
	16	_	153907	846093	153952	14624	846048	000044	03	999956		
	20		162681	837319		14334	837273	000046		999954		
	24		171280 179713	828720			828672	000048		999952		
	32			820287 812015	188036	13530	820237 811964	000052		999950 999948		
	36			803898		13282	803844	000054		999946	6	
	40			795930	201126		795874	000056	03	999944	5	
	44	56		788105	211953	12812	788047	000058	04	999942	4	
	48		219581	780419	219641	12509	780359	000060		999940	3	
-		58		772866	The Part of the Pa	12374	772805	000062		999938	2	
4	56	59	234557	765443	234621	12166	765379	000064		999936	1	
4	0	60	241855	758145	241921	11965	758079	000066	04	999934	0	06
3.	8.	1	Cosine.	Secant.	Cotang.	VALUE OF STREET	Tr	nc.		Sine.	15	œ.
			5 Ho		Acres de la constitución de la c	or	U			egrees.		
	P. t	01		5" 3560	I.a	15"	1		15"	0	10	P. 1
		01	2 9	7120	2	30			30	0	8.8	

1	20		TABLE	v.	Log	garithmic	Sine	s, Tangen	ts,				1
		lii	0 Ho		Committee	The same	or	Course		De	Cosine.	-	-
m.	_	=	Sine.	D.	Cosec.	Tang. 8.543084	D.	Cotang. 11.456916	Secant.	07	9.999735	=	m. s.
16	4	_	546422		453578	546691	SCHOOL SECTION AND ADDRESS OF THE PARTY OF T	453309	000269	07	999731	59	56
ш	8				450005		20000000	449732	000274	07	999726 999722	58 57	52
ш	12			PROPERTY.	446461 442946	553817 557336	IN THE REAL PROPERTY.	446183 442664	000278 000283	08	999717	56	44
И	20	5	560540	5765	439460	560828	5773	439172	000287		999713	55	48 44 40 36 32 28
П	24 28	6	563999 567431		436001 432569	564291 567727		435709 432273	000292 000296	08	999708 999704	59	36
П	32	8	570836			THE RESERVE AND ADDRESS OF THE PERSON NAMED IN	10000	428863	000301	08	999699	52	28
li.	36	9	574214	THE REAL PROPERTY.	425786	200000000000000000000000000000000000000	The second	425480	000306 000311	08	999694	51 50	24 20
П	44	11	577566 580892	100000	422434 419108		100000000	422123 418792	000311	08	999689 999685	1004	16
ш			584193	5460	415807	584514	5468	415486	000320		999680		12
и	52	13		1000000	412531	587795 591051	2000	412205 408949	000325	08	999675 999670	47	8
9		100		Name and Address of	11.406052	The second secon	No. of London		10.000335	08	9.999665	45	51 0
	4	16	597152	5300	402848	597492	5308	402508	000340	08	999660		56
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10	-	200	-	NAME OF TAXABLE PARTY.	11.360320	THE RESIDENCE OF	The Section of	The state of the state of	10.000414	09	9.999586	30	50 0
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		18	874938					123838	001224		998776	12	48
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	20				121715				001243		998757	40	40
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ш	32				116742			THE RESERVE OF THE PARTY.	001272		998728	37	28
	36		884903		115097			113815	001282		998718	36	24
	40		888542 888174	Total Control	-20 440			112167 110524	001292	16 16	998708 998699		20
	48		889801		111826 110199		120072001	108888	001301	16	998689	10	12
13	52		891421	2690	108579			107258	001321	16	998679	35	8
	56	SCOOL SECTION	893035	The Real Property lies	CONTRACTOR STATE	894366	DESCRIPTION OF	105634	001331	17	998669	31	4
18					11.105357			11.104016	10.001341	17	9.998659	30	42 0
100		31 32	896246 897842		103754 102158	897596 899203	123/2012/07	102404	001351	17	998649 998639	29	30
	12		899432		100568	900803			001371	17	998629	27	48
	16		901017		098983		123200	097602	001381	17	998619	24	- 44
	20	-	902596		097404			096013	001391	17	998609	25	40
1	28		904169			905570		094430 092853	001401 001411	17 17	998599 998589	90	89
20	32		907297			100		091281	001422		998578	22	28
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12	56	44	916550	-	083450	918034	HEATONING	081966	001484		998516		14
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	28		927100						001558		998442	9	32
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1	40							065384	001601		998399	3	32 28 24 20 16
1	44		934481 935942						001612		998388	8	
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10	16	4			053966				001700		998300	1004	4
9	20	567	947456 948874		052544 051126	THE RESERVE AND ADDRESS OF THE PERSON NAMED IN COLUMN TWO IN COLUMN TO THE PERSON NAMED IN COLUM		050838	001711	19	998289 998277		3
18	28	7	950287		049713	2555000		047979	001734		998266		3
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	36	10	953100		046900			045144	001757	19	998243		2
	40		954499 955894		045501 044106	The state of the state of		043733 042326	001768	100	998232		20
		12	957284		042716			040925	001791	19	998209		15
		13	958670	2302	041330		2322	039527	001803	19	998197		
	56	-	960052	THE REAL PROPERTY.	039948		-	038134	001814	19	998186	-	4
21					11.038571			11.036745	STREET, SQUARE, SQUARE	19	9.998174	900	
	-	16 17	962801 964170	projection .	037199	202103		035361 033981	001837 001849	19	998163	-	59
	12		965534	SCHOOL SECTION 1	035830 034466	CONTRACTOR OF STREET	SHEERING OF	032606	001861	20	998139		48
	16	19	966893	\$600000E	033107	968766		031234	001872	20	998128	41	44
	20		968249		031751	970133		029867	001884	20	998116		4(
	24		969600		030400		NAME AND POST OF	028504	001896		998104 998092		36
	32		970947 972289		029053 027711	972855 974209		027145	001908 001920	20	998092		26
	36		973628		026372			024440	001932	20	998068		24
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22	STATE OF THE PARTY.	_	-	-	11.018427	The second second	-	11.016423		20	9.997996	_	
	4	31	982883		017117	984899		015101	002016	20	997984		56
	8		984189	2170	015811	986217	2191	013783	002028	20	997972	28	59
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	16 20	34	986789 988083		013211	988842 990149		011158 009851	002053 002065	20 21	997947 997935		44
	24	36	989374		010626	991451		003549	002078	21	997922		36
3	28	37	990660		009340	992750	2158	007250	002090	21	997910		32
	32		991943		008057	994045	March 1997	005955	002103	21	997897		28
	36		993222 994497	MODE OF THE PERSON	006778 005503	995337 996624		004663 003376	002115 002128	21	997885 997872		24
	44		995768		003303	997908	MONGHOW.	002092	002140	21	997860	-	16
	48		997036		002964	999188		000812	002153	21	997847		12
		43	998299	DESCRIPTION OF	37.50.42	9.000465			002165	21	997835		8
_	56		999560	THE OWNER OF THE OWNER, NAMED IN	000441	001738		998262	002178	21	997822		. 4
23	0		DAMES OF THE PARTY	COLUMN 1	A STATE OF THE PARTY OF THE PAR			10.996993			9.997809		37 0
	8		002069		997931 996682	004272		995728 994466	002203	21	997797 997784		52
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	16		005805		994195	008047	2085	991953	002242	21	997758	11	44
	20		007044		992956	009298	DESCRIPTION OF THE PERSONS ASSESSMENT	990702	002255	21	997745		40
	24 28		008278		991722 990490	010546		989454 988210	002268		997732		36
	32		010737		989263	013031		986969	002294		997706	7	28
	36	54	011962	2034	988038	014268	2056	985732	002307	22	997693	6	24
	40		013182		986818	015502		984498	002320		997680	5	20
	48		014400		985600	016732 017959		983268 982041	002333 002346		997667 997654	4	16
	52		015613		984387 983176	017939		980817	002346		997641	2	8
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5	26		TABLE	100	L	garithmi	ic Sin	es, Tanger	nts,				3
E		1	0 Hc	-		l m	or	Lai			grees.	-	
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32								10.852197 851282		200	9.995753		28 0
п	-					Married Co. Co.			7-12-20-20-20-20-20-20-20-20-20-20-20-20-20	100	995717		52
и	15		146243	ALC: NO. 10	The state of the s	15054	1 1517	849456			995699	_	46
	16					The State of the S			The second secon	100	995681	1000	44
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п	28				A CONTRACT OF STREET	THE RESERVE THE PARTY OF THE PA				1	995628		
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ш	48		154208	1460	845792	Company of the last of the las	of the Controlled	THE RESERVE OF THE PERSON NAMED IN	004463	30	995537	48	12
	52				844917	I management of the contract o		2035369	004481	30	995519		8
33	_	14		Contract Contract		THE REAL PROPERTY.	Name and Address of the Owner, where	839543 10.838653		31	995501		27 0
3.3	4	****			842300			837764		31	995464		
п		17	158569	1445	841431	THE RESERVE AND PARTY.		70000000	004554		995446	100	56 52
ы		18	159435		840565				004573		995427		48
111		19	160301 161164		839699 838836			835108 834226	004591 004610		995409 995390	-	44
10		21	162025	A 10 A	837975	1 4000000000000000000000000000000000000	1 20 20 20 20 20		- CO. C. C. C. C. C.	31	995372		36
100		55	162885		837115			832468		31	995353		32
10		23	163743 164600		836257 835400	In Colombia Colombia	E CONTRACTOR IN	THE RESIDENCE OF THE PARTY OF T	004666 004684	31	995334 995316		28
		25	165454		834546				004703	31	995297		20
95	44	26	166307	1419	833693	CO AND DESCRIPTION		828971	004722	31	995278	34	16
W.		27	167159		832841	171899		828101	004740	31	995260		12
		28	168008 168856		831992 831144	172767 173634		827233 826366	004759 004778	32	995241 995222	32	1
34	- California	1	THE RESIDENCE OF THE PARTY OF T		10.830298	THE PERSON NAMED IN	The second	Secretary and the second	10.004797	32	9.995203		26 0
	4	31	170547	1405	829453	175362	1436	824638	004816	32	995184		56
17		32	171389		828611	176224	THE RESIDENCE OF	THE PROPERTY AND ADDRESS.	004835	32	995165	28	52
		34	172230 173070		827770 826930	177084 177942	Market Street	822916 822058	004854 004873	32	995146 995127	27	48
10	20	35	173908		826092	178799	STREET, STREET	821201	004892	32	995108	25	40
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10		37	175578 176411		824422 823589	180508 181360		819492 818640	004930	32	995070 995051	23	32 28
13		39	177242		822758	182211		817789	004968	32	995032	21	24
13	-	40	178072		821928	183059	1412	816941	004987	32	995013	50	20
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9.		43	179726 180551		820274 819449	184752 185597		815248 814403	005026 005045	32	994914	17	14
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35							STREET, STREET	10.812720	STATE OF THE PARTY		and the later to t	15 8	
100		46	183016 183834		816984 816166	188120	ALC: UNKNOWN	811880		33	The Control of the Co	14	56
30	12	ш.	184651		815349	188958 189794	WHEN SHAPE IN	811042 810206	005123 005143	33	994877 994857	-	52
20	16	49	185466		814534	190629	1389	809371		33		11	44
80	20	194	186280	COLD II	813720	191462		808538		33	994818		40
183	24 28		187092		812908 812097	192294		807706 806876	005202		994798	8	36
15	32		188712		811288	193953		806047	005241		994759	7	28
100	36		189519		810481	194780		805220	005261		994739	6	24
50	40		190325		809675 808870	195606 196430		804394 803570	005281		994719	5	20
34	48		191933		808067	196430		802747	005320		994680	3	12
3	52	58	192734	1333	807266	198074	1366	801926	005340	33	994660	2	8
36	56		193534		806466	198894		801106	005360		994610	1	4
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	6 0 0 9.194332 1328 10.805668 9.199713 1361 10 800287 10.005380 33 9.994620 60 24 0 4 1 195129 1326 804871 200529 1359 799471 005400 33 994600 59 56 8 2 195925 1323 804075 201345 1356 798655 005420 33 994580 58 52 12 3 196719 1321 803281 202159 1354 797841 005440 34 994560 57 48 16 4 197511 1318 802489 202971 1352 797029 005460 34 994540 56 44 20 5 198302 1316 801695 203782 1349 796218 005481 34 994519 55 40 24 6 199091 1313 800909 204592 1347 795408 005501 34 994499 54 36 28 7 199879 1311 800121 205400 1345 794600 005521 34 994479 53 32 8 200666 1308 799334 206207 1342 793793 005541 34 994459 52 28												
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36				1328	10.80566H				10.005380				
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		9	201451	1306	798549				005562		994438		24
		10	202234			207817		792183			994418		20
	44		203017		796983						994398		16
		12	203797			209420 210220		790580 789780	005623 005643		994357		8
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•		16	206906		793094	212611		787389	005705		994295		56
		17	207679		792321	213405		786595	005726		994274		52
		18	208452		791548						994254	12	48
	16	19	209222	0.14.0.0.	790778	214989		785011	005767		994233		44
		20	209992			215780					994212		40
	24		210760								994191		36
		22 23	211526 212291			217356			005829 005850		994171		28
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		26						779508			994087		16
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18									10.005997		9.994003		2 0
		31	218363		781637	224382					993982		56
	12	32	219116 219868		780884	225156					993960 993939		48
	16		220618		780132 779382	225929 226700					993918		44
		35	221367		778633			772529			993897		40
		36	222115			228239					993875		36
	28		222861	1242	777139			770993	006146		993854		38
		38									993832		28
		39	224349			230539					993811		24
		40	225092					768698			993789		20
		41	225833 226573		774167 773427			767935 767174			993768		16
		43	227311		772689	233586		2.2.2.2.2.2			993725		
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9									10.006319		9.993681	-	
	4	46	229518		770482	235859			006340		993660		56
		47	230252		2500000	236614		763386		-	993638		52
	12	48	230984	1218	769016	237368			006384	36	993616	12	52 48
		49		1516	768286	238120	1252	761880	006406		993594		44
		50							006428	37	993572		40
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		56							006560	37	993440	4	16
	48	57	237515			244097	1236	755903		37	993418	3	12
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		59							006626		993374	1	4
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n.	S.	1	Cosine.		Secant.	Cotang.		Tang.	Cosec.		Sine.	' n	ı. s.
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3	08		TABLE		Log	arithmic	Sine	, Tangent	the second named in					
4		1777- 1	0 Ho		O CONTRACTOR	more lands	or	O WHEEL I		-	grees.	(10.7)	4.00	-
m.	S.		Sine.	D.	Cosec.	Tang.	D.	Cotang.	Secant.	-	Cosine.		m.	54
48	. 0		9.317879	990	DESCRIPTION OF THE PERSON NAMED IN			10.672526	10.009596	82	9.990404		12	0
10	4 8		318473 319066	988 987	681527 680934	328095 328715		671905 671285	009622	320	990378 990351			56 52
10	12		319658		680342	329334	1000000	670666	009676	10000	990324			48
B	16		320249	984	679751	329953	100000	670047	009703	100	990297			44
19	20	5	320840		679160	330570		669430	009730		990270			40
ю	21		321430	982	678570	331187	2000000	668813	009757		990243			36
119	28		322019	400000	677981	331803		668197	009788	P 2000	990215			32
Į)	32		322607 323194	979	677393 676806	332418 333033		667582 666967	009812		990188 990161	51		28 24
100		10	323780		676220	333646		666354	009866	PRE	990134	1100		20
100	44	75 E3000 E	324366	DOM: N	675634	334259		665741	009893		990107	49		16
Ю	48	12	324950		675050	334871	1019	665129	009921	46	990079	48		12
и		2 13	325534	1000000	674466	335482		664518	009948	W 40	990052	47		8
10	56	5 14	326117	970	673883	336093	THE OWNER OF THE OWNER OWNER OF THE OWNER OWNE	663907	009978	Name and	990025	46	PS	4
49		4 DOM:	9.326700					10.663298			9.989997			0
120		16	327281	968	672719	337311			010030	10000	989970			56
10		17	327862	4 16 6 1	672138	337919		662081	010058		989942			52
125		18	328442 329021	965	671558 670979	338527 339133	200000	661473 660867	010083	1 6 6 4	989915 989887			48 44
16		20	329599	E-9-61	670401	339739		660261	010140	1000	989860			40
10	- 100	121	330176	2000	669824	N. CORPORATION CO.		659656	010168		989832	2.00	_	36
18	28	3 22	330753	960	669247	340948	1006	659052	010196	46	989804	38		32
10		2 23	331329	100 March 1990	668671	341552		658448	010223		989777	8000		28
10	36	400	331903		668097	342155		657845	010251		989749		1000	24
17.	44	25	332478 333051		667522	342757 343358		657243 656642	010279	e soute	989721 989693		_	20 16
В	48	200	333624		666949 666376	The Control of the Co		656042	01033		989665	1000		12
10	59	720	334195		665805	- 140 KT 60 KT 1	998	655442	010363		989637		Sec.	8
J.		6 29		222	665234	345157	997	654843	010391	1000	989609		00	4
50		30	9.335337	949	10.664663	9.345755	996	10.654245	10.010418	47	9.989582	30	10	0
10		431	335906		664094	THE RESERVE AND ADDRESS OF THE PARTY OF THE	4 40 4	653647	01044		989553	100		56
18		8 32			663525	Control of the National Control	993	The second second second	01047		989525			52
12	1:	THE RESIDENCE	All the second second second		662957			652455			989497			48
13		6 34			662390		991	651859	A CONTRACTOR		989469			44
16	2				661824 661258	TO THE REAL PROPERTY.	990	651265 650671		N CONTRACTOR	989441 989413	1000		36
5.	21	3 500	339307		660693		987	650078			989385		_	32
10	3	200		1000000	660129	10000000	I I I STORY OF THE			7	989356			28
(A)	3	6 39	340434	937	659566	351106	985	648894	01067	2 47	989328		OE	24
100	40	1000	THE RESIDENCE OF THE PARTY OF T		659004	W 40 W 40 4 40	983			31 000	989300			20
12	4	7 1999	III MANAGEMENT	100000	658442		982		1 11 Table 14 (1977)		989271			16
1	48		The second second		657881		11223	647124	100000000000000000000000000000000000000		989243			12
6		6 44	THE PROPERTY		657321 656761	353465 354053	980 979	200000000000000000000000000000000000000			989214 989186			4
51	-	0 45		Name and Address of the Owner, where the Owner, which is the Owner, where the Owner, which is the Owner, whic	10.656203	Call Section Control of Control		10.645360		Name of	CONTRACTOR OF THE PARTY OF	-	_	0
10	_	4 46	THE RESIDENCE AND ADDRESS OF	I I I I I I I I I I I I I I I I I I I	655645		976				989128			56
10		8 47		The second	655088	THE RESIDENCE OF THE PARTY.		A UDDECAS		1000	989100	1100		52
11	1		A STATE OF THE PARTY OF THE PAR		654531	1 2 2 3 2 7 1 2	0.000	1000000000	01092	48	989071			48
W	1	2 100	The state of the s		653976		1 CO. E.				989042	100		44
16		0 50	The second second		653421	The second second		642434		1 1000	989014			40
16		8 52			652866	100000000000000000000000000000000000000	2000		100000000000000000000000000000000000000	of Maries	The Control of the Co			90
10		2 53		990	652313 651760						988930	7	12	90
A		6 54	348799		651208							6	36	24
14	4	0 55	349343	917	650657	360474		639526	01113				00:	
9		4 56			650107	361053	965		01116	48	988840	14	40	16
2		8 57			A SHARE THE PARTY OF THE PARTY							3	MA.	
1		2 58	The second second								988782		26	8
58		6 59 0 60			648460 647912			1000000000					8	10
						-	500	N. D. Contraction of the Contrac		-	-	-	-	
m	-	S. '	The state of the s	1	Secant.	Cotang.		Tang.	Cosec.	17.10	Sine.	100	III.	
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5	or	"	3	45	427	3	45	448	31	45	22	5	or '	
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		_	0 He	ur.			or		1	_	egrees.		
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2	0			911			960	10.636636	-				8 0
*	4		352635		10.647912		100000	636060			988695		56
	8	9	353181	909	647365 646819		1000000	635485	011303		988666		52
	12		353726		646274		9.000	634910	011364		988636		48
	16	1	354271		645729			634336		1000	988607		44
	20		354815		645185			633763			988578		40
	24	6	355358		644642	366810		633190			988548		36
	28		355901	903	644099			632618				58	32
	32	8			643557			632047	011511				28
	36		356984		643016			631476			988460		24
		10	357524		642476			630906		100	988430		20
		11	358064		641936		100 100 100	630337	011599			19	16
	48	12	358603		641397			629768	011629		988371	18	12
	52	13			640859			629201	011658				8
		14	359678		640322			628633	011688	50	988312	16	4
3	0	1.5	9.360215				_	10.628067	10.011719	50	9.988282	4.5	7 0
_		16			639249			627501	011748		988252		56
		17			638713			626936	011777		988223		52
		18	361822		638178		10000	626371	011807		988193		48
		19	362356		637644			625807	011837		986163		44
		20	362889		637111	374756		625244	011867		988133		40
		21	363422	887	636578		100000	624681	011897		988103		36
		22	363954		636046		200	624119	011927		988073	38	32
		23			635515			623558	011957		988043	37	28
		24	365016		634984		933	622997	011987	50	988019		24
	40	25	365546		634454	377563	932	622437	012017	50	987983	35	20
	44	26	366075	881	633925	378122	931	621878	012047	50	987953		16
		27		880	633396	378681	930	621319	012078	50	987922		12
	52	28	367131	879	632869	379239	929	620761	012108	50	987892	32	8
	56	29	367659	877	632341	379797	928	620203	012138	50	987862	31	4
4	0	30	9.368185	876	10.631815	9.380354	927	10.619646	10.012168	51	9.987832	30	6 0
		31	368711		631289			619090			987801	29	56
		32			630764			618534	012229		987771		52
		33	369761		630239			617980	012260		987740		48
		34	370285		629715			617425	012290		987710		44
		35	370808		629192			616871	012321		987679		40
		36	371330		628670	383682	921	616318	012351	51	987649		36
	28	37	371852		628148	384234	920	615766	012382	51	987618	23	32
	32	38	372373	867	627627	384786	919	615214	012412	51	987588	22	28
	36	39	372894	866	627106	385337	918	614663	012443	51	987557		24
	40	40	373414	865	626586	385888	917	614112	012474	51	987526		20
		41	373933		626067			613562			987496		16
		42	374452	863	625548	386987	914	613013			987465		12
		43	374970	862	625030			612464	012566		987434		8
	56	44	375487	861	624513	388084	912	611916	012597	52	987403	16	4
5	0	45	9.376003	860	10.623997	9.388631	911	10.611369	10.012628	52	9.987372	15	
		46			623481	389178		610822	012659		987341	14	56
		47			622965			610276	012690	52	987310	13	52
		48	377549		622451	390270		609730	012721		987279	12	48
	16	49	378063		621937			609185			987248	11	44
		50	378577	854	621423			608640			987217	10	
	24	51	379089		620911			608097			987186	9	36
	28	52	379601		620399			607553			987155		38
	32	53	380113		619887			607011	012876		987124		28
		54			619376			606469					24
		55			618866			605927	012939		987061	5	20
		56			618357	394614		605386			987030		16
		57			617848			604846			986998		12
		58			617339			604306	013033		986967	2	8
		59			616832			603767	013064		986936	1	4
6	0	60	383675	844	616325	396771	896	603229	013096	52	986904	0	4 0
	8	7	Cosine.		Secant.	Cotang.		Tang.	Cosec.		Sine.	7	m. s.
-	-	_	5 Ho	170	Occano	County.	or	- migi		S De	grees.	_	_
-		_		-	1 101	1. 1		1 190		15"	8 1		-
	P.		118	15"	131	15	15"	139		30	15	P.	P. to
	or		2	30	263	2	30	278				15	" 70 8
S	or		3	45	394	3	45	417	3 /	45	/ 53	7.	,,

3	2		TABLE		Log	garithmic	Sine	s, Tangen			-		
	-	11	0 Ho		Cases	Tono	D.	Cotone			grees.	100	
m.	5.			D,	Cosec-	Tang.		Cotang.	Secant.	D.		_ n	
56	0	0	9.38367 <i>5</i> 384182	Electric leads	10.616325 615818	9.396771 397309	896 896	602691	10.013096 013127	52 53	9.986904 986873		4 0
100	8			842	615313		895	602154	013159	100000	986841	58	-52
ж	12	3		EMPORT OF THE PERSON NAMED IN	614808			601617	013191	DOM:	986809	57	48
м	16	4	385697	840	614303		893	601081	013222		986778	-	44
100	20	5		839	613799	399455	892	600545	013254	1000	986746	55	40
100	24 28	6	386704 387207	838 837	613296 612793	399990	891	600010 599476	013286 013317		986714 986683	54	36
	32	8	387709		612291	400524 401058		598942	013349		986651	52	28
	36	9	388210	THE REAL PROPERTY.	611790	100000000000000000000000000000000000000	888	598409	013381		986619	100	24
		10	388711	834	611289			597876	013413		986587	50	20
ш		11	389211	833	610789	402656	886	597344	013445		986555		16
100		12	389711	832	610289	403187	885	596813	013477	53	986523		12
No.	52 56	HOM.	390210 390708	100000	609790 609292	403718	884	596282 595751	013509 013541	53	986491 986459		(n 8
57	-		9.391206	828	10.608794	-	882		10.013573		9.986427	200	3 0
21	-	16	391703	827	608297	405308	881	594692	013605		986395		3 0
24		17	392199	826	607801	405836	880	594164	013637		986363		58
1-3	12		392695		607305	406364	879	593636	013669	-	986331	12	7 48
112	16		393191	824	606809		878	593108	013701		986299		41
ne	20	man a	393685		606315	The Control of the Co	877	592581	013734	100	986266	-	40
67	24 28		394179 394673		605821 605327	407945 408471	876	592055 591529	013766 013798	-	986234 986202	-	36
100	32		395166		604834		874	591003	013831	54	986169		28
Ш	36		395658		604342	409521	874	590479	013863	-	986137		24
100	40		396150		603850	THE RESERVE OF THE PERSON NAMED IN	873	589955	013896	54	986104		20
(0.5)			396641	817	603359	With the control of t		589431	013928		986072		16
83	48		397132		602868	The second second	871	588908	013961	54	986039		18
16	52		397621 398111	816	602379 601889	The second second second	870 869	588385 587863	013993 014026		986007 985974		8
58	_	_	9.398600	A COLUMN	10.601400		868		10.014058	1	9.985942		- 1
30		31	399088	200	600912		867	586821	014091		985909		2 5
10		32	399575		600425	The second second	DOM: NO	586301	014124		985876	200	58
Ю	12		400062		599938	414219	865	585781	014157	55	985843		48
	16		400549	2.602.201	599451	the second second second		585262	A STATE OF THE STATE OF	Beded.	985811	26	44
80	20	100	401035	20 60 70 11	598965	ALCOHOLD STATE OF THE PARTY OF	864	584743		99	985778		40
13	24 28		401520 402005		598480 597995	100000000000	4000	584225 583707	014255 014288		985745 985712	24	36
в			402489		597511			583190	014321	55	985679		28
	36		402972	100000	597028	ACCOUNT OF THE PARTY.	100000	582674	014354		985646		24
и	40	40	403455	804	596545	417842	859	582158	014387		985613		20
и	44	41	403938	COG. DX	596062			581642	014420	Ten de la	985580		16
м	48		404420	500000	595580			581127	014453	90	985547	_	12
	56		404901 405382	801	595099 594618		856	580613 580099	014486 014520		985514 985480		7
59	-	-	9.405862		10.594138		855		10.014553	Barbal	The state of the s	15	1 0
	-		405341	798	593659	THE RESERVE OF THE PARTY.	854	579073	014586	-	985414	14	56
15	-		406820	100000	593180	The second secon	DOM: N	578560	014619		985381	13	52
1	12		407299		592701	421952		578048	014653	Region 1	985347	12	48
1	16	49	407777	795	592223			577537	014686	90	985314	11	- 43
12	20	1	100000		591746	I sonana	nin	577026	011000	1000	985280		40
1/3	28	52			591269			576516			985247		36
1	32					424503		575497			985180		28
1	36	54	410157	791	589843	425011	847	574989			985146		24
1	40				589368			574481			985113	5	20
1		56			588894			573973			985079	4	16
	48	58			588421 587948			573466 572959			985045 985011	3	12
		59			587476			572453			984978	1	8
60		60			587004			571948			984944	0	
m.	S.	=	Cosine.		Secant.	Cotang.		Tang.	Cosec.	=	Sine.	/ 17	=
		-	5 Ho	urs.	- Secretary	o walk	or	- ung.	-	5 D	egrees.	-	
10	P	11	1 1 1	15"	1 122	18	15"	130		15"	8	1	
-	P.		2	30	244	2	30	260	2	30	16	P. 1	P. 10
01	-	1	3	45	366	3	45	391	13/	45	25	8.0	16
			-										

						and	Seca	nts.		TA	BLE V.		33
			1 Ho	ur,			or	-			grees.		
١.	8.	"	Sine.	D.	Cosec.	Tang.	D.	Cotang.	Secant.	D.	Cosine.	1	m. s.
ō	0	0		785	10.587004	9.428059	842	10.571948	10.015056	57	9 98 1944	60	60 0
Ĭ	4	ĭ	413467		586533	428557		571443	015090		984910		56
	8	2	413938	783	586062	429062		570938	015124		984876		52
	12	3	414408		585592	429566		570434	015158		984842		48
	16	4	414878	782	585122	430070		569930	015192	57	984808	56	44
	20	5	415347	781	584653			- 569427	015226	57	981774	55	40
	24	6	415815	780	584185	431075	837	568925	015260	57	984740	54	36
	28		416283	779	583717	431577	836	568423	015294	57	984706		35
	32	8	416751	778	583249	432079	835	567921	015328	57	984672		28
	36		417217		582783			567420	015362	1000	984638		21
	40		417684		582316	433080		566920	015397		984603		20
	44		418150		581850	433580		566420	015431	10.00	984569		16
	48		418615		581385	434080		565920	015465	1	984535		12
	25		419079	773	580921	434579		565121	015500		984500		. 8
	56	14	419544	773	580456	435078	830	564922	015534	57	984466	16	4
1	0	15	9.420007	772	10.579993	9.435576	859	10.564424	10.015568	5H	9.981132		
	4	16	420470		579530			563927	015603	58	984397		56
		17	420933		579067	436570		563430	015637	58	984363	43	52
	12	18	421395	769	578605			562933	015679	58	984328		48
	16	19	421857	768	578143			562437	015706	58	984294		44
	20		422318		577682	438059	825	561941	015741		981259		
	24	21	422778	767	577222	438554	824	561446	015776	7250	984224		
	28	22	423238		576762			560952	015810		984190		
	32		423697	765	576303			560457	015845	1	984155		28
	36		424156	764	575844			559964	015880	100	981120		
	40		424615	763	575385			559471	015915		984085		
	44		425073		574927			558978	015950		984050		
	48	200	425530		574470			558486	015985		981015		
	52		425987	760	574013			557994	016019		983981		8
	56	29	426443	760	573557	442497	818	557503	016054	58	983946	-	4
2	0	30	9.426899	759	10.573101	9.442988	817	10.557012	10.016089	58	9.983911		
		31	427354	758	572646	443479	816	556521	016125	58	983875	59	56
	8	32	427809	757	572191	443968	816	556032	016160	59	983840		52
	12		428263	756	571737			555542	016195	59	983805		48
	16		428717	755	571283	444947	814	555053	016230	59	983770		44
	20	35	429170	754	570830	445435	813	554565	016265		983735		40
	24		429623	753	570377	445923		554077	016300		983700		
	28		430075	752	569925			553589	016335		983664		32
	32		430527	752	569473			553102	016371		983629		28
	36		430978	751	569022			552616	016406		983591		21
	40	40	431429	750	568571	447870		552130	016442		983558		10
	44		431879		568121			551644	016477		983523		16
	48		432329	749	567671	448841		551159	016513		983487		15
	52		432778	748	567222	4 2 2 2 2 2	1	550674	016548		983452		8
	56	44	433226	747	566774	449810	806	550190	016584	59	983416	-	4
3	0	45	9.433675	746	10.566325	9.450294	806	10.549706	10.016019	59	9.983381		57 0
		46	434122		565878	450777		549223	016655	10000	983345	14	56
		47	434569		565431	451260		548740	016691	16/200	98330!	13	52
	12		435016		564984			548257	016727		983273		48
	16	49	435462	743	564538	452225	802	517775	016762		983238	11	44
	20	50	435908	742	564092			547294	016798		983202	10	40
	24		436353	741	563647			546813	016834		983166	9	36
	28	52	436798	740	563202			546332	016870		983130		32
	32			740	562758			545852	016906		983094		
	36			739	562314			545372	016942	60	983058	6	
	40				561871	455107	798	544893	016978	60	983022	5	
	44				561428			544414	017014		982986	4	16
	48	57				456064	796	543936	017050	60	982950		12
	52				560544	456542	796	543458	017086	60	982914		8
	56	59	439897		560103			542981	017122	60	982878		4
4	0	60			559662	457496		549504			982842		56 0
F	=	7	Cosine.		Secant.	Cotang.	-=	Tang.	Cosec.	-	Sine.	-	m. 8.
1.	8.				Secunt	Coung.	07	rang.	7.0	De	grees.	-	
_	_	_	4 Ho		1 111		or	1 100				_	-
	P. 1	10	13	15"		l ^s	15"		1,	30	17	10	1.7. to
			2	30	228	2	30	215					

C

I	40).		TABLE	10/10	Lo	garithmic	Sine	es, Tangen			-		
ı			-	1 Ho	-	1 Comme	- m	or	I Catana 1		-	grees.		
III	n.	5.		Sine.	D.	Cosec.	Tang.	D,	Cotang.	Secant	D.	Cosine.	-	
3	28	0	-	9-573575 573888		10.426425			10.393590 393227	032885	1000	9.967166 (56
ı		8	2	The second second	III CONTRACTOR	425800			392863	032936		967064		52
ı		12	3		1000000	425188			392500	032987	85	967013.	200	48
ı		16	4			425176			392137	033039		966961	-	44
H		20	5	THE RESERVE OF THE PARTY OF THE	100000	424864	100000000000000000000000000000000000000	0.0000	391775	033090		966910		40
ı		24 28	6	575447 575758	518 518	424553 424242	The second second	0.00	391412	033141 033192		966859 8 966808		36
п		32	8	576069		423931	The second secon		390688	033244		966756		28
ı		36	9	576379	517	423621			390326	033295	No.	966705		24
ı		40	Marie d	576689	516	423311	610036		389964	033347		966653		20
H		44	11	576999 577309		423001 422691	610397 610759	602	389603 389241	033398 033450	100000	966602		16
H		52		577618		422382	611120		388880	033501	86	966499		8
ı	1	56	14	577927	515	422073	611480	601	388520	033553	86	966447	16	4
6.0	9	0	15	9.578236	514	10.421764	9.611841	601	10,388159			9.966395		
1	II C		16	578545		421455	612201	600	387799	033656		966344		56
1		12	17	578853 579162		421147 420838	612561	600	387439 387079	033708 033760		966292 966240		59 48
1		16		579470	100000	420530	613281	599	386719	033812		966188		44
1		20	20	579777	512	420223	613641	599	386359	033864	86	966136	10	40
ı		24		580085		419915	614000	200.00	386000	033915		966085		36
u		28		580392 580699		419608 419301	614359 614718	2000	385641 385282	033967 034019	-	966033; 965981;	38	32
ı		36		581005	12/15/15	418995	615077	597	384923	034071	-	965929		24
ı		40		581312	1000000	418688	615435	100000	384565	034124		965876		20
ı		1000	26	581618	12000	418382	615793		384207	034176		965824		16
ı			27	581924	12255	418076	616151	596	383849	034228	Broke (965772		12
ı		52 56		582229 582535		417771	616509 616867	596 596	383491 383133	034280 034332	87	965720 965668		8
0	0	-	_	9.582840	-	10.417160	THE RESERVE OF THE PARTY OF THE	595	10.382776	-	87	9.965615		0
ľ		_	31	583145		416855	617582	595	382418	034437	87	965563		56
i	85		32	583449		416551	617939	595	382061	034489	87	965511	88	32
ı		12		583754		416246	618295	594	381705	034542		965458		48
I		16		584058 584361	506	415942 415639	618652 619008	594 594	381348 380992	034594 034647	87 88	965406 965353		44
н		24		584665		415335	619364		380636	034699		965301		36
ı		28		584968		415039	619721	593	380279	034752		965248	23	32
ı		32		585272		414728	620076		379924	034805		965195		28
ı		36 40		585574	504	414426 414123	620432 620787	592	379568 379213	034857 034910	88	965143 9 965090 9		21
ı		44	-	585877 586179	504	413821	621142		378858	034963		965037		20
п		48		586482	503	413518	621497	591	378503	035016		964984		12
ı		52		586783	503	413217	621852	591	378148	035069	88	964931	7	8
L	_	56		587085	502	412915	622207	590	377793	035121	ECONO		6	4
3	1			9.587386	502	10.412614		590	10.377439		Tracket I		5 29	0
I		-	46	587688 587989	501	412312 412011	622915 623269	590 589	377085 376731	035227	88	964773 1	4	56
	1	12	-	588289	501	411711	623623	589	376377	035334	89	9646661		48
I	8	16	49	588590	500	411410	623976	589	376024	035387	89	964613	1	44
I		20			500	411110	624330		375670	035440	89	9645601	0	40
I		24 28		589190	12000	410810	624683 625036		375317 374964	035493 035546	89	964507	9	36
I		32		589489 589789		410511	625388		374612	035600	89	964454	7	32
1	114	36	54	590088		409912			374259	035653	89		6	28 24
	123	40	55	590387		409613	626093	_	373907	035706	89	964291	5	20
I		14		590686		409314	626445		373555	035760	89	964240	4	16
١		48 52		590984 591289		409016 408718	626797 627149		373203 372851	035813		964187	3	12
1		56		591580		408120	627501	585	372499	035920		964080	1	20 16 12 8 4
3		0		591878		408122	627852		372148	035974			0 28	0
n	1.	8	r	Cosine.		Secant.	Cotang.		Tang.	Cosec.			, III.	8
F			E	4 Hou	ırs,	Name of the last	-	or	B 1		De	grees.	-	7
F.	P	P. 1	1	10	15"	76	10	15"	1 89	10 1	5"	1 19 1	0.0	-
		11 1		2	30	152	2 3	30	178	2 3	0	26	P. P.	
			1	3	45	229	3	45	268	3 4	5	39		

						and	Seca	nts.		TA	BLE V.		41
			1 Ho	ur,			or		29		grees.		
n.	8.	1		D.	Cosec.	Tang.	D.	Cotang.		D.		'lm	
32	0	=		==	10.408122		==					_	
,6	4				407824			371797			963972		56
	8	1 9	592170		407527			371446	036028		963919		59
	12		592770		407230			371095			963865		48
	16	4	593067		406933			370745	036189				44
	20	5			406637			370394			963757		40
	24		593659		406341			370044			963704		36
	28	7	593955		406015			369094					32
	32				405749			369344	036404				28
	36		594547		405453			368995			963542		21
	40				405158			368645	5.65.05.50.00		963188		20
	44				404863			368296			963434		16
	48				404568			367947			963379		19
	52			491	404273			367599	036675	90	963325	17	
	56				403979			367250	036729		963271		4
3	_	_	9.596315	490	10.403685	9.633098	580	10.366902	10.036783	90	9 963217	15 2	7 (
-		16			403391			366553	036837		963163		56
		17			403097			366205	036892		963108		58
	12				402804			365857	036946		963054		48
	16				402510			365510			962999		44
	20			400	402217	634838		365162			962945		40
	24		598075		401925			364815	037110		962590		36
	28		598368		401632			364468			962836		38
	32				401340			364121	037219		962781		28
	36			486	401048			363774	037 273	91	962727		24
	40	25	599214	486	400756	636572	577	363428	037328	91	962672	35	20
	44	26	599536	485	400464	636919	577	363081	037383	91	962617	34	16
	48	27	599827	485	400173	637265	577	362735			962562	33	15
	52	28			399882	637611	576	362389	037492	91	962508	35	
	56	29	600109	484	399591	637956	576	362044	037547	91	962453	31	4
4	0	30	9.600700	484	10.399300	9.638302	576	10.361698	10.037602	92	9.962398	30 2	6 (
		31			399010			361353	037657	92	962343		56
		32			398720			361008	037712		962288		59
	12		6 1570	483	398430			360663	037767	92	962233	27	48
	16		601860	482	398140	639682	574	360318	037822	92	962178	26	44
	20	35	6 12150	482	397850	640027	574	359973	037877	92	962123		40
	24	36	602439	482	397561	640371	574	359629	037933	92	962067	24	36
	28	37	602728	481	397272	640716	573	359284	037988		962012		32
	32	38	603017	481	396983	641060	573	358940	038043	92	961957	22	28
	36	39	603305	481	396595			358596	038098		961902		24
	40	40	603594	480	396406	641747	572	358253			961846	20	20
	44	41	603882		396118			357909	038209		961791		16
	48				395830			357566	038265		961735		15
	52		604457		395543		100 100 100	357223	038320		961680	3.2	
	56		601745		395255	643120	_	356880	038376	_	961624	_	4
5	0	45	9.605032		10.394968			10 356537					
	4	46			394681	643806		356194	038487		961513		56
		47			394394	750000000000000000000000000000000000000		355852	038542		961458		58
		48			394108			355510	038598				46
		49			393821	641832		355168					44
	20	50	606465		393535			354826					40
	24				393249			354484	038765		961235		36
ķ	28				392964	645857		354143	038821		961179	8	38
	35				392678			353801	038877		961123		28
	36				392393			353460			961067	6	24
	40				392108	646881		353119	038989		961011	5	20
	44				391823	647222		352778	039045	93	960955		16
	48				391539	647562	70.00	357438	039101	93	960899	3	12
	52				391255	647903		352097	039157		960843	2	8
	56				390971	648243		351757	039214		960786	1	4
6	0	60	609313	473	390687	648583	566	351417	039270	94	960730	0 24	. 0
a.	s.	1	Cosine.		Secant.	Cotang.		Tang.	Cosec.		Sine.	' m	. 8.
-			4 Ho	urs.			or			De	grees.	-	
_	-	-	14	15"	1 73	1. 1	15"	86		5"	1 14 1	5.5	
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	or	"	3	45	218	3	20	1 -10	3 /	45	141		* 30

3	2		TABLE	v.	Log	garithmic	Sine	es, Tangen	ts,		-		1
			0 Но				or			_	grees.		
m.	8.		Sine.	D.	Cosec.	Tang.	D.	Cotang.	Secant.	D.	Cosine.		m. s.
56	0		9.383675	844	10.616325		896		10.013096	52	9.986904		4 0
м	4		384182	843	615818 615313	397309 397846	896 895	602691 602154	013127 013159	53	986873 986841		56
	12		384687 385192	841	614808	398383	894	601617	013191	53 53	986809		49
100	16			840	614303		893	601081	013222	53	986778	-	52 48 44 40
100	20			839	613799	399455	892	600545	013254		986746		40
	24	6	386704		613296	399990	891	600010	013286	53	986714		36
ш	28		387207	837	612793	100000000000000000000000000000000000000	890	599476	013317	53	986683	53	32
	32		387709 388210		612291 611790	401058 401591	889 888	598942 598409	013349 013381	53	986651 986619		28 24
100	40		388711	834	611289	402124		597876	013413		986587	50	20
100	44	100	389211	833	610789	402656	886	597344	013445	53	986555		16
93	48	12	389711	832	610289	403187	885	596813	013477	53	986523	48	12
100		13	390210		609790	403718		596282	013509	53	986491	17	y 8
	_	14	390708	200	609292	404249	883	595751	013541	53	986459	-	4
57		1900	9.391206	828	10.608794		882		10.013573	53	9.986427	-	3 0
65	4		391703 392199	827 826	608297	405308	881	594692	013605	53	986395 986363		56
25		17	392695		607801 607305	405836 406364	879	594164 593636	013637 013669	54	986331		48
1 - 3		19	393191	824	606809	406892	878	593108	013701	54	986299		44
1-	20	20	393685	823	606315	407419	877	592581	013734	54	986266	40	40
		21	394179	822	605821	407945	876	592055	013766	54	986234	1000	36
		22	394673		605327	408471	875	591529	013798	54	986202	-	32
		23 24	395166 395658	820 819	604834 604342	408997	874	591003 590479	013831 013863	54	986169 986137		28
		25	396150		603850	410045	873	589955	013896	54	986104		20
2.0		26	396641	817	603359	A PRODUCTION OF THE PERSON NAMED IN	872	589431	013928		986072	1000	16
-		27	397132	817	602868	411092	871	588908	013961	54	986039	33	11
0		28	397621	816	602379	411615	870	588385	013993	54	986007		3
		29	398111	815	601889	412137	869	587863	014026	54	985974	_	
58			9.398600		10.601400	The second second	868		10.014058	54	9.985942		2 0
76		31	399088 399575	813	600912 600425		867 866	586821 586301	014091 014124	55	985909	-	56
20		33	400062	811	599938	THE RESERVE AND ADDRESS OF THE PARTY.	865	585781	014157	55 55	985876 985843	-	38
ш		34	400549		599451			585262	014189	55	985811		- 44
ш		35	401035		598965	415257	864	584743	014222	55	985778		40
8		36	401520		598480			584225	014255	-	985745		36
88		37	402005	1000000	597995	2 2 2 2 2		583707	014288	55	985712	-	32
ш		38	402489	806 805	597511 597028	416810 417326	861	583190 582674	014321 014354	55	985679 985646		25
п		40	403455	E 100	596545	100000000000000000000000000000000000000	Carrie	582158	014387	55	985613		20
и		41	403938	E-12-19	596062	The second second	100000	581642	014420		985580	100	16
w		42	404420	802	595580	418873	857	581127	014453		985547		18
•		43	404901	801	595099	419387	856	580613	014486		985514	100	- 8
-		44	405382	860	594618	the second second	855	580099	014520	-	985480		1.0
59		45	9.405862 406341	799 798	10.594138 593659		855		10.014553 014586		9.985147		1 0
10.		47	406820	797	593639		854	579073 578560	014619	56 56	985414 985381	-	59
1		48	407299	796	592701	421952		578048	014653		985347		48
	16	49	407777	795	592223	422463	851	577537	014686		985314	ш	40
1		50	408254		591746	Professional Autor A	and the	577026	the same of the State of	56	985280		1 40
1/2		51	408731		591269			576516		1000000	985247		34
1		52			590793		100	576007			985213		38
19.		54			590318 589843		The second	575497 574989	014820 014854		985180 985146		28 29
7		55			589368			574481			985113		TO
	44	56	411106	789	588894			573973	014921	56	985079	4	16
		57		20.00	588421			573466			985045	3	12
		58			587948			572959			985011	2	8
60		59 60			587476 587004			572453 571948	015022 015056		984978 984944	1 0	0 0
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m.	8	1	Cosine.		Secant.	Cotano		Tang.	Cosec.	-	Sine.	M	m. s.
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m.	S	=		_		9.668673	550	10.331327	10.042724	08	9.957276	60	90	0
40	0		9.625948 626219	451 451	10.374052 373781	669002	100	330998	042783	98				56
	8		626490		373510	669332		330668	012842	98				59
	12	3	626760		373240	669661	549	330339	042901	98				48
r	16		627030	450	372970	669991		330009	042960		957040			44
	20	5	627300		372700	670320		329680	043019					36
	24		627570		372430	670649		329351 329023	043079 043138		956921 956862			32
	28		627840 628109		372160 371891	670977 671306		328694	043197	99				28
	36		628378		371622	671634		328366						24
		10	628647		371353	671963		328037	043316	99				20
	44		628916		371084	672291	547	327709			956625	49		16
		12	629185		370815	672619		327381	043434					12
		13			370547	672947	546	327053	043494	12.0				4
	_	14	629721	446	370279	673274		326726	043553	_		-	10	0
41			9.629989	446	10.370011		546	10.326398		/ Section	9,956387 956327		19	56
	4		630257 630524	446	369743 369476	673929 674257		326071 325743	043673 043732	100				59
		17			369208	674584		325416	043792		1.72 2 to Minima			48
		19	631059		368941	674910		325090	013852	100	956148	41		44
К	20	20	631326		368674	675237	514	324763						40
		21	631593		368407	675564		324436						36
		22	631859		368141	675890		324110						32
10		23	632125		367875 367608	676217 676543	543	323783 323457						24
		24	632392 632658		367342	676869		323131	044211					20
		26		443	367077	677194		322806						16
۲.		27	633189	442	366811	677520		322480	044331					12
1	52	28	633454	442	366546	677846		322154	044391					8
	56	29	633719		366281	678171	542	321829					**	4
42			9.633984	441	10.366016				10.044512			30	18	56
1		31	634249		365751	678821		321179 320854	044572 044632		955428 955368			52
М		32	634514 634778		365486 365222	679146 679471	541	320534	044693		955307			48
		34	635042		364958	679795		320205	044753		955247			44
ь		35	635306		364694	680120		319880	044814		955186	25		40
		36	635570	439	364430	680444		319556	044874		955126			36
M		37	635834		364166	680768		319232	044935		955065 955005			32
		38	636097		363903	681092		318908 318584	044995 045056		954944			24
		39 40	636360 636623		363640 363377	681416 681740		318260	045117		954883			20
		41	636886	437	363114	682063		317937	045177		954823			16
Ш		42	637148		362852	682387		317613			954762			12
Г		43	637411	437	362589	682710		317290	045299		954701			8
	56	44	637673	437	362327	683033	538	316967	045360		954640			4
43			9.637935	436	10.362065				10.045421		9.954579	15	17	56
		46	638197		361803	683679		316321	045482 045543		954518 954457			52
		47	638458		361542 361280	684001 684324		315999 315676						48
	12	48	638720 638981		361019		537	315354	045665		954335	11		44
	20	50	639242		360758		537	315032	045726	102	954274			40
		51		434	360497	685290	536	314710	045787					36
	28	52	639764	434	360236			314388	045848	100	The second second			32
		53			359976	685934		314066						28 24
		54	640284	433	359716			313745 313423	045971 046032					20
		55 56			359456 359196			313102	046094					16
		57			358936	687219	535	312781	046155		953845	3		15
		58	641324	432	358676	687540		312460	046217	102		2		8
	56	59	641583	432	358417	687861	534	312139	046278		953722	1	10	4
44		60	641842	431	358158	688182	534	311818	046340	103	953660	=		0
m.	8,	7	Cosine.		Secant.	Cotang.		Tang.	Cosec.		Sine.	1	m.	5,
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44			TABLE	v.	Log	garithmic	Sine	s, Tangen	ts,					
			1 Ho	-			or			6 De				
m.	S.	_	Sine.	D.	Cosec.	Tang.	D.	Cotang.	Secant.	D.	Cosine.	_	m.	0
14	0		9.641842	431	10.358158 357899	9.688182 688502	534 534	10.311818 311498	046401		9.953660 953599	60	95	56
	8	2	642101	THE OWNER OF THE OWNER OWNE	357640	688823	534	311177	046463	a become	953537			52
	12	3	642618		357382	689143	533	310857	046525		953475	57		48
	16	4	642877	430	357123	689463	533	310537	046587		953413			41
	20	5	643135		356865	689783	533 533	310217 309897	046648		953352 953290	55 54		36
	24 28	6	643393 643650	1723 2	356607 356350	690103 690423	533	309577	046772		953228			3
	32	8	643908		356092	I TOTAL PROPERTY.	532	309258	04683	NE SHARROWS	953166			28
	36	9	644165		355835	100 mm		308938	046896		953104			2
	40	10	644423	1000000	355577	691381	532	308619	046958		953042 952980	-		2
	44		644680 644936		355320 355064	79 SARRO	531 531	308300 307981	047020	ALC: UNKNOWN	952918			1
		13	645193	1000000	354807	333555	531	307662	04714		952855			B
		14	645450	1000	354550	4424	0200	307344	04720		952793	16	17	13
15	0	15	9.645706	427	10.354294	9.692975	531	10.307025	10.04726	9 104		45	15	T)
		16	645962		354038			306707	04733			-	100	5
	8		646218	1000000	353782 353526	100000000000000000000000000000000000000	100000	306388	100000000000000000000000000000000000000	AND PARTY OF THE PARTY OF	7404564	-	17	5
		18 19	646474 646729	1000000	353371	1 1000 1000 1000	AUGUS.	306070	THE PERSON NAMED IN		Carlo Carlo Carlo		12	4 4
	20		646984	DOM:	353016			305434	A CONTRACTOR OF THE		76 CO 313 CO C	204	1	4
	24	21	647240	425	352760	694883	529	305117	04764	4 104	952356	39	F	3
	-	22	647494	50000	352506	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	529	304799	1000000000				10	3
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N	1000	21	648004 648258		351996	I PERFORM CO.		304164	1.0000000000000000000000000000000000000		1 (202222			2
		26		100000	351488	A STATE OF THE PARTY OF THE PAR	ALC: UK	303530	The second second second		100000000000000000000000000000000000000		м	î
Ŷ		27	648766	423	351234		528	303213				33	н	1
		28	The second second	503	350980	A SECURITION OF THE PERSON NAMED IN	10000	302897		Mark Broker	11/2/2000			
4	-	29		-	350726		-	302580					12.	į
46			9.649527		THE RESERVE AND PERSONS ASSESSED.	9.697736	10000	THE R. P. LEWIS CO., LANSING, MICH.	10.04820	(A) (B) (B) (B)	POTA OFFICE		14	P
		31	649781 650034		350219			301947		70 March	The second second			5
-		33		100000	349713	100000000000000000000000000000000000000		30131	The second second		12000000	(1000		4
ú		34		2073	34946	A PARTY AND A CO.	N 6000	of the latest terminal to the latest terminal te			THE PROPERTY.	26		K
я		35			349208	The second second	1000000	100000000000000000000000000000000000000	Call March 1					E
В		36		100000	348956 348703	The state of the s	E STATE OF							20.00
я		38		11 2020	34845	CONTRACTOR OF THE PARTY OF THE	10000		1 1 1/1-19(pc/-con		24200			3
п		39		1000	348200	CONTRACTOR OF THE PARTY OF THE	77000	100000000000000000000000000000000000000	A CHARGO NA		A CONTRACTOR OF			3
п	200	40	1 1 1 1 1 1 1 1 1 1 1 1 1		347948	A STATE OF THE PARTY OF THE PAR	1000000	The state of the s	0 0000000000000000000000000000000000000					B
15		41		1100000	34769	C TOTAL CONTRACTOR	17/0/200	100000000000000000000000000000000000000		-				ŀ
L		42		5000	34744									ĥ
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47	-	1 45	9.653308	418	10.34669	9.702466	524	10.29753	10.04915			15	13	ī
1		46	653558	417	34644	702780	523	The second second second			950778	14		A 600
		47		8 11000000	39553	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	Tribute.	100000000000000000000000000000000000000	100 000 000					1
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8	. 4		-	1-	Secant.	Cotang.		Tang.	Cosec.		Sine.	1	m.	
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5	or	"	3	45	190	3	45	238	3	45	47	1	or	*
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	-		_		-		an	d Sec	nts.		TA	DLE V.		45
_		_	_	1 Ho	AIF.			or		2'	7 De	grees.		
D.	_	8.	1	Sine.	D.	Cosec.	Tang.	D.	Cotang.	Secant.	D.	Cosine.	′ n	D. 8.
18	-	히	딝	9.657047	413	10.342953	9,70716	520		10.050119	107	9.949HH1	80 1	2 0
~		4	ĭ	657295		342703	707478		292522			949810		86
		8	9	657542		342458			292210			949752		82
		5	3	657790	412	342210	708109	520	291898	050318	108	949688		48
		16	4	658037		341963			291586			949623		44
		90	5	658284		341716			291274	050448		919558		40
			6	658531		341469			290963			949494		36
		8	7	658778		341222			290651			949489		32 28
		32 36	8	659025 659271		340975 3407 2 9			290340 290029			949364 949300		24
			เฝื	659517		340483			289718			949235		20
			iĭl	659763		340237	710593		289407			949170		16
	4		12	660009		339991	710904		289096			949105		18
			13	660255		339745			288785			949040	17	8
	å	66	14	660501	409	339499	71152	517	288475	051025	108	948975	16	4
19		0	15	9.660746	409	10.339254	9.711830	517	10.288164	10.051090	108	9.948910	15 1	1 0
		4	16	660991	408	339009	712146	517	287854	051155	108	948845		56
			17	661236		338764	712456		287544			948780		52
			18	661481		338519			287234			948715		48
			19	661726	1	338274	713076		286924			918650		44
			20	661970		338030			286614			918584		40
			2! 28	662459		337786 337541	713690 714003		286304 285995			948519 948454		36 38
			23	662703		337297	71431		285686			949388		25
			24	662940		337054			285376			948323		24
			25			336810			285067					20
			26	663433		336567			284758			948198		16
	4	18	27	663677		33632 3	71555	514	284449	051874	109	948126	133	12
			28	663920	1	336080			284140			948060		8
		56	29	664163	405	335837	71616	514	283832	052005	110	947995	31	4
50				9.664400	1	10.335594		514		10.052071				
			31	664648		335352			283215					56
			35	664891		335109			282907			947797		52
			33			334867			282599			947731		44
			34 35	66537 <i>5</i> 665617		33462 <i>5</i> 334383			282291					44
			36	665859		334141			281983 281675			947533	21	36
			37	666100		333900			281367					32
			38			333658			281060					28
			39			333417			280752					24
	4	10		666824	401	333176	71955	512	280445	052731	110			20
		ļŀ		66706	1	332935			280138					16
			42			332695			279831			947136		12
		52	1			332454			279521			947070	D	8
_	_	56	_	667786		332214			279217			947004		4
51		0		9.668087	1	10.331975			10.278911					9 0
			46			331733			278604			946871		56
		_	47	668506 668746		331494 331254			278298			946804 946738		52
			48 49			331014			277991 277685			946671		48 44
			50			330778				4.0000	111	946604	lio	40
		24	51	669464		330536	72292		277079				9	36
	1	28	82	669703	398	330297	72323		276768	053529	111	946471	8	32
	:	32	53	669942	398	330056	723 53		276462	053596	111	946404	7	28
			54	670181	397	329819	72384	509	276156	053663	4111	946331	6	24
			55			329581			275851					20
			56			329342			275546					16
			57			329104			275241					12
			58 59			328866			274936					. 8
52			60			328628 328391			274631 274326					8 0
		=	<u> </u>		_			===					*= :	
ė	_	8.	′	Cosine.		Secant.	Cotang.		Tang.	Cosec.	<u>i</u>	Sine.	Ľ	m. s.
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P	. 1	Р.	to	1.	15"		1.	15"			15"	16	P.	P. to
		DT		2	30	181	2	30	151		30	33		ar "
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3	2		TABLE		Lo	garıthmic		es, Tangen					
m.	S.	11	O Ho	ur,	Cosec.	Tang.	D.	Cotang.	Secant.	D.	grees.	I A II	n. 6
56	0		9.383675		10.616325		896	10.603229		52	9.986904	60	4 (
30	4		384182		615818		896	602691	013127	100000	986873	59	56
	8	2	384687	842	615313		895	602154	013159		986841	58	50
	12				614808			601617	013191	Biological Co.	986809	57	46
	16		385697		614303			601081	013222		986778		4
	20		386201 386704	839 838	613799 613296		892	600545 600010	013254 013286		986746 986714	55	3
	28		387207	887	612793		890	599476	013317	DOM:	986683		3
	32		387709		612291	401058	889	598942	013349		986651	100	2
	36		388210	835	611790	401591	888	598409	013381	53	986619	51	2
	40	1000	388711	834	611289	THE RESERVE OF THE PERSON NAMED IN	887	597876	013413	Long I	986587		2
	44	200	389211	833	610789		886	597344	013445		986555		1
		12	389711	832	610289 609790	403187 403718	885	596813 596282	013477 013509	53 53	986523 986491	47	1
		14	390708	DOM:	609292	404249	883	595751	013541	53	986459	10041	
57	-	-	9.391206	828	10.608794		882	-	10.013573		9.986427	-	3
(H)		16	391703	827	608297	405308	881	594692	013605		986395		5
24		17	392199	826	607801	405836	880	594164	013637	-	986363		5
	12	18	392695	500000	607305	406364	879	593636	013669		986331	42	48
		19	393191	824	606809		878	593108	013701	54	986299		4
		20	393685	823	606315			592581	013734		986266		40
	Booking	55	394179 394673	822	605821 605327	407945	876 875	592055 591529	013766 013798		986234 986202	1001	30
		23	395166	10000000	604834	and the latest and th	874	591003	013831	54	986169		9
		24	395658	819	604342		874	590479	013863		986137	36	2
	40	25	396150	818	603850	410045	873	589955	013896	54	986104	35	20
		26	396641	817	603359			589431	013928		986072		10
		27	397132	817	602868	The second secon	871	588908	013961	54	986039		11
		28	397621	816	602379	411615	870 869	588385	013993	Booker	986007		. 3
0.0	_	29	398111 9.398600	815	601889		_	587863	014026	PRODUCT	985974	31	
58	0	30	399088	813	10.601400 600912	DESCRIPTION OF THE PERSON OF T	868	586821	10.014058 014091	54	9.985942 985909	30	2 1
	- 100	35	399575	1202	600425	THE PERSON NAMED IN		586301	014124	55 55	985876	2251	51
		33	400062		599938		865	585781	014157	55	985843		48
		34	400549	2000	599451	414738		585262	014189	55	985811	26	4
		35	401035	1000	598965	No. of Street,	864	584743	014222		985778		40
		36	401520	1000000	598480	The property of the last	40.000	584225	014255	Butter	985745		36
		37	402005 402489	PK 24	597995 597511	416293 416810	862	583707 583190	014288 014321	55	985712 985679	23	31
		39	402972	40 to 241	597028		860	582674	014354		985646	21	25
		40	403455	10.00	596545		859	582158	014387		985613	DOM: N	20
		41	403938	803	596062	418358	858	581642	014420	55	985580		10
		42	404420	IEEE/CODE	595580	A STATE OF THE PARTY OF THE PAR	Contract of the Contract of th	581127	014453	-	985547	18	11
		43	404901	801	595099		856	580613	014486		985514		- 5
59	_		405382	-	594618		855	580099	014520	Market	985480		1
19		46	9.405862 406341	799 798	10.594138 593659		855 854	579073	10.014553 014586	-	9.985447 985414	15	1 (
		47	406820	1250.70	593180		100000	578560	014619		985381	13	55
0		48	407299	100000	592701	421952	852	578048	014653		985347	12	48
		49	407777	795	592223		851	577537	014686		985314	11	4
		50	408254		591746			577026		56	985280		44
		51	408731		591269			576516		The Control	985247		36
		52 53			590793 590318			576007			985213 985180		31
		54			589843			575497 574989			985146		2
		55			589368			574481	THE RESERVE AND ADDRESS OF		985113	5	20
		56	411106		588894			573973	The second second		985079	4	16
	48	57	411579		588421	INCOME STATE OF THE PARTY OF TH		573466	014955		985045	3	1 15
		58			587948			572959			985011	2	
20	56	59	412524		587476			572453			984978	1	2 3
60	_	60	412996	160	587004	428052	842	571948	015056	56	984944		0 0
m.	8.	1	Cosine.		Secant.	Cotang.	E i	Tang.	Cosec.		Sine.	10	n. 8
-			5 Ho		-		or				grees.		33
P.	P.	to	18	15"	122	Is	15"			15"	8	P. 1	P. to
8 0	200	"	3	30	244	2	30	260		30	16		OF A
			3 1	45	366	3	45	391	131	45	25	Sept.	

	_	_	1 17	_		and	Seca	nts.			BLE V.		33
n.	8.	/	1 Ho Sine.	D.	Cosec.	Tang.	D.	Cotang.	Secant.	D.	Cosine.	71	m .
0		=		_	10.587004		_						
U	4		9.412996 413467		586533			10.571948 571443	015090		984944		56
	8	1 2 3	413938		586062	429062		570938	015124	57	984876		55
	12	3	414408		585592	429566		570134	015158		984842		48
	16	4	414878		585122			569930	015199	57	984808		44
	20	5	415347		584653		838	- 569127	015226	57	981774	55	40
	21	6	415815	780	581185			568925	015260		984740		36
	28	7	416283	779	583717			568423			984706		35
	32	S	416751		583249			567921	015329		984672		29
	36 40	9	417217		582783 582316			567420 566920	015369 015397	100	984638 984603		20
	44		417684 418150		581850	100000000000000000000000000000000000000		566420			984569		10
	48		418615		581385	(a)		565920	Annual Control of		984535		15
	52		419079		580921	434579		565421	015500		984500		
	56		419544	200	580456	435078	830	564922	015534	57	984466	16	. 4
ī	0	15	9.420007		10.579993	9.435576	829	10.564424	10.015568	58	9.981432	45	59 (
	4	16	420470	771	579530	436073		563927			984397	44	50
		17	420933		579067			563430	015637		984363		5
	15		421395		578605			562933			984328		48
	16		421857		578143			562437			981294		4
	20		422318		577682			561941	015741		981259 984224		30
	24		422778		577222 576762	438554 439048		561446 560952	015776 015810	1.00	984190		
	32		423238 423697	100	576303			560457		100	984155		2
		24	424156		575844	The same of the same		559964			981120		
		25	424615		575385			559471	015915		984085		
	44	26	425073		574927		820	558978	015950	58	984050		
		27	425530	761	574470			558486			981015		
	52		425987		574013			557994	016019	No. of the second	983981		
_	56		426443		573557	442497		557503			983946	_	1
2			9.426899	759	10.573101			10.557012			9.983911		
		31	427354		572646			556521			983875		50
		32	427809		572191	443968		556032 555542	016160		983840 983805		5
	12		428263		571737 571283			555053	016193	1000	983770		4
	20		428717 429170		570830			554565	016265	113.24	983735		4
	24		429623	753	570377			554077	016300		983700		3
	28		430075	752	569925		L 100	553589	016336	59	983664	23	3
	32	38	430527		569473	446898	811	553102	016371		983629		2
	36		430978	751	569022			552616			983591		8
	40		431429		568571			552130		100	983558		1
	44		431879		568121	448356		551644	016477		983523		1
	48		432329		567671	448841		551159	016513		983487 983452		1
	52 56		432778		567222 566774			550674 550190	016548 016584	59	983416		
3		_	433226	-		-		10.549706		59	9.983381	-	-
3		46	9.433675 434122		10.566325 565878			549223		100	983345		
		47	434569		565431			548740		12.0	98330		
	12		435016		564984			548257	016727	1000	983273		
	16	-	435462		564538		1	547775	The second second second		983238		4
	20	50	435908	742	10 10 10 20 20 20			547294	016798	60	983202		40
	24		436353	741	563647			546813			983166		3
	28		436798	740	563202			546332			983130		
	32		437242		562758			545852			983094		28
	36		437686		562314			545372			983058		2
	40		438129		561871			544593 544414			983022 982986	1	1
	48		438572 439014		561428 560986			543936			982950		1
	52		439456		560544			543458	017086		982914	2	
	56		439897		560103			542981	017122		982878		
4		60	440338		559662			542504			982848		56 (
-	_	_	Cosine.				==			-	Sine.	7	m. 8
a.	8.	_			Secant.	Cotang.	0=	Tang.	Cosec.	De	grees.		
_	-	_	4 Ho		1 114	1.	0r	1 100		15"	1 9		-
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	or	"	3 /	45	311	3	4.5	368	3	45		1	8 01

48	TABLE	-	Log	garithmic	Sine	es, Tangen			-		
- 1.61	2 Ho	-	C	T.	or	I Corner I		-	grees.	1.' m	
m. s.	Sine.	D.	Cosec.	Tang.	D.	Cotang.	Secant.	D.	Cosine.	==	
0 0 0	9.698970 699189		10.301030 300811	761731	486	10.238561 238269	06254				56
8 2	699407	1200	300593	762023	486	237977	06261		1000000		52
12 3	699626	10000000	300374	762314		237686	06268			_	48
16 4 20 5	699844 700062		300156 299938	762606 762897	485	237394 237103	06276 06283				44
24 6	700280		299720	763188	485	236812	06290	284,000	125000000		36
28 7	700498	363	299502	763479	485	236521	06298	1 122	937019		32
32 8	700716		299284			236230	06305				28
36 9 40 10	700933 701151	(Decision)	299067 298849	764061 764352	485	235939 235648	06312 06320				20
44 11	701368		298632	764643		235357	06327		I CONTROLL S		16
48 12	701585	1 - 0 -	298415	764933		235087	06334				18
52 13 56 14	701802		298198 297981	765224 765514		234776 234486	06342 06349	310000	The second second		8
	9.702236		10.297764		-	10.234195	112000	Contract of the last	THE RESERVE AND ADDRESS.		9 0
4 16	702452		297548	766095		233905	06364				36
8 17	702669	360	297331	766385		233615	06371	6 123	936284	43	52
12 18	702885	THE REAL PROPERTY.	297115	Section in the second section		233325	06379				48
16 19 20 20	703101		296899 296683			233035 232745	06386 06393				44
24 21	703533	The latest and the la	296467	767545		232455	06401		100000000000000000000000000000000000000		36
28 22	703749	359	296251	767834		232166	06408		THE PERSON NAMED IN	-	32
32 23	703964		296036			231876	06416			-	28
36 24 40 25	704179 704395	1000000	295821 295605	768414 768703	100000	231586 231297	06423 06430				20
44 26	704610		295390		1000000	231008	100000000000000000000000000000000000000				16
48 27	704825	1000000	295175	The Part of the Pa		230719	06445		935513	33	12
52 28	705040	10000000	294960	The second second		230430		THE CHARLES	THE RESERVE OF THE PARTY OF THE		8
56 29	705254		294746	769860	COMMON	230140	06460	4 5000	The same of the same of		-
2 0 30	9.705469 705683		10.294531 294317			10.229852 229563	06475				56
832	705898		294102			229274	06482	2 200 8	THE RESERVE TO SERVE		52
1233			293888			228985	06490			27	48
16 34	706326	The second	293674	0.0000000000000000000000000000000000000		228697	06497				44
20 35 24 36		Name and	293461 293247	771592 771880		228408 228120	06505 06512				36
28 37		100000	293033	100000 C C C C		227832	06520		A P P P P P P P P P		32
32 38			292820	The second second		227543	06527				28
36 39			292607			227255					24
40 40			292394 292181	773033 773321		226967 226679	06542 06550	0.000	The second second		20
48 42			291968	Charles Street, et al.		226392	06557	0.000	1100000000		12
52 43			291755			226104	06565		934349		8
56 44		-	291542		_	225816	06572	Marie Contract	THE REAL PROPERTY.		-
100	9.708670		10.291330	THE RESIDENCE OF THE PARTY OF T		10.225529					
4 46 8 47		PAGE 18	291118 290906	100,000,000,000,000		225241 224954	06587 06595	OF REAL PROPERTY.	CONTROL STATES		56
12 48		and the same of	290694	The state of the state of		224667	06602				48
16 49	No. of Concession, Name of Street, or other Publisher, Name of Street, Name of	1	290482			224379	06610				44
20 50 24 51			290270	200000000000000000000000000000000000000		224092	06617			10	36
28 52			290059 289847			223805 223518		9 126	933747	1000	32
32 53	710364	352	289636				06640				24
36 54			289425								24
40 55			289214								16
48 57	The second second		289003 288792				The Control of the				12
52 58			288581			221799					8
56 59	711629		288371	778488	477	221512	06685	9 126	933141	1	
4 0 60	Name of Street,	350	288161	778774	477	221226		4 126	933066		
m. s. '			Secant.	Cotang.		Tang.	Cosec.		Sine.	' m	
	3 H	_	1		or		_	_	grees.		
P. P. to	1 2	30	107	2	15"	72	1 2	30	37	P. P.	
sor"	3	45	161	3	45	217	3	45	56	5.01	"
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_	_	_				and	d Seca	ints.			BLE V.		61
_		7	Sine.	ours,	1 Corne	1 Town	D.	1 Catoria		_	egrees.		h-
_	6.	-		D.	Cosec.	Tang.	-	Cotang,	Secant.	D.		Ľ	m.
	0	0	9.73610					10.187482	10.076409				
	8	2	73630					187206					
	12	3	73649				200	186930 186653					
	16	4	73688					186377	076737				
	20	5	73708		262920			186101	076819				
	24	6	73727					185825					
	28	7	73746		262533	81445	2 460	185548	076984	137			3
	335	8	73766	322	262339			185272		100			
	36	9	73785		262145			184996					1 7
		0	738048		261952			184721					
		1	73824		261759		10000	184445					
		13	738434	200	261566 261373			184169 183893					
_	56		73882	10000	261180			183618	077569	100			4
-3			9.73901		10.260987	-	_	10.183342		-		-	47
2	4	6	739200		260794		100000	183067	077728				
3	81	7	739396		260602			182791	077811				
3	121	8	739590		260410			182516	077894				
3	16 1	9	739783	320	260217			182241	077977				
7	20 2		73997		260025			181965	078060				
3	24 2		740167		259833			181690	078143				
-	28 2		740359		259641			181415	078226 078309				
b.	36 2		740550		259450 259258			181140 180865	078393				
41	40,2		740934		259066			180590	078476				
	44.2		741128		258875	819684	4 14 24	180316	078559				
1	48 2		741316		258684	819959	10000	180041	078643				
1	52 2	8	741508		258492	820234		179766	078726	139			
1	56,2	29	741699	318	258301	820508	457	179492	078810	139	921190	31	
1114	0,3	0	9.741889	318	10.258111	9.820788		10.179217	10.078893	139			
1	43		742080		257920			178943	078977				
9.	8,3		742271		257729	821332		178668	079061				5
R I	123		742462		257538	821606		178394 178120	079144				45
1	163		742842		257348 257158	821880 822154		177846	079228 079312				40
1	243		743033		256967	822429		177571	079396				3
	28 3		743223		256777	822703		177297	079480				39
	323		743413		256587	822977		177023	079564				28
•	363		743602		256398	823250		176750	079648				2
	404		743792		256208	823524		176476	079732		920268		20
•	414		743982		256018	823798	(6.75 TH	176202	079816		920184		16
	484	-	744171		255829 255639	824072	10000	175928 175655	079901		92009		
	564		744361 744550		255450	824345 824619		175381	079985 080069		920015 919931		4
15		-	0.744739	-	10.255261		-	10.175107	_	-	_	15	
100	44	- 8	744928		255072	825166	10.00	174834	080238		919762		
1	84		745117		254883	825439		174561	080323		919677		52
1	124		745306		254694	825713		174287	080107		919593		48
1	164		7.45494		254506	825986	100	174014	080492		919508	u	44
1	20 5		745683		254317	826259		173741	080576		919424		40
1	24.5		745871		254129			173468	080661		919339		35
1	28 5		746060 746248		253940 253752	826805 827078		173195 172922	080746 080831		919254 919169	7	39
1	36 5		746436		253564	827351		172649	080915		91908à		24
1	40 5		746624		253376	827621		172376	081000		919000	5	20
1	44 5		746812		253188	827897		172103	081085		918915	4	16
1	48 5		746999	313	253001	828170		171830	081170		918830	3	12
1	52 58	3	747187	315	252813	828442	454	171558	081255	142	918745	2	8
	56 59		747374		252626	828715	454	171285	081341		918659	1	. 4
16	060		747562	315	252438	828987	454	171013	081426	142	918574	0	
m.	S. '	1	Cosine.		Secant.	Cotang.		Tang.	Cosec.		Sign		п. в.
			3 Hou	urs,			or			Deg			
P	P 40	1	15	15"	48	18	15"	69 1	10 1 1	81 1	I Lorente		to
	P. to	ı	2	30	95	3	30						10
	-	1	3	45	143	3	45_	4					-

3	2		TABLE	V.	Lo	garithmic	Sine	es, Tangen	ts,		1		
			0 Но		1).		or				grees.		
m.	S		Sine.	D.	Cosec.	Tang.	D.	Cotang.	Secant-	D.	Cosine.		m. 8.
56			9.383675		10.616325		896		10.013096	DOM:	9.986904		4 0
123		1 1			615818			602691	013127		986873		56
9	15	3 3		842 841	615313 614808	The second second second		602154 601617	013159 013191	Description	986841 986809		52 48
72	10			840	614303	The second second		601081	013222		986778		44
110	20			839	613799	A CONTRACTOR OF THE PARTY OF TH		600545	200000000000000000000000000000000000000	10000	986746		40
	24	1 6	386704	838	613296		891	600010			986714	54	36
ш	28			837	612793			599476	013317	117200	986683		32
10	32				612291	401058		598942	013349		986651		28
100	36		THE RESIDENCE OF THE PERSON NAMED IN	835	611790	A	888	598409 597876		53	986619 986587	-	24
14		10		833	611289 610789			597344	777777	10000	986555		20
713		12		832	610289	THE RESIDENCE OF THE PARTY OF T	885	596813			986523		18
10		2 13			609790			596282	013509	200	986491	-	100 8
1	56	3 14	390708	830	609292	404249	883	595751	013541	53	986459	16	4
57	(15	9.391206	828	10.608794	9.404778	882	10.595222	10.013573	53	9.986427	Lō	3 0
May .		16			608297	405308		594692			986395		56
1		17		826	607801	405836		594164	THE RESERVE AND ADDRESS.		986363	-	1 52
100		18		825	607305 606809		740000	593636	The second second		986331 986299		48
00		20			606315	A STATE OF THE PARTY OF THE PAR		593108 592581	013701		986266		40
011		21	394179		605821	THE RESIDENCE AND ADDRESS.		592055			986234		36
1		22	394673		605327	408471	875	591529	The second secon		986202		32
172		23			604834			591003			986169		28
000		24			604342			590479			986137		24
107		25			603850			589955	Contract Contract		986104		20
63		26	THE COURSE PROPERTY AND	817	603359 602868			589431 588908	013928 013961		986072 986039		16
0		28		816	602379		4 40 40	588385	013993	Block and	986007	100	9
M		3 29		815	601889	The second second	869	587863	The second second		985974		- 4
58	_	-	9.398600	_	10.601400	9.412658	868		10.014058	THE REAL PROPERTY.	9.985942	-	2 0
20		131			600912	Management of the Control of the Con		586821	014091		985909		56
20		32			600425	ALCOHOLD IN THE	CALCAL CO.	586301	014124		985876		58
33		2 33	A STATE OF THE PARTY OF THE		599938	Total Control of the		585781	014157	Bolod	985843		48
533		6 34			599451	200000000000000000000000000000000000000		585262	The second second		985811		44
10		35	I I LOUDSCHALL A		598965 598480		864	584743 584225	100000000000000000000000000000000000000		985778 985745		36
2		8 37			597995			583707			985712		38
ш		2 38			597511	The second second		583190			985679	-	28
100	30	6 39	402972	805	597028	417326	860	582674	014354	55	985646	21	24
а		0 40			596545			582158			985613		20
н		441			596062			581642			985580		16
ш		8 42 2 43		802	595580 595099		857	581127 580613		No.	985547 985514		11
и		6 44			594618	The second second	855	580099	200 200 200		985480		
59	_		9.405862		10.594138		_		10.014553	90	9.985447		1 0
1		4 46	EAST-COLD STORY	798	593659		1000000	579073			985414		56
-		8 47	110703555		593180		10000	578560			985381		59
1		2 48			592701	421952	852	578048	100000000000000000000000000000000000000		985347		48
1		6 49	100000000	795	592223			577537			985314	-	48
-		0 50			591746			577026		56	985280	10	46
=	2	4 51 8 52	408731 409207		591269 590793			576516		56	985247 985213	30	36
		2 53			590793								32
2		6 54			589843								
1		0 55			589368			574481			985113		20
	4	4 56	411106	789	588894	426027	845	573973	014921	56	985079	-4	16
		8 57			588421						985045		12
1		2 58			587948			572959			985011		1 8
60		6 59			587476 587004			572453 571948				1	0 0
	_			100			0.00	-		90			===
m.	5	. 1	PO DATE OF		Secant.	Cotang.	1	Tang.	Cosec.		Sine.		m. 8-
=		- 4	5 Ho	_	1	-	or				grees.	-	11
		to	1 10	15"	122	1:	15"			15"	8	P	P. 10
5	or	"	3	30	366	3	30	260		30 45	25		or "
-				40	200		10	100	1 4	-	1 20	_	

-		-	1 Ho	ur-			Seca				grees.	-	33
n.	8.	7	Sine.	D.	Cosec.	Tang.	D.	Cotang.	Secant.	D.	Cosine.	11	m. 8.
Ö	0	0	9.412996	785	10.587004		819		10.015056	57	9 98 1944		
•	4	ĭ	413467	784	586533		841	571443		100	984910		56
	8		413938		586062			570938	015121	57	984876		52
	12	23	414408	783	585592	429566	839	570131	015158	57	984842	57	48
	16	4	414878	782	585122			569930			984808		44
	20	5	415347	781	584653			569127	015226		981774	55	40
	24	6	415815	780	584185			56H925			984740		36
	28	7	416283	779	583717			568423			984706		38
	38	S	416751	778 777	583249			567921 567420	015328 015362		984679 984638		21
	40	9	417217	~	582783 582316			566920		57	984603		20
	44		417684 418150		581850			566420			984569		10
	48		418615	774	581385	434080		565920	1000 000 000	100	984535		19
	52		419079	773	580921	434579		565121	015500		984500		
	56		419544	773	580456	435078		564922	015534	57	984466		4
1	0	1.5	9.420007	772	10.579993	9.435576	829	10.564421	10.015568	58	9.981432	45	59 (
П	4	16	420470	771	579530	436073		563927			984397		50
	8	17	420933	770	579067	436570	858	563430	015637	58	984363		52
	15	18	421395	769	578605			562933	015672	58	984328	18	46
	16		421857	768	578143			562437	015706		981294		44
	20		422318	767	577682			561941	015741	58	984259		40
	24		422778	767	577222			561446	100 200 5 5 7 7 7	1000	984224		36
	28		423238	766 765	576762			560952 560457	015810 015845		984155		35
	36		423697 424156		576303			559964			984120		2
	40		424615	763	575844 575385			559471	015915		984085		20
	44		425073	C2127	574927			558978	015950		984050		16
	48		425530	761	574470			558486	m 2015 to 1 1/2 1		981015		13
	52		425987	760	574013	TO 4 7 3 2 1 1 1 1		557994			983981		9
	56		426443		573557	442497		557503			983946		4
2			9.426899		10.573101	9.442988	817	10.557012	10.016089	58	9.983911	30	58 (
Т	4	31	427354		572646	443479		556521	016123	58	983875		56
	8		427809		572191	443968	400000	556032	016160	59	983840		59
	12:	33	428263		571737	444458		555542	016195		983805		48
	16		428717	755	571283	444917	814	555053	016230		983770		44
	20		429170	754	570830	445435	813	554565	016265		983735		40
	24		429623		570377	445923		554077	016300	100	983700		30
	28		430075		569925			553589			983664		38
	32		430527	752	569473			553102		59	983629		25
	36		430978		569022	447384		552616	016406	7.6	983591 983558		10
	44		431429		568571	447870		552130		59 59	983523		16
	48		431879		568121	448356 448841		551644 551159			983487		18
	52		432329	748	567671			550674	016548	59	983452		
	56		432778 433226		567222 566774			550190	016584	59	983416	16	4
3		-				-			10.016019	59	9.983381		
3	4		9.433675 434122		10.566325 565878			549223	016655	59	983345		56
	8		434569		565431	451260		548740		59	98330		5
	12		435016	G-0 (3)	564984	11 at 2 to 2 to 3 to 3 to 3		548257	016727	60	983273	12	48
	164		435462		564538			547775		60	983238		4.4
	20		435908					547294	016798	60	983202	10	40
	24				563647	453187		546813		60	983166		36
	28	52	436798		563202			546332	016870	60	983130	8	32
	32		437242	740	562758	454148	799	545852			983094		28
	36		437686	739	562314			545372	016942		983058		24
	40		438129		561871			544893			983022		20
	44		438572		561428			544414		0.31	982986		16
	48		439014		560986			543936	017050		982950		18
	52 /		439456		560544	456542	796	543458	017086		982914 982878		4
	56 8				560103	457019	795	542981	017122		982848		56 0
4	06	-1	440338	_	559662	457496	794	549504		60			-
n.	8.	1	Cosine.	-	Secant.	Cotang.	-	Tang.	Cosec.		Sine.	1	n. s.
_			4 Ho			TO 27.0	or			_	grees.		
D		. 1	15	15"	1114	15	15"	123		15"	9	10	P. to
	P. t		2	30	228	2	30	245		30	11		8 OF "
	or .		3 /	45	311	3	45	368	3 \	45	/ 56	1	

3	14		TABLE	V.	Lo	garithmic	Sine	es, Tanger	700				
			1 Ho			I Mana	or	I Catana			grees.		
m.		-	Sine.	D.	Cosec. 10.559662	Tang.	D.	Cotang.	Secant. 10.017158	D.	Cosine.	=	m. s
4	0	1	9.440338 440778		559222		CO E.	542027	017195		9.982842 982805		56
	8	2	441218	732	558782			541551	017231	61	982769	58	58
	18				558349 557904	INVESTIGATION AND INVESTIGATION		541075 540600	017267		982733 982696	57 56	48 44 40 36 32 28 24 20 16
	20				557465	The second second	10000000	540125	017340		982660		40
н	24	6	442973	1000000	557027			539651	017376		982624	54	36
	28	7	443410 443847		556590 556153		789 788	539177 538703	017413 017449	-	982587	53	32
	36	8 9	444284	DESCRIPTION OF THE PERSON OF T	555716	I TO THE COLUMN	100000	538230	017486		982551 982514		28
	40		444720	726	555280	462242	787	537758	017523	61	982477		20
1	44	11	445155	1000000	554845			537286	017559	10401	982441		16
1	48		445590 446025	100000	554410 553975	463186 463658	785 785	536814 536342	017596 017633	-	982404 982367		12
1	20.7		446459	100000	553541	464128	784	535872	017669	-	982331		4
5	0	15	9.446893		10.553107		783	10.535401	10.017706	61	9.982294	45	55 0
1	4	16	447326		552674	1000 C 200	783	534931	017743	10000	982257		56
	12	17	447759 448191	720	552241 551809	465539 466008	782	534461 533992	017780 017817	62	982220 982183		52 48 44
	16		448623	149 200 31	551377	466476	780	533524	017854		982146	41	44
			449054	DOM:NO	550946	466945	780	533055	017891	62	982109	10	
	24		449485		550515	467413	779	532587	017928		982072	39	40 36 32 28 24 20 16
	28	23	449915 450345		550085 549655	467880 468347	778	532120 531653	017965 018002		982035 981998	38	32
	36		450775	1000000	549225	468814	777	531186	018039		981961	36	24
	40		451204		548796		776	530720	018076		981924	35	20
		26	451632 452060		548368 547940	469746 470211	775	530254 529789	018114 018151		981886	34	16
	48	-	452488		547512	The second second second		529324	018188	62	981849 981812	33	12
	56		452915		547085	471141	773	528859	018226		981774	31	Ĭ.
6	0	30	9.453342	710	10.546658	9.471605	773	10.528395	10.018263	63	9.981737	30	
1	-	31	453768		546232	472068	772	527932	018300		981700	29	56 52 48 44
	12		454194 454619	1000000	545806 545381	472532 472995	771	527468 527005	018338 018375		981662 981625	97	52
ı	16		455044	10000000	544956		770	526543	018413		981587	26	44
	20	35	455469	707	544531	473919	769	526081	018451	63	981549	25	40
	24	-	455893		544107	474381	769	525619	018488	63	981512	24	36
	28	38	456316 456739		543684 543261	474842 475303	768	525158 524697	018526 018564	63 63	981474 981436	23	40 36 32 28 24 20 16
	36		457162		542838	475763	767	524237	018601	63	981399	21	24
			457584		542416	476223	766	523777	018639	63	981361	50	20
	44	41	458006		541994 541573	476683	765 765	523317	018677	63	981323	19	
		42	458427 458848	701	541152	477142 477601	764	522858 522399	018715 018753	63 63	981285 981247	17	12
		44	459268		540732	478059	763	521941	018791	63	981209	16	4
7			9.459688	699	10.540312	9.478517	763	10.521483	10.018829	63	9.981171	15	
1		46	460108	698	539892	478975	762	521025	018867	64	981133	14	56
1	12	47	460527 460946	698	539473 539054	479432 479889	761 761	520568 520111	018905 018943	64	10 4 10 10 10 10 10 10	13	48
1		49	461364	696	538636	480345	760	519655	018981	64		11	44
1	20	50	461782		538218	480801	759	519199	019019	64	980981	10	40
	24	59	462199		537801	481257 481712		518743	019058 019096		980942	9	36
1	28		462616 463032		537384 536968	482167		518288 517833	019096		980904 980866	7	32 28 24 20
1	36		463448		536552	482621	757	517379	019173	64	980827	6	24
1	40		463864		536136	483075		516925	019211		980789	5	20
1	44		464279 464694		535721 535306	483529 483982		516471 516018	019250		980750 980712	4 3	16
	52		465108		534892	484435		515565	019327		980673	2	18
	56	59	465522	689	534478	484887	753	515113	019365	64	980635	2	4
8	0	60	465935	688	534065	485339	753	514661	019404	64	980596	03	5 0
m.	8.	-	Cosine.		Secant.	Cotang.		Tang.	Cosec.		Sine.	1 0	De - B
-	-	-	4 Hot		1 100 1		or 1 ##	1 110 1		Deg 5"	grees.		21
	P. te	0	2	15" 30	106	2	30	231		0	19		P. 10
80	r"	1	3	45	319	3	45	347		5	28	80	2"
-											50000		125

			- 1			and Secants.			TABLE V.				53
2 Hours,						or			35 Degrees.			_	
n.	8.	"	Sine.	D.	Cosec.	Tang.	D.	Cotang.	Secant.	D.	Cosine.	17	m s.
20	0	=	9.758591	301	10.241409	0 845997	449	10 154779	10.086635	147	9 019965	=	
	4	ĭ	758772	100000	241228	845496		154504	086724		913276		56
	8	9	758952		241048	845764		154236	086813		913187		52
	12				240868			153967	086901	0.00	913099		48
	16	4	759312		240688	the beautiful to		153698	086990		913010		44
	20	5	759492		240508			153430	087078		912922		40
	24	6	759672		240328	846839		153161	087167		912833		36
	28	7	759852		240148			152893			912744		32
	32	8	760031	299	239969	847376		152624	087345	148	912655	52	28
	36	9	760211	299	239789	847644	447	152356	087434	148	912566	51	24
	40	10	760390	299	239610	847913	447	152087	087523	148	912477	50	20
	44	11	760569		239431	848181	447	151819	087612	148	912388		16
	48		760748	298	239252	848449	447	151551	087701	149	912299	48	12
	52		760927		239073	848717	447	151283	087790	149	912210	47	8
	56		761106		238894	848986	447	151014	087879	149	912121	46	4
1	0	15	9.761285	298	10.238715	9.849254	447	10.150746	10.087969	149	9.912031	45	39 0
Ē		16			238536			150478	088058		911942	44	56
		17	761642	297	238358	849790		150210	088147				52
		18			238179			149942	088237	149			48
		19		297	238001	850325	446	149675	088326				44
		20			237823	850593	446	149407	088416	149			40
	24		762356		237644			149139					36
		22	762534		237466			148871	088595				32
		23			237288			148604	088685				28
	-	24			237111	851664		148336	088774				24
		25	763422 763600	296 296 295	236933 236755 236578 236400	852199 852466 852733	446	148069	088864			34 33 32	20
		26						147801	088954		910956 910866		16
		27					445	147534	089134	150			12
		28						147267					8
ш		29			236223	853001	445	146999	089224	_	910776	_	4
22			9.763954		10.236046	9.853268	445	10.146732	10.089314	150			38 0
		31		295	235869			146465	089404				56
		32			235692			146198	089494				52
		33			235515			145931	089585				48
		34			235338			145664	089675	151	910325		44
		35			235162			145397	089765		910235	25	40
		36			234985			145130	089856		910144	24	36
		37	1113377		234809			144863			910054		32
		38	1,7 2,000,000		234633			144596	090037		909963	22	28
		39			234456			144329	090127		909873	51	24
		40	100 00 00 00 00 00		234280			144062			909782		
	(40)				234104			143796			909691		16
		43	100000000000000000000000000000000000000		233928			143529			909601		
		44	100000000		233753			143263			909510		8
-			766423		233577	857004		142996	090581		909419	_	4
23			9.766598					10.142730					
		46			233226			142463		200			56
		47			233051			142197					52
		48			232876			141931	090945				
		4.9			232700			141664					
		50 51			232525								
		52			232351			141132					36
		53			232176 232001			140866					32
		54			231827			140600 140334					28 24
		55			231652			140068					20
		56			231478			139802					16
		57			231478			139536				-1	12
24		58			231129			139270					8
		59			230955			139005	091859				4
		60			230781			138739			The second second second		36 0
	_	=		200			110	-				=	
n.	8.	1	Cosine.		Secant.	Cotang.		Tang.	Cosec.		Sine.	1	m 8,
			3 Ho	urs,			or		54	De	grees.	-	- + - 7
P.	P	to 1	15	15"	44	18	15"	67		15"	22	la	0 -
	or		2	30	88	2	30	133	2	30	45	1,	" 10 B
		13.7	3	45	133	3	45	200	3 1	45	10		200

3	6		TABLE	v.	Log	arithmic	Sine	s, Tangen	ts,				
			1 Ho	_	0	m	or	Cotons		_	grees.		
m.	8.		Sine.	D.	Cosec.	Tang.	D.	Cotang.	Secant.	D.	Cosine.		m. 8
12	0	0	9.489989 490371		10.510018 509629	9.511776 512206	716	10.488224 487794	10.021794 021835	68 68	9.978206 978165	59	18 (
п	8	2	490759	1000	509241	512635	Section 201	487365	021876	68	978124	58	59
	12	3	491147	ALC: NO	508853	513064	714	486936	021917	69	978083	1000	48
п	16	4 5	491535	244	508165	513493 513921	714	486507 486079	021958 021999	69 69	978042 978001	56 55	40
100	24	6	491922	A WOOD	508078 507692	514349	100000000	485651	022041	69	977959	54	36
	28	7	492695	644	507305	514777	712	485223	022082	69	977918	53	39
100	32	8	493081	-	506919	515204	0.000	484796	022123 022165	69	977877	.52	28
100	36	9	493466 493851	-	506534 506149	515631 516057	711	484369 483943	022206	69	977835	51	24
	44	11	494236	200	505764	516484	0.000	483516	022248	69	977752	100	16
10	48	12	494621	641	505379	516910	4 (0.252)	483090	022289	69	977711	48	12
ш	52	13	495005	000	504995	517335		482665	022331 022372	69 69	977669 977628	Marie 1	8
100	56	14	495388		504612		708	482239 10.481815	The second second	69	9.977586	46	47 0
13	4	16	9.495779 496154	-	10.504228 503846			481390	022456	70	977544	45	47 0 56
20	_	17	496537	-	503463	519034	2003000	480966	022497	70	977503	Total Control	52
10	12		496919		503081	519458		480542	022539	70	977461	15	48
10	16		497301	ACC IN	502699		A COLUMN TO A COLU	480118 479695	022581	70	977419	41	44
ю	20	100	497688		502318 501936			479272	022623 022665		971377	40 39	36
и	28		498444	1000000	501556	20000000	704	478849	022707	70	977293	38	32
п	32		498825		501175	521573		478427	022749	70	977251	37	28
	36		499204	400	500796		10.750	478005	022791	70	977209	36	24
1	40		499584		500416 500037	522417 522838	702	477583 477162	022833 022875	70	977167	35	20
10	48		500348	A PERSONAL PROPERTY.	499658	523259		476741	022917	70	977083	33	12
1	52	28	500721	631	499279	523680		476320	022959	70	977041	32	8
	56	_	501099		498901	524100	The state of the s	475900	023001	70	976999	31	- 4
14			9.501476	Take a	10.498524		District of the last	10.475480 475061	10.023043 023086	70	9.976957	100	
	4	31	501854	SCHOOL STREET	498146 497769			474641	023128	70	976914 976872	29	56
b		33	502607	- Carrie	497393			474222	023170		976830		48
12	500	34	502984		497016		12000	473803	023213	Total Control	976787	26	44
100		35 36	503360	10000	496640 496265		THE OWNER OF THE OWNER, WHEN	473385 472967	023255 023298		976745		36
		37	503735	4 Exercise	495890	Carlot Contracts	696	472549			976702	100	32
	32		504485	Take of	495515	1 3 3 5 5 6 6 6	The same of	472132	200 200 000	and the same	976617	laber 1	28
	36		504860	- Carlo	495140			471715	2222222	1000	976574		24
п	40	1000	505234	10000	494766	THE PERSON NAMED IN	100000	471298 470881	0.0000000000000000000000000000000000000	1000	976532		20
п	44	41	505608	THE REAL PROPERTY.	494392 494019			470465	023511 023554	71	976489		12
		43	506354	a proper	493646			470050	023596	-	976404		8
2	56	44	506727	621	493273	530366	692	469634	023639	71	976361	16	4
15			Hardward Control of the Control of t		10.492901		691	10.469219	-0104000	71	9.976318	lander of	
100	8	46	507471 507843	10000	492529 492157	531196 531611	I BOOK SAL	468804 468389	023725 023768	100000	976275 976232	2004	39
100	12	мм	508214	10000	491786		A Distriction of	467975	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	72	976189	-	48
123	16	-	508585	200	491415	III POR MANAGEMENT	10000000	467561	023854	The last	976146	Mark I	44
100	20	PH 1	508956	- War	491044	100000	Jana	467147		72	976103	Miles	40
10.		51	509826		490674 490304			466734			976060		32
п		53			489935			465908			975974	7	28
Ш		54			489566			465496			975930	6	25
111		55			489197			465084			975887		26
1		56 57			488828 488460			464672 464261	024156 024200		975844 975800		16
1		58	0.0000000000000000000000000000000000000		488093			463850			975757		8
14	56	59	512278	612	487725	536561	684	463439	024286	72	975714	1	4
16	0	60	512642	615	487358	536972	684	463028	024330	72	975670	_	_
m.	8.	1	Cosine.		Secant.	Cotang.		Tang.	Cosec.		Sine.		III. A
			4 H	_			or				grees.		
	P. 1		15	15"		10	15"			15"	10	P.	P. to
80	75 4	1	3	30	189 283	3	30 45	210	2 3	30	31		or "
	-	-	-	40	6013	-		010			-	_	

_						and	Seca	nts.	-		BLE V.		37
n.	8.	1	1 Ho Sine.	ur,	Cosec.	Tang.	D.	Cotang.	Secant.	D.	grees.	11	m.
6	0	_		_	10.487358				10.024330	=		_	_
	4		513009		486991			462618			975627		5
	8		513375		486625			462208		73	975583		5
	12		513741		486259			461798		73	975539	67	4
	16		514107		485893			461389			975496		4
	20		514472		485528			460980			975452		4
	24		514837		485163 484798			460571 460163			975408 975365		3
	32		515202 515566		484434			459755			975321		2
	36		515930		484070			459347			975277		2
		10	516294		483706			458939	024767	73	975233		2
		11	516657	605	483343			458532			975189	49	1
		12	517020		482980			458125	The state of the s		975145	48	1
		13	517382		482618			457719			975101		
		14	517745		482255	and the second s	_	457312		_	975057	_	_
7					10.481893				10.024987	73			
	4		518468		481532			456501			974969		5
		17	518829 519190		481171 480810			456095 455690		8.5	974925 974880		5
		19	519190		480449			455285			974836		4
		20	519911		480089			454881			974792		4
		51	520271	600	479729	545524	673	454476			974748	39	3
		22	520631		479369			454072			974703		3
		23	520990		479010			453669			974659		2
		24	521349		478651			453265			974614		2
		25			478293 477934			452862 452460			974570 974523		2
	44	26			477576			452057			974481		
		28			477219			451655		100	974436		
	56	1			476862			451253			974391		
8		-		_	10.476505		669		10.025653	_	9.974347	_	42
•		31	523852		476148			450450		2.01	974302		5
	8	32	524208		475792			450049			974257	28	5
	12	33	524564		475436	550352	667	449648			974212	27	4
		34	524920		475080			449248			974167		4
		35	525275		474725			448848			974122	25	4
		36	525630		474370			448448			974077	24	3
		37 38	525984 526339		474016 473661			448048 447649			974032 973987		3
		39	526693		473307			447250			973942	21	2
		40	527046		472954			446851			973897	50	9
	41		527400	100000	472600			446452			973852		ì
	48	42	527753	588	472247	553946	663	446054	026193	75	973807	18	1
		43	528105		471895			445656			973761	17	
	56	14	528458	587	471542	551741	662	445259	026284	76	973716	16	
19			9.528810		10.471190				10.026329		9.973671		
	4		529161		470839	100000000000000000000000000000000000000		444464			973625		5
		47	529513		470487		(F. F. F. F.	444067			973580 973535	13	5
		48		12 6 6	470136 469785		660 660	443671 443275			973489		4
		50			469435			442879			973444		4
		51	530915	584	469085			442483			973398	9	3
		52	531265		468735			442087			973352	8	3
	32	53	531614		468386	558308	658	441692			973307	7	2
		54			468037			441298			973261		2
		55			467688			440903			973215		2
		56			467339			440509			973169		1
		57 58			466991 466643			440115 439721			973124 973078	-	1
		59			466296			439327			973032		
20		60			465948			438934					
	_	-		==			==		===	=	Sine.	=	_
n.	S.	7	Cosine.	1170	Secant.	Cotang.	OF	Tang.		D ₁	grees.		m.
-	_	_	1º	15"	1 00	1 10 1	or 15"	1 100		15"	111	-	2
	P.		2	30	178	3	30	200		30	58	15	.P.
	or	"	3	45	268	3	45	301	13	45	1 84	-	8 01

44	T			TABLE	v.	Log	garithmic	Sine	s, Tangen						1
	1	1	/ •	1 Hou	-	Cosec.	Tang.	or D.	Cotang.	Secant	D.	Cosine.	, 1	m. s	ł
m.	8			Sine.	D.			-	10.311818		-	THE OWNER WHEN			ò
14		1	0 9	9.641842 642101	431	10.358158 357899	688502	534	311498	046401		953599		5	
		3	2	642360	431	357640	688823	534	311177	046463	100000	953537		5	
	1		3	642618	430	357382	689143	533	310857	046525	103	953475	57	4	
	1	6	4	642877	430	357123	689463	533	310537	046587	March of	III belle research related	56	4	
	20		5	643135	430	356865	689783	533	310217	046648		953359 953290	55	3	
	2		6	643393 643650	430	356607 356350	690103 690423		309897 309577	046710	e comme		53	3	
ш	3	-	8	643908	429	356092	690742	532	309258			I INCOME STATE OF	52	2	
10	3	-	9	644165	429	355835	691062	532	308938			953104	51	2	I
10	4	о в	0	644423	428	355577	691381	532	308619	120200000000000000000000000000000000000		100000000000000000000000000000000000000	50	2	
11.	4		I	644680	428	355320	691700		308300 307981	047020		952980 952918	49 48	_	6
9		8 1		644936 645193	428	355064 354807	692019 692338	531 531	307662		140000	952855	17		94 0
		6 1		645450	427	354550	692656	531	307344	100000000		952793	16		4
45	_	0 1	_	9.645706	427	10.354294		531	The second second	10.047269		9.952731	45	15	Ö
		on.	6	645962	426	354038	693293	530	306707			1 2 2 2 2 2 LOS	44	5	6
		8	17	646218		353782	693612	6450	306388	THE RESERVE OF THE PERSON NAMED IN	3 10000	14-74-50-17	-	5	
		2		646474	2220	353526	A DESIGNATION OF THE PERSON OF		306070	THE RESERVE OF THE PARTY OF THE		I WAS A COLUMN	700		
	-	6 1	20	646729 646984	722	353271 353016	694248 694566	530	305752	The second second	7727	200000	40	4	Ó
	- 23	4		647240		352760	100000000000000000000000000000000000000	TO SECO.	305117	200,000,000,000		1000000000	-		6
		8		647494		352506	THE RESIDENCE OF THE PARTY OF T	529	304799	100000000000000000000000000000000000000			191	3	
	3	2	23	647749		352251			304488	The second second					8
п		6	-	648004		351996	1000 CO.		304164	The second second					I
18		4		648258 648512	1993331	351742 351488	100000000000000000000000000000000000000	10000	303847	1215522					0
18		8		648766	2000	351234	The second second	100000		11112/06/23	3 0 30	2 44 66	33		2
10		2		649020	100000	350980	100000000000000000000000000000000000000	0.776	302897		-	DE LA COMPANIE	-		98
и		6		649274	422	350726	697420	527	302580	04814	6 103	951854	31	-	4
46		0	30	9.649527	422			527	10.302264	10.04820	9 105	9.951791		14	U
100		-	31	649781	422	350219	123355	23000	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1					_	56
0			32	650034	100000	349966	100000000000000000000000000000000000000	DOG:	1 TO SEC. 10.	The second second second					58
13			$\frac{33}{34}$	650287 650539	110000	349713 349461	The second second		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1					_	18 44
12			35		41 573 01	349208	The second section is			100000000000000000000000000000000000000		The Real Property lies		_	40
	2	4	36	651044	420	348956	699632	526		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1			24		36
п			37	651297	112020	13.72			111111111111111111111111111111111111111						32
			38	651549	100000	The second second	TANKS THE CO.	4000	1 TO 1 TO 1 TO 1 TO 1	100/00/00					28
			39		10.00000	100000000000000000000000000000000000000		10000	100,000,000	A CONTRACTOR OF THE PARTY OF TH				_	24
п		ж	41	652304	100000	1111233	A STATE OF THE PARTY OF THE PAR	1/20/20		22000		A PROPERTY OF THE PARTY OF THE	100		16
12		•	42	652555	418	347445	a management of the same	1000000	The second second	100000000000000000000000000000000000000	a 1000				12
п		del	43			The second second	4 IIII Andrewski	1 1000000	11112220000	The state of the s					8
-	_	9	44	653057	-						Marie Parley				E.
47			45	9.653308 653558	10000000	A STATE OF THE STA	A CONTRACTOR OF THE PARTY OF TH			10.04915				13	0
1			47		11/2/2012	100.0000000	C CONTRACTOR OF THE PARTY OF TH		100000000000000000000000000000000000000	100000000000000000000000000000000000000			1 140		56 58
	3		48		200	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	A STATE OF THE PARTY OF THE PAR	100000	122900		DE MOOR	412414			48
	E	16	49	654309	416	345691	703729	523	29627	04941	4 10	950586		1	41
16			50			100000000000000000000000000000000000000									40
			51												36
			53											1	21
			54												21
			55	655805	415	344193	705603	521	29439	04979	8 10	950209	5		20
			56			75,775,755	THE RESERVE AND ADDRESS OF THE PARTY NAMED IN	A 100 0000	15000501100		100 100000	The second second			16
			57												12
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48			60											12	d
m						Secant	Cotang.		Tang.	Cosec.		Sine.		m.	
-	-	-	-	4 He	HIPE	Octant.	Colang.	or	Tang.	-	63 D	egrees.	-	ans.	-
1	-			1 10 1	15"	63	1 1 1	15	7 79	1 19 1	15"	0	1		
P. 5		- 1		2	30	127	2	30	158	2	30	31		P. t	
0	01		1	3	45	190	3	4.5		3	45	47	1	or "	

							81	nd Sec	ents.		Ť	ABLE V.	_	39
Н		_		1 H	our,			OP				OFFICES.		
ń	-	1	1	Sine.	D.	Cosec.	Tang.	D.	Cotang.	Secant.	I D.		1	D (
前温		하	₹	9.554329	548	10.44567	9.5841	77 629	10.415825	10.02984	81	9.97015	1	
_		4	1	55465E					100.0000					· 5
		В	2	554987		445019								5
	1	2	3	555315		444683						970006		4
	10		4	855643 855971		444951 444029						969957 969909		44
	2		ď	556299		443701		89 6 2 7				969860		30
	28	8	7	55662 6		443374		5 626				969811		3
	31		9	556953		443047		0 626				969762		28
	30		9	557280 557606		442720		6 625				969714 969665		24 20
	44			557932		442394 442068		1 625 6 625						16
	48	. 1 – 4		558258		441742								11
	51	11:	3	558583	542	441417		6 624				969518		8
_	_	14	-	<i>5</i> 58909		441091	58944			030531	85			4
15				.559234		10.440766				10.030580		9.969420		
		10		559558		440442			409818		,	969370		56
	12	12		559883 560207	540	440117 439793	59056 59093		409438 409065			969321 969272		51 46
		19		560531	539	439469	59130		408692			969223		44
	20	2(560855	539	439145	59168	1 621	408319	030827	82	969173	40	40
	24			561178	538	438822			407946	_		969124		36
		22		561501	538	438499			407574			969075 969025		32 28
		25		561824 562146	537 537	438176 437854			406829			968976		24
		2		562468		437532			406458			968926		20
	44	2(5	562790	536	437210	59391	4 618	406086		83	968877		16
	48			563112		436888			405715		,	968827		12
	52	28		563433 563755		436567	59465		405344 404973		1	968777 9687 2 8		4
6		30	_	564075	535 534	436245 10.4359 2 5				10.031322		9.968678		
		31		564396	534	435604			404232			968629		- 56
		32			533	435284	59613		403862			968578		52
	12			565036	<i>5</i> 33	434964	59650		403492	031472	83	968328	27	48
	16				532	434644	596878		403122	031521	83	968479	6	44
	20 24			565676 565995	532 531	434324 434005	59724 59761		402753 402384	031571 031621	83	9684291 9683791		40 36
	28			566314	531	433686	59798		402015	031671	83 83	968329		32
	32			566632	531	433368	59835		401646	031722	83	968278		28
	36			566951	530	433049	59872		401278	031772		968228		24
	40			567269	530	432731	59909		400909 400541	031822 031872	84	968178 9681 2 8		50
	44 48			567587 567904	529 529	432419 432096	59945 59982		400173	031922	84 84	968078		16 12
	52			568222	528	431778	60019		399806	031973	84	968027		8
	56				528	431461	60056		399438	032023	84	967977	6	4
7	0	45	lo.	568856	528	10.431144	9.60092	611	10,399071		84	9.967927		
	4	46		569172	527	430828	601296	1 1	398704	032124	84	9678761	-1	56
	8	47			527	430512	601669		398338	032174 032225	84	9678 2 61		52
	12 16				526 526	430196 429880	602029 60239		397971 397605	032275	84	967725		48
	20	1		570435		429565	602761		397239	032326	84	9676741	o	40
	24	51	ı	570751		429249	603127		396873	032376	84	967624	9	36
•	28	52	1	571066		428934	603493	609	396507	032427	84	967573	- 1	32
	32 36	53	1	571380		428620	603858		396142	032478 032529	85		7	28
	40	5.5	ł	571695 572009		428305 427991	604223 604588		395777 395 4 1 2	032579	85		5	24 20
	44	56	ı	572323		427677	604953		395047	032630	85		4	16
	48	57	1	572636	522	427364	605317	607	394683	032681	85		3	12
	52	58	1	572950		427050	605682		394318		85		2	8
8	5 6	59 60		573263		426737	606046		393954	032783 032834	85		1 0 38	6
_	=	_	<u>!</u>	573575	221	426425	606410	606	393590		55		בבוב	
<u>.</u>	6.	,	-	Cosine.		Secant.	Cotang.	11	Tang.	Cosec.		D	7	•
_			_	4 Hou		1 60		or				Tees.		
	P. 1		1	2	15" 30	80 160	2 2	1 <i>5"</i> 3 0	93		N	18 (
8 (DT	7		3	45	240	3	45	185		45	\ ³⁵ \		
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3	8		TABLE	/ 1 1 1	Log	garithmic	Sine	s, Tangen			200		-
-		17	1 Ho	D.	Carre	Tang.	D,	Catown			grees.		
m.	S		-		- Cosec.	-		Cotang.	Secant.	D.	Cosine.		m. s
50		0 0	I AMERICAN STREET	578 577	10.465948 465601		655	10.438934 438541	10.027014 027060	77	9.972986	50 59	40 (
100				100 2021	465255		654	438149	027106	77	972894	58	59
160	15				464908		653	437756		-	972848	57	48
16	20			W-100-00	464562	The second second	653	437364 436972	027198 027245		972802	56	44
100	24			2 7 12	464217 463871		200	436581	027291	77	972709	55	36
110	28	3 7	536474	574	463526	563811	652	436189	027337	77	972663	53	35
90	32		THE RESIDENCE OF THE PARTY OF T		463182			435798	100000000000000000000000000000000000000		972617	52	28
83	36		III I TO THE PARTY OF THE PARTY	573 573	462837 462493	The second second	Brighten	435408 435017	027430 027476	77	972570 972524	51	24
67	44	M MODE	THE RESIDENCE OF THE PARTY OF T	572	462149	THE RESIDENCE AND ADDRESS OF THE PARTY OF TH	10000000	434627	027522	77	972478	19	16
11		12	538194		461806		649	434237	027569	78	972431	18	19
		13	0,00000		461462 461120		649 649	433847 433458	027615 027662	78	972385 972338	17	1 5
21	_	1000	538880 9.539223	570	10.460777		648	10.433068	-	78	9.972291	16	20 6
-		16		570	460435	The second second second	648	432680	027755	78	972245	14	50
100		3 17	539907	569	460093	567709	647	432291	027802	78	972198	13	52
		18	540249		459751		647	431902	027849	78		12	48
10		19	540590 540931	568	459410 459069	100000000000000000000000000000000000000	646	431514 431127	027895 027942	78	972105 972058	41	- 44
20		21	541272	567	458728	100000000000000000000000000000000000000	645	430739	027989	78	THE BUILDING S	39	36
66		8 22	541613		458387	569648	645	430352	028036	78	The state of the latest the	38	39
10		23	541953		458047		645	429965	028083	78	MINISTER STREET, STREE	37	28
23		25	542293 542632	565	457707 457368	570422 570809	644	429578 429191	028130 028177	78	971870 971823	36	24
23		26	542971	565	457029		643	428805	028224	78	971776	34	16
11		3 27	543310	564	456690		643	428419	028271	79	971729	13	12
9		28	543649	564	456351	571967	642	428033	028318	79	971682	32	8
99	-	29	543987	563	456013	THE RESERVE OF THE PARTY OF	642	427648	028365	79	971635	31	3
22		31	9.544325 544663	563 562	10.455675 455337	573123	642	10.427262 426877	028460	79	9.971588 971540	303	56
20		32	545000		455000	THE RESERVE OF THE PERSON NAMED IN	641	426493	028507	79	971493	18	58
55		233	545338	561	454662	III CONTRACTOR OF THE PARTY OF	640	426108	028554	79	971446	27	46
99		34	545674		454326		640	425724	028602	79	971398	26	44
120		36	546011 546347	560	453989 453653	574660 575044		425340 424956	028649 028697	79 79	971351 971303	24	40
98	28	37	546683		453317	575427	639	424573	028744	79	971256	23	36
98		38	547019	559	452981	575810	638	424190	028792	79	971208	22	28
100		39	547354	558	452646	576193	638	423807	028839	79	971161	21	24
77		41	547689 548024	557	452311 451976	576576 576959	637	423424 423041	028887 028934	79 80	971113 971066	20	20
88		42	548359	557	451641	577341	636	422659	028982	80	971018	18	12
10		43	548693	556	451307	577723	636	422277	029030	80	970970	17	- 8
00	_	44	549027	556	450973	578104	636	421896	029078	80	970922	16	- 4
23		46	9.549360 549693	555	10.450640 450307	9.578486 578867	635	10.421514 421133	029173	80	9.970874 970827	153	37 (36
1		47	550026	554	449974	579248	634	420752	029221	80	THE RESERVE OF THE PERSON NAMED IN	13	52
60	12	48	550359	554	449641	579629	634	420371	029269	80	970731	12	48
40		49	550692	553	449308	580009	634	419991	029317	80	97068	11	
1		50	551024 551356	553	448976 448644	580389 580769		419611	029365 029414	80	OTOFILE	10	40
1	28	52	551687					418851	029462		970535	8	31
100		53	552018	552	447982			418472	029510		970490	8	29
112		54	552349		447651			418093	029558		970442	5	24
100		55	552680 553010		447320 446990			417714	029606 029655	~	970394	4	20 10
100		57	553341		446659			416957	029703		970297		
	52	58	553670	549	446330	583422	630	416578	029751	81	970249	3 2 1	, 8
24		59. 60	554000		446000 445671	583800		416200	029800		970200		0 4
	8		554329	040	-	584177	029	415823	029848	21	970158	03	_
m.	-	1	Cosine.		Secant.	Cotang.	-	Tang.	Cosec.	-	Sine.	' n	In -5.
-	P		4 Ho	_	1 94	l de l	or 15"	1 00 1		Deg	rees.	-	-
P.	T.	10	2 3	30	169	2	30	96		0	12		2, 10
		- 1	3	45	253	3	45	289		45	36	80	T "
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						and	Secs	nts.		TA	BLE V.		39
_			1 Ho	ur,	_		or		21	De	grees.		
m.	8.	1'	Sine.	D.	Cosec.	Tang.	D.	Cotang.	Secant.	D.	Cosine.	1	m. 1
24	0		9.554329	548	10.445671	9.584177	629	10.415823	10.029848	81	9.970152	60	36 5 5 4 4 4 3 3
•	4		554658		445342			415445	029897	81	970103	59	5
	8	2	554987		445013		628	415068			970055		5
	12	3	555315	547	444685	585309	628	414691	029994		970006		4
	16	4	555643		444357			414314			969957		4
	20	5	555971	546	444029		627	413938			969909		4
	24		556299		443701			413561			969860 969811		9
	28		556626		443374			413185 412810			969762		9
	32 36		556953		443047 442720			412434			969714		2
		10	557280 557606	544 543	442394			412059	E I 4 L L C	81	969665		2
	44	11	557932	543	442068			411684			969616		1
	48	12	558258	543	441742		624	411309		82	969567	48	1
	52		558583	542	441417		624	410934	030482	82	969518		1
	56	14	558909	542	441091	589440	623	410560	030531	85	969469	46	(300)
5	Ö	15	9.559234	541	10.440766	9.589844	623	10.410186	10.030580	88	9.969420		
	4		559558	541	440442	590188	623	409812	030630		969370		5
	8	17	559883	540	440117	590562	655	409438	Talk a North A		969321		5
		18	560207	540	439793	THE TAX BEING THE PARTY.	622	409065		-	969272		4
		19	560531	539	439469		622	408692	030777	88	969223	41	5 4 4 4
		20	560855	539	439145		621	408319	030827	82	969173 969124		3
	24		561178	538	438822		621	407946			969075		3
	28		561501 561824	538 537	438499 438176			407202			969025		9
		23 24	562146	537	437854		619	406829	1,000		968976		2
		25	562468		437532	The second second second	619	406458	200 200 200 200		968926		2
		26	562790		437210	and the second will be		406086			968877	34	1
		27	563112		436888		618	405715	031173	83	968827		1
	52	28	563433	535	436567	594656	618	405344			968777		
	56	29	563755	535	436245	595027	617	404973		83	968728		
26	0	30	9.564075	534	10.435925	9.595398	617	10.404602	10.031322	83	9.968678		34
	4	31	564396		435604		617	404232		83	968628		5
	8	32	564716	533	435284	596138	616	403862	031422	83	968578		5
		33	565036	533	434964		616	403492	031472	83	968528		4
		34	565356	532	434644		616	403122	031521	83	968479 968429		4
		35	565676	532	434324		615	402753 402384	031571 031621	83	968379		3
		36	565995	531	434005		615	402015	031671	83 83	968329		3
			566314 566632	531 531	433686 433368		615	401646		83	968278		2
	32	38 39	566951	530	433049	The second section of the	614	401278	CONT. AND COM.	84	968228		2
		40	567269	530	432731		613	400909		84	968178		2
		41	567587	529	432413			400541	031872	84	968128		1
	7.5		567904	100 C C 100	432096		613	400173		84	968078		1
		43	568222	528	431778	600194	612	399806		84	968027		
	56	44	568539	528	431461	600562		399438		84	967977		
7	0	45	9.568856	528	10.431144	9.600929	611	10,399071		84	9.967927		33
		46	569172	527	430828	601296	611	398704		84	967876		5
		47	569488	527	430512	601662	611	398338		84	967826		5
		48	569804		430196		610	397971	032225	84	967775		4
		49	570120		429880			397605	032275 032326	84	967725		4
	20	50	570135		429565			397239	The second second		967624		3
	24	51			429249			396873 396507	1 - A		967573		3
		52	571066		428934 428620			396142	****		967522		2
		53 54	571380 571695		428305			395777			967471	6	2
		55			427991	According to the contract of		395412	032579	85	967421		2
		56			427677			395047	032630		967370	4	1
		57			427364			394683	032681	85	967319		1
		58			427050	The second second second		394318	032732		967268		
	56	59	573263	521	426737	606046		393954		85	967217		29
28	0	60	573575	521	426425	606410	606	393590	032834	85	967166		32
n.	6	7	Cosine.		Secant.	Cotang.		Tang.	Cosec.		Sine.	'	m. s
-			4 Ho	urs.			or		68		grees.		
-	-		Ta' I	15"	1 80	1 1	15"	1 93		5"	1 12		
P.	P.	to	2	30	160	2	30	185		30	25		P. to
8	or	"	3	45	240	3	45	278		45	37	1	30 8

48	TABLE	V.	Log	garithmic	Sine	s, Tangen	ts,				
	2 Hot	-	0 1	m	or	0		30 De	47.	# / lm	
m. s.	Sine.	D.	Cosec.	Tang.	D.	Cotang.	Secant.	D.	Cosine.	m.	
0 0 0	9.698970 699189	364	10.301030 300811	761731	486	10.238561 238269	06254				56
8 2	The second secon	364	300593	762023	486	237977	06261		-0200233	-	59
12 3	699626	364	300374	762314	486	237686	06268	120 120 120 120	2/2/2/2/2/2		48
16 4	The second second	363	300156	762606	485	237394	06276		12 12 15 3 12 15		44
20 5	700280		299938 299720	762897 763188	485	237103 236812	06290		5.00007.03		36
28 7	700498		299502	763479	485	236521	06298		937019	53	35
32 8	700716	-	299284	763770	485	236230	06305	/11/19/04	The second second		28
36 9 40 10		362	299067	764061	485	235939	06312				24
44 11		362	298849 298632	764352 764643	484	235648 235357	06327	2012	100000000	THE REAL PROPERTY.	16
48 12	Section in the last terms of the	362	298415	764933	484	235067	06334				18
52 13	Control of the Contro	361	298198	765224	484	234776	06349	786.00	1 1 2 12 1 1 1 1 1 1 1	C DOOR HALL	8
56 14		361	297981	765514	484	231486	06349	erforces			
1 0 15			10.297764		484	10.234195	06364				56
4 16 8 17	702452	361	297548 297331	766095 766385	484	233905 233615	06304	CHEST	THE RESERVE		52
12 18	702885	360	297115	766675	483	233325	06379	0 123	936210	12	48
16 19		360	296899	766965		233035	06386	FIG. 600	10000000		44
20 20 24 21	703317	360	296683	767255	483	232745 232455	06393			DOM: USA	36
28 22	703533		296467 296251	767545 767834	483	232455	06408	COLUMN TO SERVICE AND ADDRESS OF THE PERSON NAMED IN COLUMN TO SERVICE AND ADDRESS OF	0.0000000000000000000000000000000000000		32
32 23	703964	10000	296036	768124	482	231876	06416	171 E100	IN COUNTY OF		28
36 24	704179		295821	768414	482	231586	06423		20000	C COLUMN	24
40 25			295605	768703		231297	06430	241072	700 7 7 10 10 10		20
44 26	704610	No. of London	295390 295175	768992 769281	482	231008 230719	06438 06445	24 545 5	TAL BUILDING		12
52 28		No.	294960	769570		230430	06453		10.000		8
56 29	705254	358	294746	769860	481	230140	06460	5 124	935395	31	4
100 TO 10	9.705469		10.294531	THE RESIDENCE OF THE PARTY OF T	481	10.229852					
431	705683	The state of the s	294317	770437	481	229563	06478	10000	The second second		56
8 32 12 33		100000	294102 293888	770726	481	229274 228985	06489				48
16 34	THE RESERVE AND ADDRESS.		293674	771303		228697	06497				44
20 35			293461	771592	481	228408	06505	9.17/20	THE PERSON NAMED IN		40
24 36 28 37		Name and	293247 293033	771880 772168	10000000	228120 227832	06518	E 100 E 2	PERCUR		36
32 38		DOM:	292820	772457	480	227543	06527				28
36 39			292607	772745	12230	227255	06535		A PERMITAL SOME		24
40 40	Annual Control of the	Report to the	292394	773033	100000	226967	06542	0.00	Total Control of the last		20
44 41 48 49	707819		292181 291968	773321	480	226679 226392	06550				16
52 43	The second secon	-	291755	773608 773896		226104	06565	2000	1000000		8
56 44			291542	774184	Market St.	225816					4
(T) (C) (C) (C) (C)	9.708670	354	10.291330		479	10.225529	10.06580	1 125			
4 46	Charles and the		291118	774759	479	225241	06587				56
8 47 12 48	THE RESERVE	Seekel high	290906 290694	775046 775333	479	224954 224667	06595 06602	OF THE REAL PROPERTY.	THE PERSON NAMED IN		52 48
16 49	100000000000000000000000000000000000000	1000000	290482	775621	478	224379	06610	1000	THE RESIDENCE		44
20 50	The second second	DOM:	290270	The second second second		224092	100/3220				40
24 51			290059	Section and to the fact							36
28 52 32 53			289847 289636								32 28
36 54			289425			222945					94
40 55	710786	351	289214	777342	478	222658	06655	5 126	933445	5	20
44 56			289003			222372					15
48 57 52 58			288792 288581	777915 778201		222085 221799					100
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4 0 60	THE RESIDENCE OF THE PERSON NAMED IN		288161	778774	1000000	221226					
m. s. /	Cosine.		Secant.	Cotang.		Tang.	Cosec.		Sine.	' m.	3
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							and	Seca	nts.		TA	BLE V.		61
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52	_	==	1	0.833783		10.166217		_		10.135873	-	_	=	8 0
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	1	2	2	834189		165811			029584	136226				48
	1	6	4	834325		165675		100000	029331	136344		863656	56	44
	20	0 .	5	834460	225	165540			029078	100 00 00 00 00 00	100	863538		40
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	2		7	834730		165270			028571	136699		863301		32
	3		8	834865	11/2/2015	165135			028318	The second second second				28
	3			834999		165001			028065 027812					24
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		61		835672		164328			026799	137529				4
3			-			10.164193				10.137647	-		_	_
		4 1		835941		164059			026293	137766				56
		81		836075		163925			026040	137885				52
		2 1		836209		163791			025787	138004				48
		6 1		836343		163657	THE RESERVE		025534	138123	198	861877	41	44
	20	0 2	o	836477		163523	974719	422	025281	138242				40
		12		836611		163389			025027	138362				36
		8 2		836745		163255			024774	138481				32
		2 2		836878		163122			024521	138600				28
		62		837012		162988			024268	138720				24
		02		837146		162854			024015	138839 138959				16
		82		837279 837412		162721 162588			023762 023509	139978				12
		22		837546		162454			023256	139198				8
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54	_	_	-1-	0.837812		10.162188			the second second	10.139438	-		-	
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		83		838078		161922			022244	139678				52
		23		838211		161789			021991	139798				48
	1	63	4	838344		161656			021738	139918		860082	26	44
		03.		838477	221	161523	978515		021485	140038		859962	25	40
		43		838610		161390			021232	140158				36
		83		838742		161258			020979	140279		859721		32
		23		838875		161125			020726	140399		859601		28
		63		839007		160993			020473	140520		859480 859360		24
		44		839140 839272		160860 160728			020220	140640 140761		859360		16
		84		839404		160596			019967	140761		859119		12
		24		839536		160464			019462	141002		858998		8
		64		839668		160332		1000	019209			858877		4
55	_	_	4		_	10.160200		-		10.141244	-		_	_
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		84		840064		159936			018450	141486	100	858514		52
		24		840196		159804			018197	141607				
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		0 5		840459		159541	982309		017691		202	858151		
		45		840591		159409			017438					36
		85		840722		159278			017186					
		2 5		840854		159146			016933					28
		65		840985		159015			016680					24 20
		45		841116		158884			016427	142457				16
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8	0		TABLE	v.	Lo	garithmic	Sine	s, Tangen	ts,				6
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100	20		100000000000000000000000000000000000000	44 %	274781	797194	1 3 3 4	202806	D10 (D11)	100,000	928025		4(
п	2		SUPPLY STATE OF		274580			202525			927946		3
ı	35			2000	274378	797755 798036	A real	202245 201964	THE PROPERTY OF		927867		3:
ı	36	9	726024	1020000	273976		4000	201684	TAX 100 TO 100 T	Interestation	927708	51	2
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	48	Ordina.	726426 726626	11220	273574 273374	798877 799157		201123 200843	1000010		927470		19
	52	13	726827	334	273173	799437	467	200563	072610	133	927390	LT	
1	-	14	727027	334	272973	The second second	467	200283	A COLUMN TO SERVICE AND ADDRESS OF THE PARTY	200		-	
9	4		9.727228 727428	10000	10.272772 272572		466	199723	10.072769 072849		9.927231		36
1	8	17	727628	333	272372		466	199443			927071		52
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		22	728626	-	271374		100000	198045			926671	-	32
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н		25	729223	262	270777	802792	100000	197208			926431	35	20
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100	52	27	729621 729820	331	270379 270180	803351 803630	465	196649 196370	073730 073810		926270 926190	33	12
١.		29	730018	330	269982	THE PERSON NAMED IN	V 100	196092	073890		926110	31	4
10	0		9.730217		10.269783		465	10.195813	10.073971	134	9.926029	30 5	
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0		32	730613 730811	330	269387 269189	804745 805023		195255 194977	074132 074212		925868 925788	28	52 48
п	16	34	731009	329	268991	805302	464	194698	074293			26	44
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	0.00	36	731404 731602	329	268596 268398			194141	074455 074535		925545 925465	23	32
×	32	38	731799	329	268201	806415	463	193585	074616	135	925384	22	28
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143	48	42	732587	328	267413	807527	463	192473	074940	135	925060	18	12
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11	_	_	732980 9.733177	MODES IN	10.266823	9.808361	463	191917	10.075184	DESCRIPTION OF	924897	154	9 0
1	4	46	733373	327	266627	808638	462	191362	075265	200400	9:4735	14	36
1		47	733569	327	266431	808916	462	191084	075346	136	924654	13	58
1	12	48	733765 733961	327	266235 266039	809193 809471	462	190807 190529	075428 075509		924572 924491	11	48
1		50		326	265843	809748	11/2/07/2019	190252	075591		924409	400	40
13		51	734353		265647	810025		189975	075672	136	924328	9	36
13		52 53	734549 734744		265451 265256	810302 810580		189698 189420	075754 075836		924246 924164	8 7	36 32 28 24 20
1	36	54	734939		265061	810857		189143	075917		924083	6	24
3	40	55	735135	325	264865	811134	461	188866	075999		924001	5	20
		56 57	735330 735525	325	264670 264475	811410 811687		188590 188313	076081 076163		923919 923837	3	16
и		58	735719		264281	811964		188036	076245		923755	2	8
1	56	59	735914	324	264086	812241	461	187759	076327	137	923673	1	8
12		60	736109	324	263891	812517	461	187483	076409	37	923591	0 48	
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554987 555315 555643 555971 556299 556626 556953	547	445342	584555	9.10.0	415445	029897	81	970103		5
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556626 556953	546	444029	586062		413938	030091		969909		4
556953	545	443701	586439		413561	030140		969860		3
100 100 100 100 100 100 100 100 100 100	545	443374	586815 587190		413185 412810	030189 030238		969811 969762		2
557280	544	443047 442720	587566		412434	030286		969714		2
557606		442394	587941	1000	412059	030335		969665		2
	543	442068	588316		411684	030384	-	969616		1
No. of the last of	543	441742	588691		411309	030433		969567	48	1
558583	542	441417	589066	624	410934	030482	82	969518		113
558909	542	441091	589440	623	410560	030531	82	969469	16	
559234	541	10.440766	9.589814	623	10.410186	10.030580	88	9.969420		
559558	541	440442	590188		409812	030630		969370		5
	540	440117	590562		409438	030679	-	969321		5
Section in Francisco	540	439793	590935	622	409065	030728		969272		4
	539	439469	591308		408692	030777	88	969223		4
	539	439145	591681	621	408319	030827 030876	82	969173 969124		3
	538 538	438822 438499	592054 592426	621	407946	030925	85	969075		3
	537	438176	592798	620	407202	030975	82	969025		2
	537	437854	593171	619	406829	031024	82	968976		2
	536	437532	593542	619	406458	031074	83	968926	35	2
	536	437210	593914	618	406086	031123		968877	34	1
	536	436888	594285	618	405715	031173	83	968827		1
	535	436567	594656	618	405344	031223	83	968777		
563755	535	436245	595027	617	404973	031272	83	968728		
564075	534	10.435925	9.595398	617		10.031322	83	9.968678		
	534	435604	595768	617	404232	031372	83	968628		5
564716	533	435284	596138	616	403862	031422	83	968578		5
	533	434964	596508	616	403492	031472	83	968528 968479		4
	532	434644	596878		403122	031521	83	968429		4
	532	434324	597247 597616	615	402753 402384	031621	83 83	968379		3
	531 531	434005 433686	597985		402015	031671	83	968329		3
AND DESCRIPTION OF THE PERSON	531	433368	598354	614	401646	031722	83	968278		2
	530	433049	598722		401278	031772	84	968228	21	2
	530	432731	599091	613	400909	031822	84	968178		2
	529	432413	599459		400541	031872	84	968128		1
	529	432096	599827	613	400173	031922	84	968078		1
18222	528	431778	600194		399806	031973	84	968027		
8539	528	431461	600562	612	399438	032023	84	967977		
8856	528	10.431144	9.600929	611		10.032073	84	9.967927		
9172	527	430828	601296		398704	032124		967876		
	527	430512	601662		398338	032174		967826	13	. 5
	526	430196	602029		397971	032225 032275		967775 967725	15	4
	526	429880	602395		397605 397239	032326	84	967674	11	4
1994	525	429565	602761		396873		84	967624		5
	525 524	429249 428934	603127		396507	032427		967573		3
	딿	428620	603858		396142	032478	85	967522	7	2
	523	428305	604223		395777	032529	85	967471		2
75	523	427991	604588		395412	032579	85	967421	5	20
1	523	427677	604953		395047	032630		967370	4	10
10	122	427364	605317	607	394683	032681	85	967319	3	12
72	150	427050	605682		394318	032732	-	967268 967217	2	8
		426737	606046		393954	032783			0 32	
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		ecant.	Cotang.		Tang.	Cosec.	1	Sine.	m	. 8
		-		or		68 1	regz			
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3	8		TABLE	v.	Log	garithmic	Sine	s, Tangen	ts,		We.	
		+	1 Ho	22.4		100	or			_	egrees.	
m.	8.		Sine.	D.	- Cosec.	Tang.	D.	Cotang.	Secant.	D.	Cosine.	60 40 (
20	4		9.534052 534399	578 577	10.465948 465601	MATERIAL PROPERTY.	The second	438541	10.027014 027060		9,972986	59 50
68	8	3 2	534745	577	465255	561851		438149			972894	58 5
м	18			577	464908 464562			437756 437364			972848	57 4
83	20		The second second second	20.00	464217	The second second	653	436972	027215	77	972755	55 4
	24				463871			436581 436189	027291	10000	972709 972663	54 3
13	32		536474 536818	574	463526 463182			435798	The second second	10000	972617	52 2
100	36		537163		462837	564599		435408			972570	51 2
93	40		537507 537851	573	462493 462149	1 2 1 2 2 2 2 2 2	4000	435017 434627	027476		972524 972478	50 20
68	48	12	538194	572	461806	565768	649	434237	027569	78	972431	18 1
60		13	538538		461462	100000000	THE RESERVE	433847 433458	027615	1000	972385 972338	17
21	_	14	538880 9.539223	570	461120			10.433068			9.972291	15 39 0
NA.	4	16	539565	570	460435		648	432680	027755	100000	972245	14 50
90		17	539907	569	460093			432291	027802	10000	972198	43 65
20		19	540249 540590	569 568	459751 459410	568098 568486		431902 431514	027849		972151 972105	12 45
100		20	540931	568	459069	568873	646	431127	027948		972058	40 40
933		21	541272 541613	567	458728 458387			430739 430352	027989 028036		972011	39 36 38 38
100		23	541953	566	458047	570035		429965	028083	1000	971917	37 28
62		24	542293	566	457707			429578	028130		971870	36 24
22		25	542632 542971	565	457368 457029		The Part of	429191 428805	028177		971823 971776	35 20 34 16
12	48	27	543310	564	456690	571581	643	428419	028271	79	971729	13 11
2		28 29	543649 543987	564	456351 456013	571967		428033 427648	028318 028365		971682 971634	32 8
22	_		9.544325	563	10.455675	STREET, SQUARE,		10.427262	STREET, SQUARE, SQUARE,	1	9.971588	30 38 0
100	4	31	544663	562	455337	573129	641	426877	028460	79	971540	29 56
64		32	545000 545338	562	455000 454662	THE PERSON NAMED IN		426493 426108	028507 028554	12770	971493	28 50
22		34	545674	561	454326	A STATE OF THE PARTY OF THE PAR	THE RESERVE	425724	028602	100000	971446 971398	26 44
94		35	546011	560	453989			425340	028649	100000	971351	25 40
99		36	546347 546683	560 559	453653 453317	THE RESIDENCE OF THE PERSON NAMED IN	1000000	424956 424573	028697 028744		971303 971256	24 36
90	32	38	547019	559	452981	575810	638	424190	028792	79	971208	22 28
20		39	547354 547689	558 558	452646 452311	576193 576576	ALC: UNKNOWN	423807 423424	028839 028887	400	971161	21 24
22		41	548024	557	451976	100000000000000000000000000000000000000	10000000	423041	028934		971066	19 16
10		42	548359	557	451641	577341	900000	422659	028982	1000	971018	18 18
2		43	548693 549027	556	451307 450973	577723		422277 421896	029030 029078		970910	17 8
23	0	45	THE RESERVE AND ADDRESS OF THE PERSON NAMED IN	555	10.450640	9.578486	635	10.421514		1	9.970874	15 37 0
11	4	46	549693	555	450307 449974			421133	029173	100001	970827	14 56
1		48	550026 550359	554	449641	579248 579629		420752 420371	029221		970779 970731	13 51
11	16	49	550692	553	449308	580009	634	419991	029317	80	97068	11 44
10		50	551024	553	448976 448644	BODWAR	000	419611	029365 029414	100	4446	10 40
	28	52		552	448313	581149		418851	029462	80	970586 97053F	9 36 8 32
1		53	552018	552	447982			418472			970490	8 32 7 25 6 24
13		55			447651 447320			418093 417714	029558 029606		970148	5 20
101	44	56	553010	550	446990	582665	631	417335	029655	81	970345	4 10
1		57	553341 553670		446659 446330			416957 416578	029703 029751		970291	3 14
10	56	59	554000	549	446000	583800	629	416200	029800	81	970200	1
24	-	60	554329	548	445671	584177	629	415823	029848	81	970159	036 0
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				30	169	2	30	193	2	30	24	P. P. to
				1.5	253	3	45	289	3	45	36	s or "

						and	Sec	nts.		TA	BLE V.		39
_			1 He	ur,			or		21	_	grees.		
n.	8.	Ľ	Sine.	D.	Cosec.	Tang.	D.	Cotang.	Secant.	D.		_	m. 36
4	0		9.554329		10.445671		629		10.029848	81	9.970152		36
	4		554658		415312		1.00	415445	029897	81	970103		5
	12		554987		445013			415068 414691	029945 029994		970055 970006		4
	16		555315 555643		444685			414314	030043		969957		
	20		555971	546	444029		1000	413938	11 (50.0) 20.00 (10.0)	81	969909		
	24		556299		443701			413561			969860	54	3
	28	7	556626	545	443374	586815		413185			969811		
	32		556953	- 50	443047			412810			969762		
	36		557280		442720			412434	001200		969714 969665		
	44	10	557606 557932	543 543	442394 442068		625 625	412059 411684			969616		
		12	558258	543	441742		624	411309			969567	48	
	52	13	558583		441417	the second secon		410934	030482		969518		
		14	558909	542	441091	589440	V 2. 2/2.	410560	030531	88	969469	46	
5	_	-	9.559234	541	10.440766	9.589844	623	10.410186	10.030580	82	9.969420	45	
		16	559558	541	440442	590188	623	409812	030630	82	969370		
		17	559883	10000	440117			409438		-	969321		5
		18	560207	540	439793		622	409065	030728	82	969272 969223		
		19	560531	539	439469		622 621	408692 408319	030777	82	969223		1.0
		20	560855 561178	539	439145 438822			407946	030876		969124		
		21	561501	538	438499		620	407574	030925	82	969075		
	32	23	561824		438176		620	407202		82	969025		2
		24	562146	537	437854		619	406829	031024	82	968976		
		25	562468		437532	593542	619	406458	031074		968926		
	44				437210		618	406086	031123	83	968877		1
		27	563112		436888	Marie and the	618	405715	031173		968827		
		28			436567		618	405344	031223 031272	83 83	968777 968728		
_		29	563755	-	436245	and the second second	617	404973		_	9.968678		
6			9.564075	534	10.435925		617	10.404602 404232	031372	83 83	968628		
	4	31 32	564396 564716	534 533	435604 435284		617 616	403862	031422	83	968578		
	19	33	565036		434964		616	403492	031472	83	968528		4
		34	565356		434644		616	403122	031521	83	968479		
		35	565676		434324		615	402753	031571	83	968429		
		36	565995	531	434005	597616	615	402384	031621	83	968379		3
		37	566314	531	433686		615	402015		83	968329 968278		3
		38	566632		433368			401646 401278	031722 031772	83	968228		2
		39	566951	530	433049		614	400909	031822	84	968178	20	2
	40	40	567269 567587	530 529	432731 432413		613	400541	031872	84	968128		
		42	567904		432096	20,211,312	613	400173	031922	84	968078		
		43	568222		431778			399806	031973	84	968027		
		44	568539		431461	600562	612	399438	032023	84	967977		
7	0	145	9.568856	528	10.431144	9.600929	611	10,399071	10.032073	84	9.967927		
1	4	46	569172	527	430828	601296	611	398704	****	84	967876		
		47	569488		430512		611	398338		84	967826 967775		
		48			430196			397971	032225 032275	84	967775		4
		49	570120		429880			397605 397239	000000		967674		
	20	50	570135 570751		429565 429249			396873			967624		3
	29	52	571066		428934			396507	032427	84	967573	8	3
	32	53	571380		428620			396142	032478	85	967522	7	2
	36	54	571695		428305	604223	608	395777	032529		967471		
	40	55	572009	523	427991	604588	608	395412		-	967421		
	44	56	572323		427677			395047		-	967370 967319		
		57			427364			394683 394318			967268	2	
		58		100000	427050			393954	032783	85	967217		1
10		59 60			426737 426425			393590	The second secon		967166	0	32
8	_		_	021			===	_		=	Sine.	=	-
n.	. 6.	1	Cosine.		Secant.	Cotang.	_	Tang.	Cosec.	D			m.
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8	or	"	3	30 45	160 240	2 3	30 45	185	3	45	37	1	8 01
			3	40	1 240		40	210		-0	1 0.	_	_

66	101	TABLE	IX.	700	Diurn	al Log	garithn	ns.	1	-	-		1
Monn		h. m.	h. m. 0 30	h. m	h. m. 1 30	h. m.	h. m. 2 30	h. m.	h. m. 3 30	h. m.	h. m. 4 30	h. m. 5 0	h. m. 5 30
m. s.	SUN.	h. 0	h. 1	h. 2	h. 3	h. 4	h. 5	h. 6	h. 7	h. 8	h. 9	h. 10	h. 11
0 0		3.15836	1.38021									38021	33882
1 (2	2.85733	1.36597	1.0720	0 89829	77455	67836	59966	53305	47532	42436	37877	33751
2 30	4	2.55630	1.35218 1.34545	1.0649	4 89355	77097	67549	59726	53090	47352	42276	37733	33620
3 30	6	2.38021	1.33882	1.0579	9 88885	76743	67264	59488	52895	47173	42117	37589	33489
4 30	8	2.25527	1.32585 1.31951	1.0511	5 88421	76391	66981	59252	52692	46994	41958	37446	33359
5 0	10	2.15836	1.31327	1.6444	287961	76042	66700	59016	52490	46817	41800	37303	33229
6 0	12	2.07918	1.30103 1.29504	1.0377	9 87506	75696	66421	58782	52288	46640	41642	37161	33099
7 0	14		1.28913	1.0312	6 87056	75353	66143	58549	52087	46464	41485	37020	32970
8 0	16	1.95424		1.0248	2 86611	75012	65868	58318	51888	46288	41329	36878	32842
9 0	18	1.90309	1.26627	1.0184	8 86170	74674	65594	58087	51689	46113	41173	36738	32713
10 0	20	1.85733	1.25527	1.0122	4 85739	74339	65321	57858	51491	45939	41018	36597	
10 30	22	1.83614 1.81594	1.24455	1.0060	8 85301	74006	65051	57630	51294	45766	40863	36457	32458
11 30 12 0	24	1.79664 1.77815	1.23408	1.0000	0 84873	73676	64782	57403	51098	45593	40709	36318	32331
12 30 13 0	26	1.76042 1.74339	1.22387	9940	1 84450	73348	64515	57178	50903	45421	40555	36179	32204
13 30 14 0	28	1.72700	1.21388	9881	5 84239 0 84030	73023	64249	56953	50709	45250	40402	36040	32018
14 30 15 0		1.69597 1.68124			83822								
15 30 16 0	200	1.66700 1.65321			9 83408 2 83203								
16 30 17 0	46	1.63985 1.62688		9708	7 82998 4 82795	72061	53462	56287	50131	44740	39945	35627	31700
17 30 18 0	THE PERSON	1.61430 1.60206	Service Burkey Co.		3 82593 4 82391								
18 30 19 0	37	1.59016 1.57858			82190 81991								
19 30 20 0		$\frac{1.56730}{1.55630}$	STATE OF THE OWNER, TH	and the second	81792	The same of the same of	-	THE RESERVE AND ADDRESS.					31389
20 30 21 0	41	1.54558 1.53511	1.15404	9515	81397 81201	70966	62561	55522	49466	44153	39419	35151	
21 30 22 0	43	1.52490 1.51491	1.14554	9461	81006	70658	62307	55306	49278	43986	39270	35015	31141
22 30 23 0	45	1.50515 1.49561	1.13717	9408	80618	70352	62054	55091	49091	43820	39121	34880	31017
23 30 24 0		1.48627 1.47712	1.12898 1.12494	9356	80234 80043	70048	61803	54877	48905	43655	38973	34746	30894
24 30 25 0	49	1.46817	1.12094	93048	79853	69747	61554	54664	48719	43491	38825	34612	30772
25 30 26 0	51	1.45079 1.44236	1.11304	9253	79475 79288	69447	61306	54452	48534	43327	38678	34178	30649
26 30 27 0	53	1.43409	1.10529	92039	79288 79101 78915	69150	61059	54241	18350	13164	38531	34345	30527
27 30 28 0	55	1.41800	1.09767	91533	78730 78545	68854	60814	54032	18167	43001	38385	34212	10406
28 30 29 0	57	1.40249	1.09018	91039	78362 78179	68561	60570	53823	17985	12839	38239	34080 3	10284
29 30	59	1.38751			77997								

Moon		h. m.	h. m. 6 30	h. m.	h. m. 7 30	8 0	h. m. 8 30	9 0	9 30		n. m. 10 30		h. m.
	SUN.		h.	h.	h.	h.	h.	h.	h.	h.	h.	h.	h.
m. s.	m.	12	13	99100	15	17000	17	18	10146	20	21	22	23
0 0	0												01817
1 0	2												01786
1 30	3												01754
2 0	4												01723
2 30	5	29803	26349	23151	20172	17384	14764	12293	09956	07738	05627	0361	01691
3 0	6												01660
3 30	. 7												01629
4 0	8												01597 4 01566
4 30	9	75.00		_		_				-			-
5 0	10												1 01535 9 01504
5 30	11												6 01472
6 30	13												3 01441
7 0	14												01410
7 30	15	59208	25800	22640	19694	16936	14342	11895	09578	07379	05285	0328	01379
8 0	16												6 01348
8 30	17												01317
9 0	18												1 01286
9 30	19	W. W. W. Y.	100			_	-	-	-	-	1		8 01255
10 0	20												6 01224 3 01199
10 30	22												1 01162
11 30	23												901131
12 0	24												6 01100
12 30	25												4 01069
13 0	26												201038
13 30	27												0 01007
14 0 14 30	28												7 00976 5 00 94 5
	-		2 2 4 4 4 4 4 4 4		-		-			-	-	C. E. P. (3)	3 00914
15 0 15 30	30												1 00884
16 0	32												9 00853
16 30	33												7 00822
17 0	34												5 00791
17 30	35												2 00761
18 0	36												0 00730
18 30	37												8,00699 6,00669
19 0 19 30	39												4 00638
-	40	and the second of	_				_		_		_	-	2 00608
20 0	41												1 00577
21 0	42												9 00546
21 30	43												00516
22 0	44	27527	24244	21191	18339	15663	13142	10760	08501	06354	04309	0235	5 00485
22 30	45	27470	24191	21142	18293	15620	13101	10721	08465	06319	04275	0232	3 00455
23 0	46												00424
23 30 24 0	48												00394
24 30	49	27944	23981	20946	18110	15447	12939	10567	08318	06180	04142	0219	6 00333
25 0	50	27192	23090	20897	18064	15404	12898	10520	08282	06145	04109	0216	00303
25 30	51	27132	23876	20849	18018	15361	12857	10490	08245	06111	04076	02133	3 00272
26 0	52	27075	23824	20800	17973	15318	12817	10452	08209	06076	04043	0210	00242
26 30	53	27018	23772	20751	17927	15275	12776	10413	08172	06041	04010	02069	00212
27 0	54	26962	23720	20703	17882	15233	12736	10375	08136	06007	03977	02038	00181
27 30	55	26906	23668	20654	17836	15190	12696	10337	06100	05972	03914	0107	00151
28 0 28 30	56	26850	92564	90557	17745	15104	19616	10299	08003	05937	03911	01945	00091
28 30 29 0	58	26738	23519	20500	17700	15069	12574	10222	07991	05868	03845	01911	00060
29 30	59	26683	23460	20460	17655	15019	12534	10184	07954	05834	03812	01880	00030
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0 Degree, or 0 Hour.

-		400		1	-	1	A COLUMN	I I I	-	-	
1	8	Om	1m	2m	3m	4m	5m	6m	7m	8m	gm +
1	0	The same	2.25527	1.95424	The second second	Management of the Control of the Con	and the second	of Section Colleges of the	and the land to the land		Battle deduction
1	1	4.03342		95064	77575			100000000000000000000000000000000000000	40914	35128	30023
1	2	3.73239		94706	77335			THE RESERVE AND ADDRESS OF THE PERSON NAMED IN	Section 1	35038	29948
1	3 4	55630 43136	23408 22724	94352	76861	64603			40708 40606	34948 34858	29868
1	5	33445	22051	93651	76625	100000000000000000000000000000000000000	THE RESIDENCE AND ADDRESS.		40503	34858	29782 29703
1	6	25527	21388	93305	76391	64249			40401	34679	29623
1	7	18833		92962	76158	F F T T T T T T	1.00/20/20	The second second	40300	34589	29544
10	8	13033	20091	92621	75927	63897	54487		40198	34500	29464
1	9	07918	19457	92283	75696	63722	54347	46640	40097	34411	29385
1	0	3.03342	2.18833	1.91948	1.75467	1.63548	1.54206	1.46522	1.39996	1.34323	1.29306
1	1	2.99203	18217	91615	75239	63375			39895	34234	29227
	2	95424	17609	91285	75012	63202			39794	34146	29148
	3	91948	17010	90957	74787	63030		1.00 Table 100	39694	34058	29070
	4	88730	16419	90632	74562	62859		No. of Concession, Name of Street, or other Persons, Name of Street, Name of S	39593	33970	28991
	5	85733 82930	15836 15261	90309 89988	74339	62688 62518		45939 45824	39493	33882	28913
li	6	80297	14693	89670	73896	62349	53236	The state of the later	39394 39294	33794 33707	28835
li		77815	14133	89354	73676	62180	53100		39294	33707	28757 28679
i		75467	13580	89041	73457	62012	52963	10000000	39096	33532	28601
2	-	The second second	2.13033	1.88730	1.73239			THE PERSON NAMED IN	THE R. P. LEWIS CO., LANSING	The second second	1.28524
2		71120	12494	88420	73023	61678	52692	45250	38899	33359	28446
2		69100	11961	88114	72807	61512	52557	45136	38800	33272	28369
2		67170	11435	87809	72593	61347	52422	45022	38702	33186	28292
2		65321	10914	87506	72379	61182	52288	44909	38604	33099	28215
2		63548	10400	87206	72167	61018	52154	44796	38506	33013	28138
2	-	61845	09893	86907	71956	60854	52021	44684	38409	32927	28061
2		60206	09390	86611	71745	60691	51888	44571	38312	32842	27984
2		58627	08894	86316	71536	60529	51755	44459	38215	32756	27908
2		57103	08403	86024	71328	60367	51623	44347	38118	32671	27831
30		2.55630	mercace.			1.60206	1.51491	1.44236	1.38021	1.32585	THE PERSON NAMED IN
3		54206	07438	85445	70914	60045	51360	44125	37925	32500	27679
3	-	52827	06964	85158	70709	59885	51229 51098	44014	37829	32415	27603
33		51491 50194	06494	84873	70504 70301	59726 59567	50968	43903 43793	37733	32331	27527
3	-	48936	06030 05570	84590 84309	70099	59409	50838	43683	37637	32246	27451
30		47712	05115	84030	69897	59251	50708	43573	37446	32077	27500
3		46522	04665	83752	69696	59094	50579	43463	37351	31993	27225
38		45364	04220	83477	69497	58938	50451	43354	37256	31909	27150
38		44236	03779	83203	69298	58782	50322	43245	37161	31826	27075
40	7	2.43136	2.03342	.82930	1.69100	1.58627	1.50194	1.43136	1.37067	1.31742	.27000
h		42064	02910	82660	68903	58472	50067	43028	36972	31659	26925
48	2	41017	02482	82391	68707	58317	49940	42920	36878	31575	26850
43		39996	02060	82124	68512	58164	49813	42812	36784	31492	26776
44		38997	01639	81858	68318	58011	49687	42704	36691	31409	26701
4.5		38021	01223	81594	68124	57858	49560	42597	36597	31326	26627
46		37067	00812	81332	67932	57706	49435	42490	36504	31244	26553
47		36133	00404	81071	67740	57554	49309	42383	36411	31161	26479
48		35218	00000	80811	67549 67359	57403	49184	42276	36318	31079	26405
Section 1	4,5	THE RESERVE OF THE PERSON NAMED IN	.99600	80554		STATE OF THE PARTY				Market Street, St.	The Real Property lies
50	6 B		Olividadiudiudud la	.80297 1	CONTRACTOR OF THE PARTY OF THE	56953	1.48936 1 48812	41958		309151	
51		32585	98810 98421	80043 79790	66981	56804	48688	41958	36040	30833	26110
53		30915	98035	79790	66607	56656	48565	41747	35856	30670	26037
54		30103	97652	79287	66421	56508	48442	41642	35765	30588	25964
55		29306	97273	79039	66236	56360	48320	41538	35673	30507	25891
56		28524	96897	78791	66051	56213	48197	41433	35582	30426	25818
57		27755	96524	78545	65868	56067	48076	41329	35491	30345	25145
58	п	27000	96154	78300	65685	55921	47954	41225	35400	30264	25672
59		26257	95788	78057	65503	55775	47833	41121	35309	30183	25600
	-		_								

				Propor	tional I	ogarith	ms.	TABL	EX.	69
				0 D	egree, or	0 Hour.				
8	10m	11 ^m	12m	13 ^m	14m	15 ^m	16m	17m	18m	19m
0	1.25527	1.21388	1.17609	1.14133		1.07918	1.05115	1.02482	1.00000	0.97652
1	25455	21322	17549	14077	10863	07870	05070	02440	0.99960	97614
2	25383	21257	17489	14022	10811	07892	05025	02397	99920	97576
3	25311	21191	17429	13966	10760	07774	04980	02355	99880	97538
4	25239	21126		13911		07726	04935	02312	99839	97500
5	25167	21060	17309	13855	10657	07678	04890	02270	99799	97462
6	25095	20995	17249	13800	10605	07630	04845	02228	99759	97424
7	25024	20930	17189	13745	10554	07582	04800	02185	99719	97386
8	24952	20865	17129	13690	10503	07534	04755	02143	99679	97348
9	24881	20800	17070	13635	10452	07486	04710	02101	99640	97310
10	1.24809	1.20735	1.17010	1.13580	1.10400	1.07438	1.04665	1.02059	0.99600	0.97273
11	24738			13525			04620			
12	24667	20605		13470						
13	24596	20541	16832	13415		07295		01932		
14	24526	20476		13360		07248	04486	01890	99441	
15	24455	20412		13306		07200	04442	01848	99401	
16	24384	20348		13251	10095		04397	01806		
17	24314	20284		13197	10044	07105	04353	01764	99322	
18	24244	20219		13142		07058	04308	01723		
19	24173	20155	16478	13088	09943	07011	04264	01681	99243	96934
20	1.24103	1,20091	1.16419	1.13033	1.09893	1.06964	1.04220	1.01639	0.99203	0.96897
21	24033			12979						
22	23963							01556		
23	23894						1 2 2 2 2 2			
24	23824					06775				
25	23754			12763		06728	03999			
26	23685	19710		12709		06681	03955			
27	23616	19647						01348		
28	23546			12601	09490	06588	03867	01306		
29	23477	19520			09440	06541	03823	01265		
	45011		-500	-50-20		- 55011			20010	2000

1.23408 1.19457 1.15836 1.12494 1.09390 1.06494 1.03779 1.01223 0.98810 0.96524

.4

.3

1.05570 1.02910

.5

.6

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.7

1.00404 0.98035 0.95788

0.98421 0.96154

.9

1.08894

.2

.22724

1.22051

Proportional Part to

tenths of " or s.

1.18217 1.14693

1.18833 1.15261

.11961

.1

5 14

1.11435 1.08403

76	2	TABLE	X.	Propor	tional 1	ogarith	ms.			
				0 D	egree, o	0 Hour.				
8	20m	21m	22m	23m	24m	25m	26m	27m	28m	29m
0	95424	93305	91285	89354	87506 87476		84030 84002	82391 82364	80811 80786	79287 79263
5	95388 95352	93271	91252	89323	87446		83974	82337	80760	79238
3	95316	93202	91186	89260	87416	THE RESERVE TO SERVE THE PERSON NAMED IN	83946	82311	80734	79213
5	95280 95244	93168 93133	91154	89229	87386 87356		83919 83891	82284 82257	80708 80682	79188
6	95208	93099	91088	89166	87326	STATE OF THE OWNER, TH	83863	82230	80657	79138
8	95172 95136	93065	91055 91023	89135 89103	87296 87266		83835 83808	82204 82177	80631 80605	79113 79088
9	95100	92996	90990	89072	87236	III III III III III III III III III II	83780	82150	80579	79063
10	95064	92962	90957	89041	87206	The second second	83752	82124	80554	79039
11	95028 94992	92928 92894	90925	89010 88978	87176 87146		83725 83697	82097 82070	80528 80502	79014 78989
13	94956	92860	90859	88947	87116	85358	83670	82044	80477	78964
14	94921 94885	92825 92791	90827	88916 88885	87086 87056	85330 85301	83642 83614	82017 81991	80451 80425	78939 78915
16	94849	92757	90762	88854	87026	85272	83587	81964	80400	78890
17	94813	92723	90729	88823	86996	THE RESERVE OF THE PERSON NAMED IN	83559	81938	80374	78865
18 19	94778	92689 92655	90697	88792	86967 86937	85215 85187	83532 83504	\$1911 \$1884	80349	78840 78816
20	94706	92621	90632	88730	86907	85158	83477	81858	80297	78791
21	94671	92587	90599	88699	86877	85129	83449	81832	80272	78766
22	94635 94600	92554	90567	88668 88637	86848 86818	85101	83422 83394	81805 81779	80246	78742
24	94564	92486	90502	88606	86788	85044	83367	81752	80195	78693
25	94529 94493	92452 92418	90470	88575 88544	86759 86729	85015	83339 83312	81726 81699	80170	78668
27	94458	92385	90438	88513	86699	84958	83285	81673	80119	78643 78619
28	94423	92351	90373	88482	86670	84930	83257	81647	80094	78594
30	94387	92317	90341	88451	86640	84902	83230	81620	80068	78570
31	94317	92250	90277	88390	86581	84845	83175	81568	80017	78545 78521
32	94281	92216	90245	88359	86552	84816	83148	81541	79992	78496
33	94246	92183 92149	90213	88328 88297	86522 86493	84788	83121 83094	81515 81489	79967	78472 78447
35	94176	92115	90148	88267	86463	84732	83066	81463	79916	78423
36 37	94141	92082 92048	90116	88236 88205	86434 86404	84703 84675	83039 83012	81436 81410	79891 79865	78398 78374
38	94070	92015	90052	88175	86375	84647	82985	81384	79840	78349
39	94035	91981	90020	88144	86346	84619	82958	81358	79815	78325
40	94000 93965	91948 91915	89988 89957	88114 88083	86316	84590 84562	82930 82903	81332 81305	79790 79764	78300 78276
42	93930	91881	89925	88052	86258	84534	82876	81279	79739	78252
43	93895 93860	91848 91815	89893 89861	88022 87991	86228 86199	84506 84478	82849	81253	79714	78227
45	93825	91781	89829	87961	86170	84450	82822 82795	81227	79689 79663	78203 78179
46	93791	91748	89797	87930	86141	84421	82768	81175	79638	78154
47	93756 93721	91715 91682	89766 89734	87900 87870	86111	84393 84365	82741 82714	81149 81123	79613 79588	78130 78106
49	93686	91648	89702	87839	86053		82687		79563	78081
50	93651	91615	89670	87809	86024	84309	82660	81071	79538	78057
51 52	93617 93582	91582 91549	89639 89607	87778 87748	85995 85965	84281 84253	82633 82606	81045 81019	79513 79488	78033 78009
53	93547	91516	89575	87718	85936	84225	82579	80993	79463	77984
54	93513 93478	91483 91450	89544 89512	87687 87657	85907 85878	84197 84169	82552 82525	80967 80941	79437	77960
56	93443	91417	89481	87627	85849	84141	82498	80915	79412	77936
57 58	93409	91384	89449	87597	85820	84114	82471	80889	79362	77888
59	93374 93340	91351 91318	89417 89386	87566 87536	85791 85762	84086 84058	82445 82418	80863 80837	79337 79312	77863
12,000	Proport	ional Pa	rt to	.1		3 .4	.5	.6	-	8 .9
	tenths	of "or	8.	3	6	9 12	15	18	21 2	

				Propor	tional I	Logarith	ms.	TABL	EX.	7
				0 D	egree, or	0 Hour.				
" 5	30m	31 ^m	32m	33 ^m	34m	35m	36m	37m	38m	39
0	77815	76391	75012	73676	72379	71120	69897	68707	67549	6649
1	77791	76368	74990	73654	72358	71100	69877	68698	67530	6640
3	77767	76344	74967	73632 73610	72337 72316	71079	69857 69837	68668 68648	67511	6636
4	77719	76298	74922	73588	72294	71038	69817	68629	67473	663
5	77695	76275	74899	73566	72273	71017	69797	68609	67454	663
6	77671	76251	74877	73544	72252	70997	69777	68590	67435	663
7	77647	76228	74854	73523	72231	70976	69756	68570	67416	662
8	77623	76205	74832	73501	72209	70955	69736	68551	67397	662
9	71599	76181	74809	73479	72188	70935	69716	68531	67378	662
0	77575	76158	74787	73457	72167	70914	69696	68512	67359	662
1 2	77551	76135 76112	74764	73435 73413	72146	70894	69676 69656	68492 68473	67340	662
3	77503	76089	74719	73392	72103	70852	69636	68454	67302	661
4	77479	76065	74697	73370	72082	70832	69616	68434	67283	661
5	77455	76042	74674	73348	72061	70811	69596	68415	67264	661
6	77431	76019	74652	73326	72040	70791	69576	68395	67245	661
7	77407	75996	74629	73305	72019	70770	69557	68376	67226	661
8	77385	75973 75950	74607	73283 73261	71998	70750	69537 69517	68356 68337	67207 67188	660
u	77335	75927	74562	73239	71956	70709	69497	_	67170	660
ĭ	77311	75903	74540	73218	71935	70688	69477	68298	67151	660
2	77288	75880	74517	73196	71914	70668	69457	68279	67132	660
3	77264	75857	74495	73174	71892	70647	69437	68259	67113	659
4	77240	75834	74473	73153	71871	70627	69417	68240	67094	659
5	77216	75811	74450	73131	71850	70606	69397	68221	67075	659
6	77192 77169	75788 75765	74428	73109 73088	71829	70586	69377	68201 68182	67036	659
έl	77145	75742	74383	73066	71787	70545	69338	68163	67019	659
9	77121	75719	74361	73044	71766	70525	69318	68143	67000	658
0	77097	75696	74339	73023	71745	70504	69298	68124	66981	658
1	77074	75673	74317	73001	71724	70484	69278	68105	66962	658
5	77050	75650	74294	72980	71703	70464	69258	68086	66944	658
3	77026	75627	74272	72958	71682	70443	69239	68066	66925	658
5	77002	75604 75581	74250 74228	72936 72915	71662	70423	69219	68047 68028	66906 66887	657
6	76955	75559	74205	72893	71620	70382	69179	68008	66869	657
7	76931	75536	74183	72872	71599	70362	69159	67989	66850	657
8	76908	75513	74161	72850	71578	70342	69140	67970	66831	657
9	76884	75490	74139	72829	71557	70381	69120	67951	66812	657
0	76861	75467	74117	72807	71536	70301	69100	67932	66794	656
1	76837	75144	74095	72786	71515	70281	69080	67912	66775	656
3	76813	75421 75398	74072	72764	71494	70260	69061	67893	66737	656
4	76790	75376	74028	72721	71453	70220	69021	67855	66719	656
5	76743	75353	74006	72700	71432	70200	69002	67836	66700	655
6	76719	75330	73984	72678	71411	70179	68982	67816	66681	655
7	76696	75307	73962	72657	71390	70159	68962	67797	66663	655
8	76672	75285	73940	72636	71369	70139	68942	67778	66644	655
9	76649	75262	73918	72614	71349	70119	68923	67759	66625	655
0	76625	75239 75216	73896 73874	72593 72571	71328	70099	68903 68884	67740	66607	655
5	76578	75194	73852	72550	71286	70058	68864	67702	66570	654
3	76555	75171	73830	72529	71265	70038	68844	67682	66551	654
4	76531	75148	73808	72507	71245	70018	68825	67663	66532	654
5	76508	75125	73786	72486	71224	69998	68805	67644	66514	654
6	76485	75103	73764	72465	71203	69977	68785	67625	66495	653
8	76461 76438	75080 75058	73742	72443 72422	71183 71162	69957 69937	68766 68746	67606 67587	66477 66458	653
9		75035	73698	72401	71141		68727		66439	
- !		ional Pa		.1		.3 .4	.5	.6		8
		s of " or		2	4	6 8	10	13	15 1	

1	2	TABLE	X.	Propor	rtional 1	Logarith	ms.			
	-		-	01	egree, o	r 0 Hour				-
's	and the second	41m	42m	4.3m	41m	4.5m	46m	47m	48m	49m
	65321	64249	63202	62164	61182		59251 59236	58317 58302	57403 57388	56508
100	65985	64214	63168	62147	WALL DO NOT		59220	58287	57373	56478
	65267	64196	63151	62130	61133		59204	58271	57358	56163
	65249	64178	63133	62113	61116	the last of the last of	59189 59173	58256	57343	56449
100	65213	64143	63099	62080	61083	60110	59157	58225	57313	56419
1	STATE OF THE PARTY.	64125	63082	62063 62046	61067		59141	58210 58194	E MANGEMENT OF	56404
1		64090	63048	62029	61034		59110	58179	57268	56375
10	65141	64073	63030	62012	61018	60045	59094	58164	57253	56360
11	The second second	64055	63013	61996	61001		59079	58148	57238	56345
15		64038 64020	62996	61979	60985		59063 59047	58133 58118	57223	56331
14	65069	64002	62962	61945	60952	59981	59032	58102	57193	56301
18		63985	62945	61929	60936	59965	59016	58087	57178	56287
17		63950	62910	61895	60903		58985	58056	57148	56257
18	64997	63932	62893	61878	60887	59917	58969	58041	57133	56243
19	and the second	63915	62876	61862	60871	59901	58954	58026	57118	56228
20		63897 63880	62859 62842	61845	60854	59885	58938 58922	58011 57995	57103 57088	56213
22	64925	63862	62825	61812	60822	59854	58907	57980	57073	56184
23	S. Billion Schools St.	63845	62808	61795	60805	59838	58891	57965	57058	56169
24		63827	62791	61778	60789	59822	58875 58860	57949	57013	56155
26	64853	63792	62757	61745	60756	59790	58844	57919	57013	56125
27		63775	62739	61728	60740	59774	58829 58813	57904	56998	56111
29		63757	62722 62705	61712	60708	59758	58798	57888. 57873	56983 56968	56098 56081
30	and the second	63722	62688	61678	60691	59726	58782	57858	56953	56067
31		63705	62671	61662	60675	59710	58766	57843	56938	56052
33		63688	62654 62637	61645	60659	59694 59678	58751 58735	57827	56923	56037 56023
34	64710	63653	62650	61612	60626	59663	58720	57797	56893	56008
35	The second second	63635	62603	61595	60610	59647	58704	57782	56879	55991
36		63618	62586 62569	61579	60594	59631 59615	58689 58673	57767	56864 56849	55979
38	64639	63583	62552	61515	60561	59599	58658	57736	56834	55950
39	64621	63566	62535	61529	60545	59583	58642	57721	56819	55935
40	64603	63548	62518	61512	60529	59567 59551	58627 58611	57706 57691	56789	55921 55906
42	64568	63514	62484	61479	60496	59536	58596	57675	56774	55892
43	64550	63496	62468	61463	60480	59520	58580	57660	56759	55877
44	64539	63479	62451	61446	60464	59504	58565 58549	57645 57630	56745	55862 55848
46	64497	63444	62417	61413	60432	59472	58534	57615	56715	55833
47	64479 64461	63427	62400	61396	60416	59457	58518	57600	56700	55819
49	64443	63410 63392	62383	61363	60383	59441	58503 58487	57581 57569	56685	55804 55790
50	64426	63375	62349	61347	60367	59409	58472	57554	56656	55775
51	64408	63358	62332	61330	60351	59393	58456	57539	56641	55761
52 53	64390	63340	62315	61314	60335	59378 59362	58441	57524	56626	55746 55732
54	64355	63306	62282	61281	60303	59346	58410	57494	56596	55717
55		63289	62265	61264	60286	59330	58395	57479	56582	55703
56	64300	63271	62248	61248	60270	59314	58379	57463	56567	55688 55674
58	64284	63237	62214	61215	60238	59283	58348	57433	56537	55659
59		63220	62197	61198	60555	59267	58333	57418	56522	55645
15-		ional Par		2		3 .4 6	.5	10	.7 .8 11 13	

				Propor	tional I	ogarith	ıns.	TABL	x.	73
				0 D	egree, or	0 Hour.				
" s	50m	51m	52m	53m	54m	55m	56m	57m	58m	59m
0	55630	54770	53927	53100	52288	51491	50708	49940	49184	48412
1	55616	54756	53913	53086	52274	51478	50696	49927	49172	48430
2	55601	54742	53899	53072	52261	51465	50683	49914	49159	48418
3	55587	54728	53885	53059	52248	51452	50670	49902	49147	48405
4	55572	54714	53871	53045	52234	51438	50657	49889	49135	48393
5	55558	54699	53857	53031	52221	51425	50644	49876 49864	49122	48381
6	55543	54685	53843	53018	52208	51412 51399	50631 50618	49851	49097	48356
7	55529	54671	53830	53004	52194	51399	50605	49838	49085	48344
8	55515	54657	53816	52991	52181	51373	50592	49826	49072	48339
9	55500	54643	53802	52977	52167			49813	49060	48320
10	55486	54629	53788	52963	52154	51360	50579 50566	49800	49047	48307
1	55171	54614	53774	52950	52141	51346 51333	50554	49788	49035	4829
12	55457	54600	53760	52936	52127 52114	51320	50541	49775	49023	48283
13	55442	54586	53746	52922 52909	52101	51307	50528	49762	49010	48271
15	55428 55414	54572 54558	53732 53719	52895	52087	51294	50515	49750	48998	48258
16	55399	54544	53705	52882	52074	51281	50502	49737	48985	48246
17	55385	54530	53691	32868	52061	51268	50489	49724	48973	48234
8	55370	54516	53677	52855	52047	51255	50476	49712	48960	4822
9	55356	54501	53663	52841	52034	51242	50464	49699	48948	48210
20	55342	54487	53649	52827	52021	51229	50451	49687	48936	48197
21	55327	54473	53636	52814	52007	51215	50438	49674	48923	4818.
25	55313	54459	53622	52800	51994	51202	50425	49661	48911	48173
23	55299	54445	53608	52787	51981	51189	50412	49649	48898	
24	55284	54431	53594	52773	51967	51176	50399	49636	48886	48149
25	55270	54417	53580	52760	51954	51163	50387	49623	48874	48136
26	55255	54403	53567	52746	51941	51150	50374	49611	48861	48124
27	55241	54389	53553	52732	51927	51137	50361	49598	48849	48113
8	55227	54375	53539	52719	51914	51124	50348	49586	48836	48100
9	55212	54361	53525	52705	51901	51111	50335	49573	48824	48088
30	55198	54347	53511	52692	51888	51098	50322	49560	48812	48070
31	53184	54332	53498	52678	51874	51085	50310	49548	48799	48063
35	55169	54318	53484	52665	51861	51072	50297	49535	48787	4803
33	55155	54304	53470	52651	51848	51059	50284	49523	48775	4802
34	55141	54290	53456	52638	51835	51046	50271 50258	49510 49498	48750	4801
35	55127	54276	53442	52624	51821	51033	50246	49485	48737	4800
36	55112	54262 54248	53429 53415	52611 52597	51795	51007	50233	49472	48725	4799
37 38	55098 55084	54231	53401	52584	51781	50994	50220	49460	48713	4797
19	55069	54220	53387	52570	51768	50981	50207	49447	48700	4796
			_	-	-	50968	50194	49435	48688	4795
10	55055 55041	54206 54192	53374 53360	52557 52543	51755 51742	50955	50194	49422	48676	4794
5	55026	54178	53346	52530	51729	50942	50169	49410	48663	47930
3	55012	54164	53332	52516	51715	50929	50156	49397	48651	4791
4	54998	54150	53319	52503	51702	50916	50143	49385	48639	4790
5	54984	54136	53305	52489	51689	50903	50131	49372	48626	4789
6	54969	54122	53291	52476	51676	50890	50118	49360	48614	4788
7	54955	54108	53278	52462	51662	50877	50105	49347	48602	4786
8	54941	54094	53264	52449	51649	50864	50092	49334	48590	4785
9	54927	54080	53250	52436	51636	50851	50080	49322	48577	4784
0	54912	54066	53236	52422	51623	50838	50067	49309	48365	4783
1	51898	51052	53223	52409	51610	50825	50054	49297	48553	4782
2	54884	54038	53209	52395	51596		50041	49284	48510	4780
3	54870	54024	53195	52382	51583		50029	49272	48528	4779
14	54855	54011	53182	52368	51570		50016	49259	48516	4778
55	54841	53997	53168	52355	51557	50773	50003	49247	48503	47775
6	51827	53983	53154	52342	51544	50760	49991	49234	48491	47760
57	54813	53969	53141	52328	51530	50747	49978	49222	48479 48467	47748
8	54799	53955	53127	52315	51517	50734	49965	49197	18451	47724
9	54784	53941	53113	52301	51504	50721	49952			_
-	Proport	ional Pa	rt to	.1	.2	.3 .4	.5	.6	.7 .	8 .

74		TABLE	X.	P	roporti	onal L	ogarith	ms.				-1
					1 De	gree, or	1 Hour					
"s	0m	1m	2m	3m	4m	5m	6m	7m	gm	gú	10m	11 ^m
0	47712	46994 46982	46288 46276	45593	44909 44898	44236	43573 43562	42920 42909	42276 42266	41642 41632	41017	40401
2	47688	46971	46265	45570	44887	44214	43551	42898	42255	41621	40997	40381
3 4	47676 47664		46253 46241	45559		44203 44191	43540 43529		42244 42234	41611 41600	40986	
5	47652 47640	September 1	46230 46218	45536 45524	44853 44841	44180 44169		42866 42855		41590 41579	40966	40350
7	47628	THE RESERVE OF	46206	45513			43496	42844	42202	41569	40945	40330
8 9	47616 47604	46899 46888	46195 46183	45501 45490	44819 44808		43485			41559	40935	40320
10	47592	46876	46171	45478	44796	44125	43463		42170	41538	40914	40300
11	47580 47568	A 100 Miles (1997)	46160 46148	45467 45456	44785	44114			42159 42149		40904 40894	40289
13	47556	46840	46137	45444	44762	44091	43431	42780	42138	41506	40883	40269
14	47544 47532	CONTRACTOR OF	46125 46113	45433	44751	44080 44069	A COLUMN TO STATE OF THE PARTY		42128 42117		I Bellindar Males	The Contract of the Contract o
16	47520	46805	46102	45410	44729	44058	43398	42747	42106	41475	40852	40239
17 18	47508 47496	DESCRIPTION AND ADDRESS.	46090 46078	45398 45387	44717	44047			42096 42085	Called Section 1	40842	40228
19	47484	46769	46067	45375	44695	44025	43365	42715	42075	41443	40821	40208
20 21	47472 47460	46758 46746	46055 46044	45364 45353		44014	The same of the same			The Public Section	40811	40198 40188
22	47448		46032	45341	44661	43992	43332	42683	42043	41412	40791	40178
23	47436 47424	The second second	46020	700000	44650				Access Charles Add	41402	40780	
25	47412	46699	45997	45307	44627	43958	43300	42651	42011	41381	40760	40147
26 27	47400 47388	The second lives	PROPERTY.		44616 44605		43289	Marine Control of the		No. of Contract of		
28	47376	46663	45962	45273	44594	43925	43267	42618	41979	41350	40729	40117
30	47364	A CONTRACTOR OF THE PARTY OF TH	THE REAL PROPERTY.	45261	44583	43914		A Revision Control	41969	The second second		40107
31	47840	46628	45928	45238	44560	43892	43234	42586	41948	41318	40698	
32	47328 47316	P. Charles St. W.	45916 45905	THE RESIDENCE OF	44549 44538	AV1.237.4303	The second second		41937		Military and the state of the s	
34	47304	46593	45893	45204	44526	43859	43202	42554	41916	41287	40667	40056
35 36	47292	46581	The second second		44515					The second second	Market Service	40046
37	47268	46557	45858	45170	44493	43826	43169	42522	41884	41256	40637	40026
38	47256	The State of the Local Division in the	45847 45835	45159 45147	44482			42511 42500			Manager Contraction of the Contr	
40	47232		45824	45136	44459	The Control of the Co	43136	42490	41853	41225	40606	39996
41	47220	The second second	The second second		44448			42479			Branch and California	
43	47196		45789	45102	44426	43760	43104	42458	41821	41194	40575	39965
44	47185		45777	The second second	44414			COLUMN	A CONTRACTOR OF		TO STORY SHOW	00000
46	47161				44392		43071	42426	41789	41162	40544	39935
48	47149	46428	45743 45731	45045	44370	43705	43050	42415 42404	41768	41142	40524	39915
49		46417	45720	45034	44359	43694	43039	42394	41758	41131	40514	39905
50	47113	46393	45708	45022	44347	43683	43028	42383	41747	41121	40508	39895 39885
52	47089	46382	45685	45000	44325	43661	43006	42362	41726	41100	40483	39874
53 54	47066	46358	45662	44977	44309	43639	42985	42340	41705	41080	40463	39864 39854
55	47054	46346	45651	44966	44292	43628	42974	42330	41695	41069	40452	39844
56	47030	46323	45628	44943	44269	43606	42952	42308	41674	41059	40442	39834 39824
58	47018	46311	45616	44932	44258	43595	42941	42298	41663	41038	40422	39814
	- Marie Company	ional Pa	A DESCRIPTION OF THE PERSON NAMED IN	-	44247	.2	42931	4	-5			39804
12	LIE	of " or		- 9	1	2	3	. 4	5	7	-	9 10

1 Degree, or 1 Hour.													
" 8	12m	13 ^m	14m	15 ^m	16 ^m	17 ^m	18m	19m	20m	21 ^m	22m	23m	
0	39794	39195	38604	38021	37446	36878	36318	35765	35218	34679	34146	3361	
1	39784	39185	38594	38011	37436	36869	36309	35755	35209	34670	34137	3361	
2	39774	39175	38585			36859			35200	34661	34128	3360	
3	39764					36850				34652	34119	3359	
4	39754	39155	38565			36841				34643	34111	3358	
5	39744					36831							
6	39734	39136			37389	36822	36262	35710	35164	34625	34093	3356	
7	39724	39126		37954					35155	34616	34084	3355	
R	39714					36803				34607	34075	3355	
9	39704	39106	38516	37934	37360	36794	36234	35682	35137	34598	34066	3354	
10	39094	39096	38506	37925	37351	36784	36225	35673	35128	34589	34058	3353	
11	39684	39086	38497	37915	37341	36775	36216	35664		34581			
12	39674	39076	38487	37905	37332	36766	36207	35655	35110	34572	34040		
13	39664	39066	38477	37896	37322	36756	36197	35646	35101	34563	34031	3350	
14	39653	39056	38467	37886	37313	36747	36188	35636	35092	34554	34022	3349	
15	39643	39046	38458	37877	37303	36737	36179	35627	35083	34545	34014	3348	
16	39633	39037	38448	37867	37294	36728	36170	35618	35074	34536	34005	3348	
17	39623	39027	38438	37857	37284	36719	36160	35609	35065	31527	33996	3347	
18	39613	39017	38428	37848	37275	36709	36151	35600	35056	34518	33987	3346	
19	39603	39007	38419	37838	37265	36700	36142	35591	35047	34509	33978	3345	
20	39593	38997	38409	37829	37256	36691	36133	35589	35038	34500	33970	3344	
21		38987				36681							
22	39573	38977	38389		37237			35563		34483			
23	39563		38380		37227			35551			33943		
24	39553					36653							
25	39543		38360					35536		34456			
26	3953 3	38938	38351			36634				34447		3339	
27	39523	38928	38341	37761						34438			

28 39513 38918 38331 37752 37180 36616 36059 35509 34966 34429 33899 33376

3947: 38879 38292 37713 37142 36569 36022 35472 34930 34394 38864 39341 39461 38869 38282 37704 37123 36569 36032 35463 34921 34385 33856 33833 39451 38859 38253 37694 37123 36569 36003 35454 34912 34376 33847 33324 39444 38849 38263 37685 37114 36550 35994 35445 34903 34367 33838 33815 39434 38839 38253 37675 37104 36541 35985 35456 34894 34358 33829 33307 39424 38830 38244 37665 37095 36532 35976 35427 34885 34349 33820 33298 39414 38820 38234 37656 37085 36522 35967 35418 34876 34340 33812 33289

39404 38810 38224 37646 37076 36513 35957 35409 34867 34332 33803 33281 39394 38300 38215 37637 37067 36504 35948 35400 34858 34323 33794 33272 39384 38790 38205 37627 37057 36494 35939 35391 34849 34314 33785 38263

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39291 38702 38118 37541 36972 36411 35856 35309 34768 34234 33707 33186 39284 38692 38108 37532 36963 36401 35847 35300 34759 34225 33698 33177 38682 38098 37522 36953 36392 35838 35291 34750 34217 33689 33168

52 39264 38673 38089 37513 36934 36383 35829 35828 34732 34790 33672 33165 54 39254 38663 38069 37513 36934 36384 35820 35273 34732 34199 33672 33151 55 39245 38663 38069 37494 36926 36364 35810 35264 34723 34199 33672 33151 56 39235 38643 38060 37484 36916 36926 35801 35254 34715 34181 33654 33134 57 39225 38633 38050 37474 36916 36936 35801 35254 34715 34181 33654 33134 57 39225 38633 38050 37474 36906 36346 35792 35245 34706 34172 33646 33125 58 39215 38624 38040 37465 36887 36387 35784 35287 34688 34155 33628 33108

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38321 37742 37171 36606 36050 35500 34957 34420 33891 33367 38899 38312 37733 37161 36597 36040 35491 34948 34411 33882 33359

38302 37723 37152 36588 36031 35481 34939 34403 33873 33350

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Proportional Part to tenths

of " or s.

76	0	TABLE	X.	1	roport	ional I	ogarith	nms.				
					1 De	gree, or	1 Hou					
8	24m	25m	26m	27m	28m	29m	30m	31 ^m	32m	33m	34m	35m
0	33099 33091	32585 32577	32077 32069	31575 31567	31079 31071	30588 30580	30103 30095	29623 29615	29148 29141	28679 28671	28214 28207	27755 27747
23	33082 33073	32568 32560	32061 32052	31559 31550	31063 31054	30572 30564	30087 30079	29607 29599	29133 29125		28199 28191	27740 27732
4	33065	32551	32044	31542	31046	30556	30071	29591	29117	28648 28640	28184 28176	27724
5	33056 33048	III CONTRACTOR IN CONTRACTOR I	CONTRACTOR OF THE PARTY OF THE	31525	31030	30548 30539	30063 30055	29575	29101	28632	28168	27717 27709
7 8	33039 33030	32526 32517	32019	1000	31021	30531 30523	30047	29567 29560	29093 29086	28625 28617	28161 28153	27702 27694
9	33022	32509	32002		31005	30515	STATE OF THE PERSON.	29552	29078	28609	28145	27686
10 11	33013 3300 <i>5</i>	32500 32492	31993 31985		30997 30989	30507 30499	30023 30015	29536	29062	28593	28130	27679 27671
12 13	32996 32987	32483 32475	31977 31968	31476 31467	30980	30491 30483	30007 29999	29528 29520			28122 28114	27664 27656
14	32979	32466	31960	31459	120200	30475	29991 29983	29512	29038 29031	28570 28562	28107 28099	27648
16	32970 32962	32458 32449	31951 31943		30918	30458	29975	29496	29023	28555	28091	27641 27633
17 18	32953 32944	32441	31935 31926	COLUMN TO SERVICE	30939 30931	30450	29967 29958	29488 29480		28547 28539	28084 28076	27626 27618
19	32936	32424	31918	31418	30923	30434	29950	29472	28999	28531	28068	27610
20 21	32927	32415	31909 31901	31409	30915	30426	29942 29934	29464 29456	28991 28984	28524 28516	28061 28053	27603. 27595
22	32910 32902	32398	31893	31393	30898	30410	29926	29448		28508	BACK STORY	27588 27580
23 24	32893	32390 32381	31884 31876	31376	30882	30393		29433	28960	28493	28030	27572
25 26	32884 32876	32373 32365	31867		DOMESTIC OF THE PARTY OF THE PA	30385	29902 29894		28952 28944	28485 28477	28022	27565 27557
27	32867	32356	31851	31351	30857	30369	29886	29409	28937	28469 28462	28007 27999	27550
28	32859 32850	32348 32339	31842 31834	31343 31335	30849 30841	30361 30353	29878 29870		28929 28921	28454	27992	27542 27534
30	32842 32833	32331	31826	31326 31318	not but	30345	29862 29854		28913 28905	28446 28438	STATE OF THE PARTY OF	27527 27519
32	32824	32314	31809	31310	30817	30329	29846	29369	28897	28431	27969	27512
33	32816 32807	32305	31801	31302	THE RESERVE ASSETS	30321	29838 29830	BASES 1207	28890 28882	28423 28415	27961 27953	27504
35	32799 32790	32288	31784		30792 30784	30305	Management of the Control of the Con					27489 27481
37	32782	32271	31767	31269	30776	30288	29806	29330	28858	28392	27930	27474
38	32773 32765	32263 32255	31759 31750	DESCRIPTION OF THE PERSON OF T	30768	30280	29798 29790	10000	288 <i>5</i> 1 288 <i>4</i> 3	28384 28376	27923 27915	27466 27459
40	32756	32246	31742	31244	30751	30264	29782	29306	28835	28369	27908	27451
41	32747 32739	32238	31734	PORT 2 370	30743	30256 30248	29775 29767	29298 29290	28827 28819	28361 28353	27900 27892	27444
43	32730 32722	32221 32212	31717		30727	30240	29759 29751	29282 29275	28811	28346 28338		27429 27421
45	32713	32204	31700	31203	30710	30224	29743	29267	28796	28330	27869	27413
46	32705 32696	32195	31692 31684		30702	30216	29735 29727	29259 29251	28788 28780	100000000000000000000000000000000000000	27862 27854	27406 27398
48	32688 32679	32179	31675						28772	28307	27846 27839	
50	32671	32162	31659	31161	30670	30184	29703	29227	28757	28292	27831	27376
51 52	32662	32153	31650	31153	30662	30175	29695	29219	28749	28284	27824 27816	27368
53	32645	32136	31634	31137	30645	30159	29679	29204	28733	28268	27808	27353
55	32628	32120	31617	31120	30637 30629	30143		29188	28718	28253	27801 27793	27338
56 57					30621		29655 29647				27785 27778	
58 59	32602	32094	31592	31095	30605	30119	29639	29164	28695	28230	27770	27315
	roportio	onal Pa	31584		30.596	.2	.3	29156	_		27763	COLUMN TO SERVICE SERV
_	300	of " or	8,	2	1	2	2	. 3	4	200	6 (

					Proport	ional I	ogarit	hms.	7	Cabi.e	X.	77
					1 De	gree, or	1 How					
# 8	36m	37 <u>m</u>	38m	39m	40 ^m	41m	42m	43m	44m	45m	46m	47m
0	27300		26405			25095			23824		22997	22589
5	27293 27285		26397 26390	25956 25949				24237 24229			22990 22983	
3		26828		25942	25506		24646	21222	23803			2256
4	27270	26820						24215	23796	23381		2256
5 6	27262 27255	26813 26805	26360		25491 25484		24632 24625	24201			22963 22956	22554 2254
7	27217	26798	26353	25913	25477	25045	24618	24194	23775	23360		
8	27240			25905				24187			25915	
9	27232	26783	26331	25898			24603			23346		2252
10 11	27225 27217	26776 26768		25891 25883	25455 24148	25024 25016		24173 24166	23754 23747			2252 2251
12		26761				25009		24159			22915	
13		26753					24575				22908	
14 15	27195	26746 26738	26294	25861 25854		21995 21988	24568 24561		23727 237 2 0		22901 22894	
16	27180	26731	26287			21981		24131			22888	
17	27172					24973	24547	24124	23706			
18 19	27165 27157	26716 26709	26271	25832 25825	25397	24 966 24 959		24117 24110				
20	27150					24952		24103				2245
21		26694				24945		24096				
22			26242	25803	25368	21938	24511	24089	23671	23257	22847	2244
23 24		26679 26671			25361 25354			24082 24075				
25		26664						24068			22833 22826	
26		26656	26213	25774				24061	23643	23229	22819	2241
27	27097			25767	25332			24054				
28 29	27090 27082		26198 26191			24895 24888		24047 24040			22806 22799	2240
30	27075		26184			24881	24455	84033	23616		22792	2238
31 32	27067		26176 26169			24874 24866		24026 24019	23609 23602			2238 2237
33						24859		24012				2236
34	27045					24852		24005	23588		22765	
35 36	27037 27030					24845 24838		23998 23991	23581 23574			2235 2234
37	27022	26575				24831						
38	27015	26567		25687	25253	24824	24398					5533
39	27007	26560		25680			24391	23970	23553		22731	2232
40 41	27000 26992	26553 26545	26110	25672 25665	25239 25231	24809 24802		23963 23956				2231 2231
42	26985					24795						2230
13	26977	26530	26088	25650	25217	24788	24363	23942	23526	23113	22704	2229
14 15	26970 26962	26523 26516	26081 26074			24781 24774			23519 23512		22697 22690	
16	26955	26508	26066	25629	25196	24767	24342	23921	23505	23092	22684	2227
47	26947	26501	26059	25621	25188	24760	24335	23914	23498	23086	22677	2227
48 49	26940	26493	26052	25614	25181	21752	24328 24321	23908	23491	23079	22670	2226
	26095	26470	26037	95800	95180	94799	24321	93801	94477	23012 99085	99842	2220
51	26917	26471	26030	25592	25160	24731	24307	23887	23470	23058	22650	2224
52	26910	26464	26022	25585	25152	24724	24300	23880	23464	23051	22613	2223
53 54							24293					
55	26987	26442	26000	25563	25138	24703	24286 24279	23859	23443	23038	22623	22219
56	26880	26434	25993	25556	25124	24696	24272	23852	23436	23024	22616	2221
							24265					
							24258 24251					
		nal Par			.1	.2	3.301		.5			~~.0

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78		TABLE	X.	P	roporti	onal L	ogarith	ms.				
	-				1 De	gree, or	1 Hour					- 11
"	48m	49m	50m	51m	52m	53m	51m	55m	56m	57m	58m	59m
0	22185 22178	21785 21778	21388 21381	20995 20988	20605 20599	20219	19837 19830	19457 19451	19081 19075	18709 18702	18339 18333	17973 17966
5	22171	21771	21375	20982	20593	20207		19445			18327	17960
3 4	22165 22158	21765 21758	CONTRACTOR OF THE PARTY OF THE	20975 20969	20586 20580		DESCRIPTION OF THE PARTY OF THE	19439 19432	19063 19056	7 40 50 50	18321 18315	17954
5	22151	21751	21355	20962	20573		19805		19050		18308	17942
6	22145		100000000000000000000000000000000000000	20956	20567	20181	19799 19792	19420		18672 18665	18302 18296	17936
8	22138 22131	21738 21732	100000000000000000000000000000000000000	100 D D D D	20560		19786	19407	19038		18290	17924
9	22125	-	CO. 12 CO.	20936	20547		19780	19401	19025	_	18284	17918
10	22118	21718	The state of the s	0.35/1/2	20541	20155	19773	19395 19388	19019		18278 18272	17912
12	22105	21705	21309	20917	20528	20143	19761	19382	19007	18634	18266	17900
13	22098 22091	21698 21692	PROPERTY AND ADDRESS.		20522 20515			19376 19369		18628 18622	18259 18253	17894
15	22084	21685	21289	20897	20509	20123	19742	19363	18988	18616	18247	17881
16 17	22078	21678 21672	1000 1000	MACO BY STATE	20502	20117	22022	19357 19351	18982 18976	18610 18604		17875
18	22064	21665	21270	20878	20189	20104	19723	19344	18969	18597	18229	
19	22058	THE OWNER OF THE OWNER OF	21263	RESPONSE N	20483	1	19716	BOOKING LAN	18963	The Section Section 1		See all the latest the
20 21	22051 22044	21652 21645			20476		19710		18957 18951		18217	BERTHAM STREET
22	22038	21639	21243	20853	20164	20079	19697	19319	18944	18573	18204	17839
23	22031 22024		21237 21230		20457		19691 19685				SEASON STATES	District or Street, St.
25	22018	21619	21224	20832	20444	20060	19678	19300	18926	18554	18186	17821
26	22011	21612			20438		11 31 31 31 5 75	REPORT OF	The second			REPORT MATERIAL PROPERTY.
28	21998	21599	21204	20813	20425	20040	19659	19282	18907	18536	18168	17803
29	21991	-	100000000000000000000000000000000000000	-	20418	Control of the last	100 100 100	THE PERSON NAMED IN		18530	Charles Property	-
30	21984 21978	DOMESTIC STREET	The second second	20800	20412	THE RESIDENCE	19647 19640		BOOK STATE OF	The Control of the Co	18155 18149	Designation of the last of the
32	21971	0 DO 0000	SECOND PROPERTY.	BEST STATE OF	20399	HARD STREET,	No. of Concession,	19257	18882	18511	18143	17778
33	2000	21566 21559	A CONTRACTOR OF	10000000	10000000			19250	The second second		18137	
35	21951	21553	21158	20767	20380	19996	19615	19238	18864	18493	18125	17760
36	21944	21546 21540	PURCOUNT NO.	The second second	20373	March Street		100000000000000000000000000000000000000	18857 18851	18487 18480		The second second
38	21931	21533	21139	20748	20361	19977	19596	19219	18845	18474	18107	17742
39	21924				20354	Contract of the last	The State of	_	18839	-	18100	AND DESCRIPTION
41	21911	The second second	FIRST COMPANY			The second second					18094 18088	
42	21904	STATE OF THE PARTY.	Sally and the Control	20722	Participation of	19951	19571	19194	18820	18450	18082	17718
44	21898 21891	20000000	100000000000000000000000000000000000000	1000000	District Street		PACKET PACKET			18443 18437		
45	21884	BACKSTON	1 20 20 20	20702	20316	19932	19552	19175	18802	18431	18064	17700
46	21878 21871	21474	21080	20696	20303	19919	19539	19163	18789	18425 18419	18052	17688
48	21864	21467	21073	20683	20296	19913	19533	19156	18783	18413	18046	17682
50						19907					18040	
51	21844	21447	21054	20664	20277	19894	19514	19138	18764	18394	18027	17663
	21838	21441	21047	20657	20271	19888	19508	19131	18758	18388	18021	17657
53 54	21824	21427	21034	20644	20258	19875	19495	19119	18746	18376	18015	17645
55	21818	21421	21028	20638	20251	19869	19489	19113	18740	18370	18003	17639
56 57	21805	21408	21021	20625	20239	19862	19483	19106	18733	18357	17997 17991	17633
58	21798	21401	21008	20618	20232	19849	19470	19094	18721	18351	17985	17621
			art to to		1 .1	.2	.3		.5	_	17979	8 .9
	1	of " or			1	1	2	3	3	4		6 6
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U	17009	11249	10991	10001	10100	10000	13490	10141	14000	1.2200	14122	13800
1	17603	17243	16885	16531	16179	15830	15484	15141	14801	14463	14127	13795
2	17597		16879	16525	16173	15825	15479	15135	14795	14457	14122	13789
3	17591	17231	16873	16519	16168	15819	15473	15130	14789	14451	14116	13784
4	17585	17225	16868	16513	16162	15813	15467	15124	14784	14446	14111	13778
8	17579		16862				15461			14440		
6	17573	17213	16856					15113	14779	14435	14100	13767
7	17567	17207	16850	16496			15450		14767	14429	14004	19761
		17201	16844			14700	15444	15101	14761	14400	14094	13701
8	17561				10130	15790	10444	10101	14701	14423	14088	13700
9	17555		16838		-					14418		
10	17549	17189	16832	16478	16127	15778	15433	15090	14750	14412	14077	13745
11	17543	17183	16826	16472	16121	15773	15427	15084	14744	14407	14072	13739
12	17537	17177	16820	16466	16115	15767	15121	15079	14738	14401		13734
13		17171	16814							14395		
14			16808							14390		
15		17159			16000	15740	15404	15061	14799	14384	14049	
	17513				16000							
				16443						14379		
17		17147	16791	16437						14373		
18	17501	17141	16785	16431			15387					13701
19	17495	17135	16779	16425	16074	15726	15381	15039	14699	14362	14027	13695
20	17489	17129	16773	16419	16068	15721	15375	15033	14693	14356	14022	13690
21										14351		
	17477									14345		
23	17471			16402		15709	15989	15016	14676	14339	14005	19679
24										14334		
25		17099								14328		
26			16737			15686	15341	14999	14659	14323		
27		17087		16378						14317		13651
28	17441	17082	16725	16372	16022	15674	15330	14988	14648	14311	13977	13646
29	17435	17076	16720	16366	16016	15669	15324	14982	14643	14306	13972	13640
30	17429	17070	71614	16361	16010		15318		and the second of	14300		
31			16708							14295		
32		17058				15051	10012	14971	14031	14289	10001	13029
				16349	15999	10001	10307	14900	14020	14209	13935	13024
33										14284		
34		17046		16337			15295	14954	14614	14278	13944	13613
35	17399	17040	16684	16331						14272	13938	
36	17393	17034	16678	16325			15284				13933	
37	17387	17028	16672	16320	15970	15623	15278	14937	14598	14261	13927	13596
38	17381	17022	16666	16314	15964	15617	15272	14931	14592	14256	13922	13591
39	17375	17016	16660	16308	15958	15611	15267	14925	14586	14250	13916	13585
40	17369	17010	LEGES	A Company of the Comp		and the late of	and the second	4.17	A	14244	12011	19500
41	17363	17004	16649									13574
				10290	10940	15599	15255	14914	14575	14439		
42	17357	16998	16643							14233		
43	17351									14228		
44	17345			16279						14222		
45	17339	16980								14217		
46	17333	16974		16267	15917	15571	15227	14885	14547	14211		13547
47	17327	16968	16613	16261			15221		14541	14205	13872	13541
48	17321	15963	16607	16255			15215			14200		13536
49	17315		16602							14194		
	17309		16596									
50										14189		
51			16590							14183		
	17297		16584	16232	15883	15536	15192	14852	14513	14177	13844	13514
53	17291	16933			15877	15530	15187	14846	14508	14172	13839	13508
54	17285	16927	16572							14166		
55	17279	16921	16566	16214	15865	15519	15175	14835	14496	14161	13828	13497
56	17273 17267	16915	16560	16208	15859	15513	15170	14829	14491	14155	13822	13492
57	17267	16909	16551	16203	15854	15507	15164	14823	14485	14150	13817	13486
58	17261	16903	16540	16192	15848	15509	15158	14818	14480	14144	13811	13481
	17255											
												_
P	roportio			nths	.1	.2	.3			6 .		
		of " or	8.		1	1	2	2	3	4		5

18	0	TABI.	EX.	1	Proport	ional I	Logarit	hms.				
					2 De	grees, or	2 Hou	rs.				
8	12m	13m	14m	15m	16m	17m	18m	19m	20m	21m	22m	23m
	M INDMINIOR	a marcon months	The second	12494 12489				10000000	10914			09994
100	13459	13131	12806	12483	12169	11845	11529	11215	10904	10595	10288	09984
	O DESCRIPTION		The state of the s	12478 12472	150000000	N. St. Control of the	11524	1000000	THE RESERVE	10590 10585	The second second	09978 09973
1	SI DEPOSITION		3000000	200 2166	12147	I REAL PROPERTY.	11513			4 2 0 7 5		09968
1	13431	13104	12779	12456	III DO STORES OF THE PARTY OF T	11818	11503	11189	10878	10569	10263	09958
1 5	a procuped	13099 13093		10000000	LOIGUIGO	11813	10 to 100000	1 SC 20 T ST SC		10559	10253	09953 09948
10	THE PERSON NAMED IN			12440	12120		11487		10863 10858	10554 10549	10247	09943
15	13404	13077	12752	12430	12110	11792	11476	11163	10852	10544	10237	09933
18			12747 12741	12424		PERSONAL PROPERTY.	11471	11158 11153	100 000 000 000	10539 10534		09928
15		13061 13055	12736 12730	Section 2	12094 12088	The board of the	11461 11456	11148 11143	0.570000	10528 10523	10222	09918
17	13377	13050	12725	12403	12083	11765	11450	11137	10827	10518	10212	09908
18		13044 13039	12720 12714	12397 12392	12078 12072		11445		10821 10816	10513 10508	10207	09903
20	III DESCRIPTION OF THE PERSON	13033			12067	11750	11435	11122	10811	10503	10197	09893
21	13355 13349	13028 13023	12703 12698	12381 12376	12062 12056		11429 11424	11117	10806 10801	10498 10493	10192	09887 09882
23	I Debendenting	13017		12371 12365	12051 12046	11734 11729	11419	100 2 4 5 5 6	10796 10791	10487 10482	10181	09877
25	13333	13006	12682	12360	12041	11723	11408	11096	10785	10477	10171	09867
26	13328	13001 12995	12677	12355 12349	12035 12030	11718	11403 11398	11091 11085	10780	10472	10166	09862
28	13317 13311	12990 12985	12666 12660	12344 12339	12025	11708 11702	11393	11080	10770 10765	10462 10457	10156 10151	09852
30	13306	12979	12655	12333	12014	11697	11387	11070	10760	10452	10146	09842
31	13300 13295	12974 12968	12650 12644	12328 12323	12009 12003	11692 11686	11377 11372	11065 11059	10754 10749	10446	10141	09837 09832
33	13289	12963	12639	12317	11998	11681	11367	11054	10744	10436	10131	09827
34	13284	12957 12952	12634 12628	12312	11993 11987	11676 11671	11361 11356	11049	10739 10734	10431	10125	09822
36	13273 13267	12947 12941	12623 12617	12301 12296	11982	11665 11660	11351 11346	11039 11034	10729 10724	10421	10115	09812
38	13262	12936	12612	12291	11972	11655	11340	11028	10718	10411	10105	09802
39	13257	12930	12607	12285	11966	11650	11335	11023	10713	10406	10100	09797
41	13246	12920	12596	12275	11956	11639	11325	11013	10703	10395	10090	09787
42	13240 13235	12914	12590 12585	12269 12264	11950 11945	11634 11629	11320	11008	10698 10693	10390 10385	AND RESIDENCE OF	09782
44	13229 13224	12903 12898	12580 12574	12259 12253	11940 11935	11623 11618	11309	10997	10688 10682	10380	10075	09772
46	13218	12892	12569	12248	11929	11613	11299	10987	10677	10370	10065	09761
47	13213 13207	12887 12882	12564 12558	12243 12237	11924		11294	10982	10672	10365	Deleterated of 1	09756 09751
49		12876	12553		11913	11597	11283	10971	10662	10355	10049	
50 51	13197 13191	12871	12548 12542	12221	11908	11592 11587	11278	10966	10657		10044	
52 53	13186	12860 12855	12537	12216	11897	11581	11267	10956	10646	10339	10034	09731
54	13175	12849	12526	12205	11887	11571	11257	10945	10636	10329	10024	09721
55 56	13169	12844	12521	12200	11882	11566 11560	11252				10019	
57 58	13158	12833	12510	12189	11871	11555	11241	10930	10621	10314	10009	09706
59	13148	12822	12499	12179		11550 11545					09999	09701
F	roportio	nal Par		nths	.1	.2	.3	.4		6 .1		.9
		or or	0,				-	-	4	-	4	-1

Pro	portional	Logarithms.

TABLE X.

2 Degrees,	or 2	Hours.
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3	,			, 1	, 1	,		,	,	-		
8	24m	25m	26m	27m	28m	29m	30m	31m	32m	33m	34m	35m
0	09691	09390	09092	08796	08501	08209			07343	07058	06775	06494
1	09686	09385	09087	08791	08496	08204			07338	07053	06770	06489
2	09681	09380	09082	08786	08491		07908			07049	06766	06485
3	09676	09375	09077	08781	08486		07904			07044	06761	06480
4	09671	09370	09072	08776	08482	08189				07039	06756	06475
5	09666		09067	08771	08477	08184			07319	07034	06752	06471
6	09661	09361	09062	08766	08472	08179			07314		06747	06466
7	09656			08761	08467	08175			07310 07305	07025	06742 06738	06461
8	09651	09351	09052	08756	08462 08457	08170 08165			07300	07020	06733	06457 06452
9	09646	09346	and the second second	08751			-	-			-	-
10	09641	09341	09042	08746	08452	08160			07295 07291	07011 07006	06728 06724	06447
11	09636	09336	09037 09033	08741	08447	08155 08150	07865 07860		07286	07001	06719	06438
15	09631	09331 09326		08736 08732	08438	08146			07281	06997	06714	06433
13 14	09621	09321	09023	08727	08433	08141	07851	07562		06992		
15	09616	100 000 000 000		08722	08428	08136			07272	06987	06705	06424
16	09611	09311	09013	08717	08423	08131	07841		07267	06982	06700	06419
17	09606	09306		08712	08418	08126			07262	06978	06695	06415
18	09601	09301	09003	08707	08413	08121	07831	07543	07257	06973	06691	06410
19	09596	09296	08998	08702	08408	08116	07827	07539	07253	06968	06686	06405
20	09591	09291	08993	08697	08403	08112	07822	07534	07248	06964	06681	06401
21	09586	09286		08692	08398	08107	07817	07529	07243	06959	06677	06396
22	09581	09281	08983	08687	08394	08102	07812	07524	07238	06954	06672	06391
23	09576	09276	08978	08682	08389	08097	07807			06949	06667	06387
24	09571	09271	08973	08678	08384	08092	07802			06945	06663	
25	09566	09266	08968	08673	08379	08087	07798		07224	06940	06658	06377
26	09561	09261	08963		08374	08083		07505		06935	06653	06373
27	09555	09256	08958	08663		08078				06931	06648	06368
28	09550	09251	08953	08658	08364	08073				06926	06644	06364
29	09545	09246	08948	08653	08359	08068	07778	07491	07205	06921	06639	06359
30	09540	09241	08943	08648	08355	08063		07486	07200	06916	06634	06354
31	09535	09236	08939	08643	08350	08058	07769	07481	07196	06912	06630	06350
32	09530	09231	08934	08638	08345	08053	07764	07476 07472	07191	06907 06902	06625 06620	06345 06340
33 34	09525	09220	08929 08924	08633 08628	08340 08335	08049 08044	07759 07754		07181	06898	06616	06336
35	09520 09515	09221		08624	08330	08039	07750		07177	06893	06611	06331
36	09510	09211	08914		08325	08034	07745			06888	06606	
37	09505	09206			08320	08029	07740	07453		06883	06602	06322
38	09500	09201	08904	08609	08316	08024	07735	07448	07162	06879	06597	06317
39	09495	09196	08899	08604	08311	08020	07730	07443	07158	06874	06592	06312
40	09490	09191	08894	08599	08306	08015	07726	07438	07153	06869	06588	06308
41	09185	09186	08889	08594	08301	08010	07721		07148	06865	06583	06303
42	09480	09181	08884	08589	08296	08005	07716		07143	06860	06578	06298
43	09475	09176		08584	08291	08000	07711	07424	07139	06855	06574	06294
44	09470	09171	08874	08579	08286	07995	07706		07134	06850	06569	06289
45	09465	09166		08575	08282	07991	07702		07129	06846	06564	06284
46	09460	09161	08865	08570	08277	07986	07697	07410		06841	06560	06280
47	09455	09156		08565	08272	07981	07692			06836	06555	06275
48	09450	09151	08855	08560	08267	07976	07687	07400	07115	06832	06550	06271
49	09445	09147	08850	08555	08262	07971	07682	07395	07110	06827	06545	06566
50	09440	09142	08845	08550	08257	07966	07678		07105	06822	06541	06261
51	09435	09137	08840	08545	08252	07962	07673		07101	06817	06536	06257
52	09430	09132		08540	08248	07957	07668		07096	06813	06531	06252
53	09425	09127		08535 08530	08243 08238	07952	07663 07658		07091 07087	06808	06527	
54	09420	09122			08238	07942	07654			06803 06799	06517	06238
55 56	09410	09117	08815	08521	08228	07937	07649			06794	06513	06233
57	09405	09107		08516	08223	07933	07644			06789	06508	06229
58	09400	09108	08805	08511	08218	07928	07639		07068	06785	06503	06224
59		09097	No. of Contract of		08213		07634			06780	06499	06219
	roportio				.1	.2	.3	.4		and the same of th	7 .	3 .9
	- opor en	of " or	8.		ō	1	1	2	2			4
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82		TABLE	X.	P	roport	ional I	ogaritl	nms.				
	-11				2 Deg	rees, or	2 Hour	5.				
5	36m	37 ^m	38 ^m	39m	40 ^m	41m	4.2m	43m	44m	45m	46m	47/1
0	06215	05937 05933	05662	05388 05383	05115	04845	04576 04571	04308	04043 04038	03779	03516	03256
5	06206	05928	05652	05378	05106	04836	04567	04300	04034	03770	03508	03247
3	06201	05923	05648	05374 05369	05102	04831 04827	04562	04295 04291	04030	03766 03761	03503	03243
5 6	06192 06187	05914 05910	05639 05634	05365 05360	05093	04822	04558	04286 04282	04021	03757	03495	
7	06189	05905	05630	05356	05084	04813	01544	04277	04012	03748	03486	03225
8 9	06178 06173	05900 05896	05625	05351	05079 05075	04809 04804	04540 04536	04273	04008	03744	03482	03221
10	06168	05891	05616	05342	05070	04800	04531	04264	03999	03735	03473	03212
11	06164 06159	05887 05882	05611	05337	05066	04795	04527	04260	03994	03731	03469	03208
13	06155	05877	05602	05328	05056	04786	04518	04251	03986		03160	03199
14	06150 06145	05873 05868	05597	05324	05052	04782	04513	04246	03981	03717	03455	03195
16 17	06141 06136	05864 05859	05588	05315 05310	05043	04773	04504	04237 04233	03972	03709	03447	03186
18	06131	05854	05579	05306	05034	04764	04495	04229	03963	03700	03438	03178
19	06127	05850		05301	05029	04759	04491	04224	03959	03696	03434	03173
20	06122	05845 05841	05570 05565	05297 05292	05025	04755 04750	04482	04220	03950	03687	03429	03169
22	06113 06108		05561 05556	05288 05283	05016 05011	04746	04478	04211 04206	03946	03682 03678	03416	03160
24	06108	05831 05827	05552	05278	05007	04737	04469	01202	03937	03674		03152
25 26	06099 06094	05822 05818	05547 05543	05274	05002 04998	04732	04464	04198		03669	03408	03147
27	06090	05813	05538	05265	04993	04723	04455	04189	03924	03661	03399	03139
28	06085 06080	05808 05804	05533 05529	05260	04989	04719	04451 04446	04184	03919		03395	03134
30	06076	05799	05524	05251	04980	04710	04442	04175	03911	03647	03386	03126
31	06071 06067	05795 05790	05520		04975	04706	04437 04433	04171 04167	03906			03121
33	06062	05785	05511	05238	04966	04697	04429	04162	03897	03634	03373	03113
34	06057 06053	05781	05506 05501	05233	04962	04692	04421	04158 04153	03893			03108
36	06048	05772	05497	05224	04953		04415	DOUBLE LINES	03884	03621	03360	03100
37	06043 06039	05767 05762	05492 05488	4.50 25750	04948 04944	04679 04674	04411	04144	03880 0387 <i>5</i>	03617	03355	03096
39	06034	05758	05483	LAST SCORE	04939	01670	04402	04136	03871	03608	03347	03087
40	06030	05753 05749	05479	05206 05201	04935	04665 04661	04397	04131	03867	03601	03342	03083
42	06020		05170 05465	0.000.000.000	04926 04921	04656 04652	04388 04384	04122	03858		03334	03071
44	06011	05735	05460	05188	04917	04647	04380	DOMEST PARTY	03853 03849	03591 03586	03329	03070 03065
45	06006	05730 05726	05456 05451	05183	04912	04643 04638	04375	01109	03845	03582	03321	03061
47	05997	05721	05447	05174	04903	04634	04366	04100	03836	03573	03319	03052
48	05993 05988		05442 05438	Subtract and particular	04899	04629	04362	04096 04091	03832	03569	03308	03044
50	05983	05707	05433	05161	04890	04620	04353	04087	03823	03560	0.1299	03039
51 52				05156							03295	
53	05970	05694	05419	05147	01876	04607	04310	01074	03810	03547	0 248	0.3025
54				05147							01232	
56	05956	05680	03406	05133	04863	04594	01326	04061	05796	03534	03273	03014
57 58	05947	05671	05397	05129 05124	04854	04585	01317	04052	03788	03525	03269	03005
59	ALASKA STILLIAN	ACCRECATION AND ADDRESS OF	Section Sectio	05120		THE RESIDENCE				ACCRECATE VALUE OF THE PARTY OF	03260	-
1	roporti	onal Pa		intos	.1	.2	.3	.4	.5		7 .8	
-			-	-		_	_			-	-	_

					2 Deg	rees, or	2 Hou	rs.				
"	48m	49m	50m	51m	52m	53m	54m	55 ^m	56m	57m	58m	59m
0	02996		02482	02228	01974	-	01472	01223	00976	00730	0018/	00242
ĭ	02992	COLUMN TO A STATE OF	The second second	02223	01970	Comment of	01468	01219	00972	00721	00481	00238
2	02988	02730		02219	01966		01464		00968	00722	00477	00234
3	02983	Terrendo de		100000000000000000000000000000000000000	11-75	2000		The Control of the	00964		0017:	00230
4	02979		02465	2000	01958	CONTRACTOR STATE	01456 01452	01207	00960	00714		00226
5	02975				01953		01447			00705		00218
6	02966	Terreton at	Company of Company			01693				00701	0015	00214
8	02962				01941				00943	00697	00453	
9	02958		02444	02190	01937	01685	01435	01186	00939	00693	00149	00206
10	02953	02696	02440		01932		01431	01182			00445	00202
11	02949				01928		01427	01178		00685		0.)197
12	02945					01672				00681	00436	
13	02940					01668		01170			00432	
14 15	02936	The second of	02419						00914			
16	02927		02414	02160	01907	01656						
17	02923		02410	02156	01903	01652	01402					
18	02919			02152	01899	01647	01398					
19	02915	02657				01643			_			
20	02910	The second second				01639			00894			
21	02906				01886	01635 01631					00 400	
22	02902	02644				01627	01377			00636		00149
23 24		02636	1.32 2.5.			01622						
25	05888	The second				01618						
26		02627				01614					00380	
27		02623				01610						10. 2. 2. 2
28		02619			01857				12 4 4 4 5	00616	00372	
29	_	-	02359	-			01352		00857	00611	00367	00125
30	02867	02606	The state of the s		01848	01597 01593	01348	01100 01095	00853 00849	00607	00363	00121
31 32		05905				01589	01339		00845	00599		
33		02597	44444			01585		01087				
34	02850		02338		01832			01083			00347	
35	02846										00343	
36	02841					01572		01075	00828			
37 38	02837 02833			02071		01564			00820		00331	00089
39	02829	man calmi	02317		01811	01560	01310		10000	00571	00327	
40	02824	_	-		01806	_	01306			00567		0 4 80
41	02820	0.75	DESCRIPTION AND ADDRESS OF THE PARTY AND ADDRE		01802		01302			00563	the facilities of	00076
42	02816	2 5 5 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6	02304			01547	01298		00804	00559		00072
43	02811					01543			00799			00068
44	02807					01539			00795	00550		00064
45 46	02803 02799	A CAST OF A CAST			01785		01286	01038	00787			
47	02794	Programme and the second		02029		01526		01029				
48	02790			02025	01773	01522						
49	02786	02529	02274	02021	01769	01518	01269	01021	00775	00530	00286	00014
50	02781	02525	02270	02017	01764	01514	01265	01017	00771	00526	00585	00040
51	02777	02521	05566	05015	01760	01510	01561	01013	00767	00522	00278	00036
	02773	02516	02262	02008	01756	01506	01257	01009	00763	00518	00274	00032
53	02769	02512	02257 02253	05001	01752	01407	01202	01003	00754	00510	00270	00028
54 55	02760	02504	02249	01995	01744	01493	01244	00997	00750	00506	00262	00050
56	02756	02499	02245	01991	01739	01489	01240	00992	00746	00502	00258	00016
57	02751	02495	02240	01987	01735	01485	01236	00988	00742	00497	00251	00012
58	02747	02491	02236	01983	01731	01481	01232	00984	0073H	00193	00250	00008
59			02232									
·P	roporti			nths	.1	.2	.3	.4			7 .1	
_	_	of " or	8.		0	1	1	2	8	4	3	3

84 TABLE XI. TABLE XIII.-Correction to be added to the Observed Altitude of the Sun's Lower Limb, when taken by a Depression or Dip of Fore Observation, to find the True Altitude. the Horizon. Height of the Eye above the Sea in Feet. Dip of Height Horiz of Eye. Dip of Horiz Obs Alt. 12 14 16 18 20 22 30 24 26 28 11 11 ø 0 16 3 58 5 3.8 3.5 3.1 2.8 2.5 2.3 2.1 1.8 1.6 1.4 1.9 0.8 1.0 14 1 7 4 2 161 6 5.3 4.9 4.6 4.3 4.0 3.7 3.5 3.3 3.0 2.8 2.6 2.4 2.2 16 1 13 17 5 7 6.4 6.0 5.7 5.1 4.4 4.1 3.9 3.7 3.5 3.3 5.4 4.8 4.6 19 1 175 9 7.2 6.8 6.5 6.2 5.9 5.7 5.4 5.3 5.0 4.8 4.2 4.6 9 1 24 18 4 12 9 7.2 7.9 7.5 6.9 6.6 6.4 6.1 5.9 5.7 5.5 53 5.1 4.9 184 21 1 29 4 16 10 8.5 8.1 7.8 7.5 7.2 6.9 6.7 6.5 6.2 6.0 5.8 5.6 5.4 21 1 34 19 19 11 8.9 8.6 8.2 7.9 7.4 6.9 6.7 6.5 6.3 7.6 7.2 6.1 5.9 23 1 191 39 4 23 12 9.3 9.0 8.7 8.3 7.6 7.3 6.9 8.0 7.8 7.1 6.7 6.5 6.3 43 20 4 26 9.6 9.2 8.9 8.2 7.9 7.7 14 9.9 8.7 7.5 8.4 7.3 7.1 6.9 31 1 47 21 4 33 16 10.4 10.1 9.7 8.9 8.7 8.4 8.2 8.0 7.8 9.4 9.1 7.6 7.4 3 51 22 4 39 18 10.8 10.4 10.1 9.8 9.5 9.3 9.0 8.8 8.4 8.2 8.6 8.0 7.8 34 55 99 46 9.6 20 11.1 10.7 10.4 10.1 9.8 93 9.1 8.9 8.7 8.5 8.2 8.1 59 24 52 22 11.4 11.0 10.7 10.4 10.1 9.8 9.6 9.4 9.1 8.9 8.7 8.5 8.3 2 3 25 4 58 26 11.7 11.4 11.0 10.7 10.5 10.2 10.0 9.7 9.5 30 12.0 11.7 11.3 11.0 10.8 10.5 10.3 10.0 9.8 9.3 8.7 9.1 8.9 2 41 6 26 5 4 9.6 9.4 9.2 9.0 10 10 43 2 27 5 35 12.3 11.9 11.6 11.3 11.0 10.7 10.6 10.3 10.1 9.7 9.9 9.4 9.2 5 2 13 28 5 16 40 12.5 12.2 11.8 11.5 11.3 11.0 10.8 10.5 10.3 10.1 9.9 9.7 9.5 51 2 17 29 5 22 45 12.7 12.4 12.0 11.7 11.5 11.2 11.0 10.7 10.5 10.2 10.1 9.7 5 2 20 30 5 97 50 12.8 12.5 12.2 11.9 11.6 11.3 11.1 10.9 10.6 10.4 10.3 10.0 9.8 2 54 23 5 32 31 55 13.0 12.6 12.3 12.0 11.7 11.5 11.2 11.0 10.7 10.5 10.3 10.1 9.9 2 26 32 5 37 6 60 13.1 12.7 12.4 12.1 11.8 11.6 11.3 11.1 10.9 10.6 10.4 10.2 10.1 61 2 32 33 5 42 65 13.2 12.8 12.5 12.2 11.9 11.7 11.4 11.2 11.0 10.7 10.5 10.3 10.1 70 13.3 12.9 12.6 12.3 12.0 11.8 11.5 11.3 11.0 10.8 10.6 10.4 10.2 80 13.4 13.1 12.7 12.4 12.1 11.9 11.7 11.4 11.2 11.0 10.8 10.6 10.4 2 38 34 5 47 71 2 43 35 5 53 2 8 48 36 5 58 90 13.6 13.2 12.9 12.6 12.3 12.0 11.8 11.6 11.3 11.1 10.9 10.7 10.5 2 53 84 6 2 Month. Jan. Feb. Mar. May, April, June, 9 2 58 38 6 + 0'.3 + 0'.2 +0'.1 0'.0 -0'.1 Correction. - 0'.2 91 3 39 6 12 July, Month. Aug. Nov. Sept. Oct. Dec 10 3 8 40 6 17 -0'.2 -0'.3 Correction, -0'.1 + 0'.1 + 0'.2 + 0'.3 101 3 12 42 6 26 m 3 17 TABLE XIV .- Correction to be subtracted from the Ob-44 6 35 114 3 21 6 44 46 served Altitude of a Fixed Star, to find the True Altitude. 12 3 26 6 52 Height of the Eye above the Sea in Feet. Obs 121 3 31 50 10 | 12 | 14 | 16 | 18 | 20 122 | 24 Alt 26 3 35 7 21 13 55 134 3 39 60 7 41 12.3 12.7 13.0 13.3 13.6 13.8 14.1 14.3 14.6 14.8 15.0 15.2 15.3 3 43 70 18 6 10.9 11.3 11.6 11.9 12.2 12.4 12.7 12.9 13.2 13.4 13.6 13.8 13.9 144 3 47 8 80 53 9.8 10.2 10.5 10.8 11.1 11.3 11.6 11.8 12.1 12.3 12.5 12.7 12.8 7 15 3 51 90 9 25 9.9 10.2 10.4 10.7 10.9 11.2 11.4 11.6 11.8 11.9 8 8.9 9.3 9.6 154 3 55 100 9 56 8.6 8.9 9.5 9.7 10.0 10.2 10.5 10.7 10.9 11.1 11.2 9 8.2 9.2 TABLE XII. 10 7.7 8.1 8.4 8.7 9.0 9.2 9.5 9.7 10.0 10.2 10.4 10.6 10.7 11 7.2 7.6 7.9 8.2 8.5 8.7 9.0 9.2 9.5 9.7 9.9 10.1 10.2 Dip at differ. Distances 12 6.8 7.2 7.5 7.8 8.1 8.3 8.6 8.8 9.1 9.3 9.5 9.7 9.8 from the Observer. 14 6.2 6.6 6.9 7.2 7.5 7.7 8.0 8.2 8.5 8.7 8.9 9.1 9.2 Height of the Eye 16 5.7 6.7 7.0 8.0 6.1 6.4 7.5 7.7 8.2 8.4 8.6 8.7 7.2 in Feet. 18 5.3 5.7 6.0 6.3 6.6 6.8 7.1 7.3 7.6 7.8 8.0 8.2 8.3 10 |15 |20 |25 |30 20 5.0 5.4 5.7 6.0 6.3 7.3 8.0 6.5 6.8 7.0 7.5 7.7 7.9 1' 23' 34' 45' 57' 68' 6 12 17 23 28 34 11' 23' 22 4.8 6.3 7.3 5.2 5.5 5.8 6.1 6.6 6.8 7.1 7.5 7.7 7.8 5.4 5.7 6.2 26 4.4 4.8 5.1 5.9 6.4 6.7 6.9 7.1 4 12 15 19 23 4.1 5.1 70 30 4.5 4.8 5.4 5.6 5.9 6.1 6.4 6.6 6.8 7.E 3 6 9 12 15 17 6.3 35 3.8 4.2 4.5 4.8 5.1 5.3 5.6 5.8 6.1 6.5 R.R 3 7 10 12 14 40 3.6 4.0 4.3 4.6 4.9 5.1 5.4 5.6 5.9 6.1 6.3 6.5 14 3 8 10 6 12 45 3.4 3.8 4.1 4.4 4.7 4.9 5.2 5.4 5.7 5.9 6.1 6.3 6.5 2 2 5 7 8 9 50 3.2 3.9 4.2 4.5 4.7 5.2 5.7 5.9 6.1 6.3 3.6 5.0 5.5 2 8 4.4 21 3 4 6 7 55 3.1 3.5 3.8 4.1 4.6 4.9 5.1 5.4 5.6 5.8 6.2 4.3 7 3 2 3 5 6 60 3.0 3.4 3.7 4.0 4.5 4.8 5.0 5.3 5.5 5.7 5.9 6.1 34 2 2 3 5 6 6 65 2.9 3.3 3.6 3.9 4.2 4.4 4.7 4.9 5.2 5.4 5.6 6.0 2.8 3.2 4.3 3 5 6 70 3.5 3.8 4.1 4.6 4.8 5.1 5.3 5.5 5.7 5.9 5 3 6 80 2.6 3.0 3.3 3.7 3.9 4.1 4.6 4.9 5.1 5.3 5 5 2.8 3.1 3.4 3.7 3.9 4.7 4.9 5.1 5.5 90 2.4 4.2 4.4

			ABLE emi-dia		&c.					LE		-		85
4	Ŋ	Time of Sun's Sdiam.	Sun's	Sun's Hourly	Sun's		Sur	's Pa		X in			-	
Month.	Days.	passing Merid.	diameter.	Motion.	Distance.	Z.D.	Alt	Jan.		Nov.		Sept.		July.
		m. s.	1 "	. "	Falviv		-	Par.	Par.	Par.	Par.	Par.	Par.	Par.
					9.992659	0	90	0.00	1.00	0.00	178	100	2.0	0.00
a,	7				9.992727	1	89	0.15			0 15		0.15	
January	13 19				9.992852 9.993046	2	88	0.31	0.31	0.31	0.30	0.30	0.30	
ř	25				9.993329	3	87	0.46			0.45		1000000	0.45
	1	1 8.1			9.993779	5	86 85	0.62	0.62		0.61	0.61	0.60	0.60
February.	7				9.994231	6	84	0.93		0.92		Marie Barrier	0.89	10000
n n	13	20 772	with the same of		9.994722	7	83	1.08				1.05	200	1000
Fe	19 25				9.995879	8	82	1.23	200	42.73.5			1.19	
-	1	1 5.2		_	9.996323	-	81	1.38	-	-		1.35	_	
å	7				9.997016	10	80 79	1.53	100 2 20	6.1	1.66	1.64	100000	1.68
March.	13	1 4.5	16 6.5	2 29.4	9.997719	12	78	1.84					1.77	1.76
Σ	19	V 170			9.998431	13	77	1.99	1.98	1.97	1.95	1.93	1.92	1.91
_	25			-	9.999170	14	76 75	2.14						2.06
	7	1 4.2			0.000068	15 16	74	2.29	200	2.27			2.22	2.21
Pr.	13				0.001554	17	73	2.59				2.52		
₹	19		15 56.4	2 26.3	0.002254	18	72	2.73			2.68			
	25			_	0.002948	19	71	2.88						
					0.003626	20	70	3.02	500 C	3.00	2000	2.94	100000	
May.	13				0.004254	22	69	3.17	3.16	3.14	200		3.06	
Σ	19				0.005323	23	67	2000	3.44		3.39		3.34	
	25				0.005794	24	66		3.58		3.53		3.48	
	1				0.006281	25	65			3.70				00000
je.	7				0.006616	26	63	3.87	72.7 2.2	3.84				
June.	13				0.006864	28	62	4.14	2277.0		4.07			4.00
9	25				0.007173	29	61	1 1 1 1 1 1	4.27	1.00	4.21		4.15	
	1	1 8.5			0.007237	30	60	4.41	4.40	4.38	4.34	4.30	4.28	4.27
·	7	1 8.3	15 45.5	2 23.0	0 007212	32	58	4.68	100,000		4.60		100 0000	
July.	13				0.007095	34	56 54	5.19	W. C. C.	4.89 5.14			1772	4.78
,	19				0.006910 0.006675	38	52	5.44	10,000			7		1000
-	1	1 6.5		_	0.006325	40	50	5.68		2. 1.4.0		5.53		
4					0 005933	42	48	5.92	10000	COLUMN TO SERVICE AND ADDRESS OF THE PARTY O			5.72	
August.	13				0.005463	44	46	6.15	6.13			5.98		1000
¥	19				0.004949	48	42	6.57	6.55	100.00	6.24	100	1. 1. (2.)	1000
	25			_	0.001403	50	40	6.77	6.75	_		6.60		_
September.	7				0.003705	52	38	6.97			6.84			40.00
Ē	13				0.003040	54	36	7.15				6.96	6.91	State In the
pte	19	1 3.8			0.001617	56 58	34	7.33		7.27	7.20		1.000	50.000
Š	25				0.000898	60	30			7.43				
	1				0.000162	62	28	7.80	7.78	7.73	7.66	7.59	7.54	7.53
October.	13				9.999398 9.998633	0.5	26	7.94	7.92	7.87	7.80	7.73	7.68	7.66
cto	19				9.997898	66 68	24			8.00				
0	25				9.997200	70	22			8.12				_
÷	1				9.996411	72	18	8,41	8.39	8.23	8.26	8.19	8.04	8.02
November.	7				9.995749	74	16	8.49	8.47	8.42	8.34	8.27	8.22	8.20
ven	13				9.995135	76	14	8.57	8.55	8.50	8.42	8.35	8.30	8.28
S.	19 25				9.994592 9.994120		12	8.64	8.62	8.57	8.49	8.42	8.37	8.35
_					9.993697	80	10			8.63 8.68				
per					9.993322	84	6			8.71				
December.	13	1 10.8	16 16.9	2 32.6	9 993024	86	4	8.81	8.79	8.74	8.66	8.59	8.54	8.59
ě					9.992823		2	8.82	8.80	8.75	8.67	8.60	8.55	18.5
,	2.5	1 11.0	16 17.7	2 32.9	9.992714	90	0	8.83	8.81	1876	18.6	9.8 16	1/82	8/0

1	- 1-27 (F	ahrenhei	t's Th	ermo	me	ter	500	English	Baron	meter 30) [nches.	Same II	
7 17	80	E Village All	:0161	BY.		-	30	Log. 80		Lean	-	30	Ton 34	Diff.
Z.D.	0 8	Log. de	Ditt.	2.	D.	-	00	Log. 00	Din.	2. D.	1	00	Log. 30	Dill.
0 0	0 0.00	0.0000		10	0	0	10.30	1.0129	72	20 0	0	21.26	1.3277	38
10	0.17	9.2304	3011	-	10	-	10.47	1.0901	72	10		21.45	1.3315	39
20	0.34	9.5315	1761	***	20	9	10.65	1.0273	71	20		21.65	1.3354	39
30	0.51	9.7076	1249		30	2	10.82	1.0344	70	30		21.84	1.3393	38
40	0.68		969	100	40	2	11.00	1.0414	69	40		22.03	1.3431	38
50	0.85		791		50	_	11.17	1.0483	69	50	-	22.23	1.3469	38
1 0		0.0085	670	11	10	0	11.35	1.0552	66	21 (22.42	1.3507	37
20	1.19	0.0755	580		20	1	11.53	1.0618	66	20		22.62 22.81	1.3544	38
30	1.53		457	100	30	1	11.89		65	30		23.01	1.3619	37
40	1.70	0.2304	414		40		12.06		64	46		23.21	1.3656	37
50	1.87	0.2718	379	100	50		12.24	1.0879	62	50)	23.40	1.3693	36
2 0	0 2.04	0.3097	347	12		0	12.42	1.0941	62	22 (23.60	1.3729	37
10	2.21	0.3444	322		10	ı	12.60	1.1003	61	10		23.80	1.3766	36
20	2.38 2.55	0.3766	301	1	30		12.78	1.1064	60	20		24.00		36
30 40	2.55	0.4067	263		40		12.95	1.1124	58	40		24.20	1.3838	36
50	2.89	0.4610	250	1	50		13.31	1.1242	58	50		24.60	1.3909	36
3 0	CA SHARE	0.4860	235	13	1000	ō	-	1.1300	57		0	24.80	1.3945	36
10	3.23	0.5095	224	1	10		13.67	1.1357	57	10		25.00	1.3981	34
20	3.40	0.5319	211	-	20	H	13.85	1.1414	55	20		25.20	1.4015	34
30	3.57	0.5530	203	m	30		14.02	1.1469	55	30		25.41	1.4049	35
40	3.74	0.5783	193	88	40	a	14.20		54	40		25.61	1.4084	34
50	3.91	0.5926	186	-	50	_	14.38	1.1578	56	50		25.81	1.4118	33
4 0	0 4.08 4.26	0.6113	178	14	10	0	14.56	1.1634	52 54	24 (26.01	1.4151	34
20	4.43	0.6290	171 165	-	20	1	14.74	1.1686	53	20		26.21	1.4185	34
30	4.60	0.6626	158	93	30	3	15.11	1.1793	52	30		26.62	1.4253	33
40	4.77	0.6784	153	355	40	a	15.29	1.1845	52	40		26.83	1.4286	33
50	4.94	0.6937	149	12	50		15.48	1.1897	50	50)	27.03	1.4319	33
5 ()		0.7086	142	15	0	0	15.66	1.1947	51		0	27.24	1.4352	33
10	5.28	0.7228	139	100	10	g	15.81	1.1998	50	10		27.45	1.4385	33
20	5.45	0.7367	135	an	20	V	16.03	Application of the control of the co	50	20		27.66	1.4418	33
30 40	5.63 5.80	0.7502	131	100	30	ı	16.21 16.39	1.2098	49	30		27.86	1.4451	32
50	5.97	0.7760	122	6.0	50		16.58	1.2195	46	50		28.28	1.4515	32
6 0	AND ROWSELL STATE	0.7882	120	16	U	0	16.75	1.2241	46	26 0	-	28.49	1.4547	32
10	6.31	0.8002	116	NA PAR	10		16.93	1.2287	47	10		28.70	1.4579	32
20	6.48	0.8118	114		20		17.12	1.2334	46	20		28.91	1.4611	32
30	6.66	0.8232	111		30		17.30	1.2380	46	30		29,13	1.4643	31
40	6.83	0.8343	108		40		17.48	1.2426	46	40		29.34	1.4674	32
2.0	7.00	0.8451	106	00	50	1	17.67	1.2472	47	50	-	29.55	1.4706	30
7 0	0 7.17 7.34	0.8557	102	17	10	U	17.86 18.05	1.2519	45	27 0		29.76	1.4736	32
20	7.52	0.8760	99	19-3-	20		18.23	1.2609	44	10		29.97	1.4768	31
30	7.69	0.8859	97	20.4	30		18.42	1.2653	44	30		30.40	1.4829	31
- 40	7.86	0.8956	95		40		18.61	1.2697	43	40		30.62	1.4860	30
50	8.04	0.9051	93	1	50		18.79	1,2740	44	50	1	30.83	1.4890	31
8 0		0.9144	90	18	0	0	18.98	1.2784	42	28 (0	31.05	1.4921	31
10	8.38	0.9234	89		10		19.17	1.2826	42	10		31.27	1.4952	30
20 30	8.56	0.9323	87		20		19.36	1.2868	42	20		31.49	1.4982	31
40	8.90	0.9410	85 84		30	U	19.55	1.2910	42	30		31.72	1,5013	30
50	9.08	0 9579	84		50		19.92	1.2991	42	50		32.16	1.5043	29
B 11 / 12 / 1	0 9.25	0.9663	80	19	100	0	20.11	1.3036	39	29 ()	-	32.38	1.5102	31
10	9.42	0.9743	80	1.11	10		20.30	1.3075	39	10		32.60	1 5133	29
20	9.60	0.9823	78		20		20.49	1.3116	41	20	1	37.83	1.5162	30
30		0.9901	77		30			1.3157	41	30	1-		1 5192	29
40	9.95	0.9978	76	+ 11	40		20.88	1.3197	40	40	11.	33.27	1.5991	29

75 72

9.95 0.9978 10.12 1.0054 10.30 1.0129

20 0

20.88 1.3197 21.07 1.3237 21.26 1.3271

0 0 32.38 1.5102 10 32.60 1.5133 20 32.83 1.5162 30 33.05 1.5192 40 33.27 1.5221 50 33.50 1.5250

33.72 1.5279

Fahrenheit's T	hermometer 50°.	English I	Barometer 30 Inches.
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	_		autennen		CELLIOI	meu		English			30	-	urnieg.		_
Z. D	1	88	Log. 8 #	Diff.	Z. I	D.	88	Log. 8	Diff.	Z. I	2.	,	80	Log. 8	Di
	olo	33.72	1.5279	29	40	0	0 48.9	1.69010	257	50	0	1	9.52	1.84208	2
	ol		1.5308	29		10		1.69267			10		ME 123.7	1.84464	
2			1.5337	29		20	49.5	1.69523	257		20			1.84721	
3			1.5366	29		30		1.69780			30			1.84977	
4	_		1.5395	28		40		6 1.70037			40			1.85234	
5		34.86	1.5423	29		50	50.4	6 1.70293	257		50			1.85490	
	00	00,00		29	41	~		1.70550		51	0	1		1.85747	
1		35.32		29		10		6 1.70804			10			1.86005	
2		35,56		28		20		6 1.71058			20			1.86264	
3		35.79		28		30		6 1.71311			30			1.86522	
4		36.02		28		40		6 1.71564			40 50			1.86781	
_	0	36.26		28	-15	50	-	1.71818	-	_	_	-			-
	00		1.5622	28	42	-		1.72070		52	10	ı		1.87298	
	0	36.73		28 29		10 20		8 1.72322 9 1.72574	The second		20			1.87558 1.87819	
3	0	37.21		28		30		01.72826	112 332		30			1.88080	
	0		1.5735	27		40		11.73078	100		40			1.88341	
100	0	37.69		28		50		21.73329	100000		50			1.88601	1
	00			28	43	0		3 1.73580	_	53	0	1		1.88863	-
	0	38.17		27		10		1.73833	Contract of the last		10			1.89125	
	0	38.42		28		20		1.74087			20		18.33	1.89387	2
3	0	38.66	1.5873	27		30	55.4	0 1.74340	253		30			1.89650	
	0	38.90		27		40		2 1.74593			40			1.89913	
	0	39.15		27		50		4 1.74847	-		50		-	1.90176	
	UO			27	44	0		5 1.75100		54	0	1		1.90440	
	0	39.64		28		10		8 1.75352			10	1		1.90705	
2		39.89		27		20		21.75604			20			1.90970	
3	-		1.6036	27		30		5 1.75856 9 1.76108			30 40			1.91236	
5		40.39	0.2022	27 26		50		2 1.76108	100000		50			1.91502	
	o o		1.6116	27	45	0	-	1.76611	-	55	0	1	-	1.92036	-
35	24.		1.6143	27	45	10		1.76863		200	10	•		1.92304	
2			1.6170	27		20		1.77115	77.7		20			1.92573	
3		7.7	1.6197	26		30		1.77367	1000000		30	ľ		1.92841	
4	0	41.91	1.6223	27		40	59.7	1.77619	252		40		25.36	1.93112	2
5		42.16		26	6.	50		8 1.77871	252		5 0		25.88	1.93382	2
36	ōŌ	100 400 200	1.6276	27	46	0		3 1.78123		56	0	ı		1.93659	
1	_	42 68		27		10		9 1.78375			10			1.93924	
2	-	42.95		26	1	20		1.78628	The same of		20		1	1.94196	
3		43.21		26		30		01.78880			30			1.94469	
4	-	43.47		26 27		40	-	6 1.79132	100000		40 50	Sq.		1.94742	
5		43.74			-	50		1 1.79385		_	-	1	_		
-	00			26	47	10		1.79637	1000	57	10		10.00	1.95291	
1 2		44.27	1.6461	26 26		20		4 1.79890 1 1.80143			20			1.95566	
3		44.80		26		30	7.7	91.80396			30			1.96120	
4		45.07	1.71.3.77	26		40		61.80649			40			1.96397	
	o		1.6565	26		50		1.80902			50			1.96676	
	00		1.6591	26	48	0		1.81155	_	58	-	1		1.96955	
1	se la	45.89	1.6617	26		10		1.81409			10	1		1.97235	
2	0	46.16	1.6643	26		20	5.5	1.81663	253	1.0	20		34.46	1.97516	2
3	0		1.6669	26		30		1.81916			30			1.97797	
4	0		1.6695	25		40	6.3	1.82170	254		40			1.98080	
_	0		1.6720	26		50		21.82424			50			1.98362	-
			1.6746	26	49	0		1.82678		59		ı		1.98646	
	0		1.6772	26		10		11,82933			10			1.98931	
	0		1.6798	26		20		1.83188			20	19		1.99216	
	0		1.6824	26		30		1.83448			30	1		1.99503	
	0		1.6850	26		40		1.83698			40	0		1.99790 2.00079	
	0		1.6876	25	50	50		1.83953 1.84208			50	6		2.00368	
WU .	ч_	49.33	1.0901	103	OU.	엑	9.0.	11.04208	230	00	U	-	10.00	12.00000	1 6

Fahrenheit's Thermometer 50°. English Barometer 30 Inches.

Z.D.	20	Log. b	D.	Z.D.	1	80	Log. 80	D.	$\frac{d\delta\theta}{d\tau}$	Z.D.		8 8	Log. 30	Diff	d 8 0 d 7	did
0 1	' "	22100		0 /	1	"		100	170	01	1	"		100	-	п
0 0		2.00368		10000000			2.20185			80 0	5		2.50541		0.030	-
10		2.00658		10			2 20573		100	10			2.51237		0.031	
20		2.00949		30			2 20963 2.21356		178	20 30			2.52660		0.033	
30		2.0153		40			2.2175		199	40			2.53387	10000	0.034	
50		2.01829		50			2.22150			50	я		2.54125		0.038	
1 0		2.02124	1		-	2000	2 22552	-	-	-	5		2.54874		0.040	80
10		2.0212		10	107		2.22956		10	81 0			2.55635	100000	0.048	
20		2.02718					2.23363		6	20	0		2.56407		0.044	
30		2.0301					2.23773		6.00	30	я		2.57192		0.046	
40		2.0331	of Inches of	40			2.24186			40		District Co.	2.57989		0.049	
50		2.0361		50			2.24603		550	50		6 4 6 6	2.58800		0.051	
20	1 49.44	2.03918	303	72 0		10000000	2.25022			82 0	-	THE RESERVE	2.59624		0.053	-0
10		2.0422		10	10.7		2.25445		3	10	_		2.60462	Million and red	0.057	- 10
20	50.99	2.0452	305				2.25870	10000	6 (4)	20		The state of the s	2.61313		0.060	
30		2.04830					2.26299		100	30			2.62179		0.063	
40	52.57	2.0513	308	40		5.06	2.26732	436		40	7	7.19	2.63062	899	0 067	7 0
50	53.36	2.0544	309	50		6.93	2.27168	440	(44)	50		16.13	2.63961	914	0.071	LK
3 0	1 54.17	2.0575	310	73 0	3	8.83	2.27608	443		83 0	7	25.40	2.64875	931	0.074	ik
10	54.99	2.06064	1312	10		10.77	2.28051	447	0.003	10		35.05	2.65806	949	0.079	916
20	55.81	2.06370	312	20		12.74	2.28498	450	0.003	20	-	45.10	2.66755	967	0.084	K
30	56.66	2.06688	3 315	30		14.75	2.28948	454	0.004	30		55.58	2.67722	986	0.089	1
40		2.0700					2.29402			40	8		2.68708			
50	A CONTRACTOR OF THE PERSON NAMED IN	2.0731		50		18.88	2.29860	462	0.005	50	1	17.90	2.69714	1026	0.101	ľ
-		2.0763			3		2.30322				8		2.70740			
10		2.0795					2.30789						2.71787			
20		2.08273		20		-	2.31259	100000	and a	40.00			2.72856			
30	100000	2.0859	OF REPORTS	100			2.31734			30	-		2.73948	Printed in the		
40		2.0891		40			2.32213						2.75063			
50		2.0924	2000		_	Telephone Street	2.32696	-	No. of Concession, Name of Street, or other Persons and Street, or other P	50			2.76202	Name and Address of the Owner, where the Owner, which is the Own	-	10
5 ()		2.0956			-		2.33184						2.77367			
10		2.0989				175 A B 175 A	2.33677	10000	The second second		10		2.78558			
30		2.1022				100000	2.34174	200	THE REAL PROPERTY.				2.79777			
40	11/00/00	2.1033	or bedience	1000	20	975.70	2.35183	1003.0	1000000		11		2.82302	THE OWNER OF	MODEL OF THE PARTY OF	•
50		2.1122				1000000	2.35695	1000	20.00	50	**		2.83611	PORTON NA		•
6 0		2.1155			1	50.21		_			11	No. of Concession, Name of Street, or other Publisher, Name of Street, Name of Street, or other Publisher, Name of Street, or other Publisher, Name of Street, Nam	2.84951	THE REAL PROPERTY.		
10	10 March 2017	2.1189	OF REAL PROPERTY.		1-		2.36735				12		2.86325			
20	100000000000000000000000000000000000000	2.1223	District Co.	100.00			2.37263					100	2.87735	Indicated in		
30		2.1257					2.37796				_		2.89182			
40		2.1291					2.38334						2.90666	DOM: N		
50		2.1325					2.38879						2.92189			
7 0	2 16.78	2.1360	3 348	77 0	4	7.91		_			14		2.93751	PRODUCTION	100000	100
10		2.1395			1	11.11					-		2.95362			
20	10000000	2.1430					2.40550				15		2.97016			
30		2.1465					2 41119						2.98717			
40		3 2.15000			1		2.41695			40	1	50.8	3.00466			
50	22.43	32.1536	1 358	50	1 5	24.72	2.42278	589	0.017	, 50	17	33.6	3.02267	1855	0.654	1
8 0	2 23.6	₹.1571	9 359	78 0	1	28.33	2.42867	596	0.018	88 0	18	19.6	3.04122	1909	0.722	I
10		2.1607			1		2.43463				19	9.0	3.06031	STATE STATE OF	NAME AND ADDRESS OF	
20	26.0	2.1644	0 364	20			2.44066				20		3.07998			
30		2.1680				39.75	2.44677	618	0.020	30			3.10024			
40		2.1717					2.45295				55		3.12113			
50		8 2.1753				100000	2.45921	AND MANAGE	THE RESIDENCE OF	1	23		3.14268	MONROOM	-	
9 0		2.1791					2.46556						3.16489			
10		2.1828					2.47198						3.18779			
20		2.1865			5		2.47848				27		3.21140			
30		2.1903					2.48507						3.23574			
501		2.1941					2.49176						3.26083			
	767.76	6 2.19800	JUNE S	50	11	15,16	2.49853	1088	10.028	90 0	132	15.0	3.28667	2007	2.019	5

TABLE XVIII							89			TAB. XXThermometer				
			-	200					Th.	Log.	Th.	Log.		
		Therm	omet	er.					100	0.00173	50°	0.00000		
							TABLE XIX.			0.00169	51	9.99996		
P. P. Th. Log. P. P. Th. Log.										0.90164	52	9.99991		
-1	100	0.03779	_	50°	0.00000				13	0.00160	53	9.99987		
10	1	0.03680	9	. 1	9.99910	1	Barom	eter.	14	0.00156	54	9.99983		
20	2	0.03582	18	2	9.99820	0.7		9,049	15	0.00151	55	9.99978		
29	3	0.03484	27	3	9.99730			-5	16	0.00147	56	9.99974		
39	4	0 03386	36	4	9.99640	P. P.	Bar.	Log.	17	0.00143	57	9.99970		
49	5	0.03288	45	5	9.99550		27.5	9.96221	18	0.00138	58	9.99965		
59	6	0.03191	54	6	9.99460		6	9.96379	19	0.00134	59	9.99961		
69	7	0.03094	63	7	9.99371		7	9.96536	20	0.00130	60	9.99957		
78	8	0.02997	72	8	9.99282		8	9.96692	21	0.00126		9.99955		
88	9	0.02900	81	9	9.99193		9	9.96848	22	0.00121	65	9.99948		
-	20	0.02803	_	60	9.99104	+	28.0	9.97004	23	0.00117		9.99944		
10	1	0.02503	9	1	9.99104	15	28.0	9.97158	24	0.00113		9.99940		
19	2	0.02609	18	2	9.98927	30	2	9.97313	25	0.00108		9.9993		
29	3	0.02514	26	3	9.98839	46	3	9.97466	26	0.00104		9.9993		
38	4	0.02418	35	4	9.98751	61	4	9.97620	27	0.00100		9.9992		
48	5	0.02323	44	5	9.98663	76	5	9.97772	28	0.00095		9.9992		
58	6	0.02323	53	6	9.98575	91	6	9.97924	29	0.00091	69	9.99918		
67	7	0.02132	62	7	9.98488	106	7	perior en rein.	30	0.00087		9.9991		
77	8	0.02037	70	8	9.98401	122	8	9.98076 9.98227	31	0.00083		9.99909		
86	9	0.02031	79	9	9.98314	137	9	9.98378	32	0.00078		9.99904		
00			19			131	-		33	0.00074		9,9990		
. 1	30	0.01848		70	9.98227		29.0	9.98528	33	0.00070		9.9989		
9	1	0.01754	9	1	9.98140	15	1	9.98677	35	0.00065		9.9989		
19	2	0 01660	17	2	9.98054	29	2	9.98826	36	0.00061		9.9988		
28	3	0.01566	26	3	9.97967	44	3	9.98975	37	0.00057		9.9988		
38	4	0.01472	34	4	9.97881	59	4	9.99123	38	0.00052		9.9987		
47	5	0.01379	43	5	9.97795	73	5	9.99270	39	0.00048		9.9987		
56	6	0.01285	52	6	9.97709	88	6	9.99417		177 9 10 15 1	7.5			
66	7	0.01192	60	7	9.97623	103	7	9.99563	40	0.00043	7.5	9.99870		
75	8	0.01099	69	8	9.97537	118	8	9.99709	41	0.00039		9.9986		
85	9	0.01006	77	9	9 97452	132	9	9.99855	42	0.00034		9.9986		
7.7	40	0.00914		80	9.97367		30.0	0.00000	43	0.00030		9.9985		
9	1	0 00822	8	1	9.97282	14	1	0.00145	44	0.00026		9.9985		
18	2	0.00730	17	2	9.97197	29	2	0.00289	45	0.00051	100	9.99848		
28	3	0.00638	25	3	9.97112	43	3	0.00132	46	0.00017	86	9.9984		
37	4	0.00546	34	4	9.97027	57	4	0.00575	47	0.00013		9.99840		
46	5	0.00455	42	5	9.96913	71	5	0.00718	48	0.00008		9.9983		
55	6	0.00363	50	6	9 96859	86	6	0.00860	49	0.00004		9.9983		
64	7	0.00272	59	7	9.96775	100	7	0.01002	50	0.00000		9.9982		
74	8	0.00181	67	8	9.96691	114	8	0.01143		P. to tent				
83	9	0.00090	76	9	9 96607	129	9	0.01284		.2 .3 .4				
0.14	50	0.00000		90	9.96524		31.0	0.01424	1-0	1 1 2	5 3	3 3 3		

EXPLANATION.

The true refraction is computed by the following formula, viz. $r = \frac{1}{1+\beta(\tau-50)} \times \frac{p}{30} \times \delta \theta + \frac{d\delta\theta}{d\tau}(\tau-50^{\circ}) - \frac{d\delta\theta}{dp}(30-p)$; in which r denotes the true refraction, $\beta = 0.00375$ $\times \delta \theta + \frac{1}{d\tau} (\tau - 50^{\circ}) - \frac{1}{dp} (30 - p)$; in which r denotes the true refraction, $\beta = 0.00375$ the exponsion of a given volume of air at the surface of the earth for one degree of the centigrade thermometer, p the height of the English barometer, r the temperature in the open air by Fahrenheit's thermometer, $\delta\theta$ the mean refraction for 30 inches and 50°; and $\frac{d\delta\theta}{d\tau}$ and $\frac{d \cdot \theta}{d p}$ are expressions for determining the effects of changes in the temperature and barometric

Table XVII. contains \mathcal{U}_{\uparrow} , the mean refractions, and the expressions for $\frac{d\mathcal{U}}{d\tau}$ and $\frac{d\mathcal{U}}{dp}$. Table XVIII. contains the logarithms of $\frac{1}{1+\beta(\tau-50^{\circ})}$; Table XIX. the logarithms of $\frac{p}{30}$; and Table XX. the logarithms of $-\frac{\tau-50}{10000} \times .434$.

TABLE XXII. TABLE XXI. 00 Augmentation of the Moon's Semi-Reduction of the Moon's Parallax in the diameter in Altitude and Zenith Dist. Spheroid. 55' 56' 57' 58' 59 60 61' Lat. 54' 15 15 30 16 0 16 30 17 0 2 14 30 /3 00 0.0 0 90 0.00 0.00 0.00 0.00 0 00 0.0 0.0 0,0 0.0 0.0 0.0 1 89 0.29 0.0 0.0 0.0 0.24 0.25 0.27 0.31 0.33 0.0 0.0 0.0 0.0 0.0 288 0.48 0.50 0.54 0.58 0.62 0.65 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 387 0.86 3 0.0 0.0 0.71 0.75 0.80 0.92 0.97 0.0 0.0 0.0 0.0 00 0.0 4 86 1.07 1.15 1.23 1.30 0.0 0.0 0.0 0.1 0.1 0.1 0.1 0.95 1.00 0.0 5 85 1.18 1.25 1.34 1.43 1.53 1.62 5 0.1 0.1 0.1 0.1 0.1 0.1 0.1 0.1 6 84 1.71 1.83 0.1 1.41 1.50 1.60 1.94 6 0.1 0.1 0.1 0.1 0.1 0.1 0.1 7 83 1.65 1.75 1.87 2.00 2.13 2.26 7 0.2 0.2 0.2 0.2 0.2 0.2 0.2 0.2 8 82 1.88 0.2 0.2 2.28 2.43 8 0.2 0.2 0.2 2.00 2.14 2.58 0.2 0.2 0.2 981 2.56 2.73 9 0.3 0.3 0.3 0.3 0.8 0.3 2.11 2.25 2.40 2.90 0.3 0.3 1080 2.67 2.85 10 2.35 2.50 3.03 3.22 0.3 0.3 0.3 0.3 0.3 0.3 0.4 0.3 79 3.13 3.33 11 2.58 2.75 2.94 3.54 11 0.4 0.4 0.4 0.4 0.4 0.4 0.4 0.4 3.41 3 63 3.20 3.86 0.5 12 78 2.81 3.00 12 0.4 0.5 0.5 0.5 0.5 0.5 0.5 13 77 3.04 3.25 3.47 3.69 3.93 4.18 13 0.5 0.5 0.6 0.6 0.6 0.6 0.5 0.6 14 76 3.27 3.50 3.73 3.97 4.23 4.49 14 0.6 0.6 0.6 0.6 0.6 0.7 0.7 0.7 4.80 15 75 3.50 3.74 4.25 4.52 0.7 0.7 0.7 0.8 3.99 15 0.7 0.7 0.8 0.8 16 74 3.73 3.98 4.25 4.53 4.81 5.11 16 0.8 0.8 0.8 0.8 0.8 0.9 0.9 0.9 17 73 3.95 4.22 4.51 4.80 5.10 5.42 17 0.9 1.0 1.0 1.0 1.0 0.9 0.9 18 72 4.17 4.46 4.76 5.07 5.39 5.73 18 1.0 1.0 1.0 1.0 1.1 1.1 1.1 1.1 1971 4.40 5.35 5.68 6.04 1.2 1.8 4.70 5.02 19 1.1 1.1 1.1 1.2 1.2 1.2 20 70 4.62 4.94 5.27 5.62 5.97 6.35 20 1.3 1.3 1.3 1.3 1.4 1.2 1.2 1.4 21 69 4.84 5.18 5.52 5.89 6.26 6.65 21 1.3 1.4 1.4 1.4 1.4 1.5 1.5 1.5 22 68 5.06 5.42 5.77 6.16 6.55 6.95 22 1.5 1.5 1.5 1.6 1.6 1.6 1.5 23 67 5 28 5.65 6.02 6.42 6.83 7.25 23 1.6 1.6 1.7 1.7 1.7 1.8 1.6 21 66 5.49 5.88 6.27 6.68 7.11 7.54 24 1.7 1.8 1.8 1.9 1.9 1.9 1.7 1.8 25 65 5.71 6.11 6.52 6.94 7.39 7.84 25 1.9 1.9 1,9 2.0 2.0 2.0 2.1 2.1 26 64 7.66 8.13 2.3 5.92 2.1 2.1 6.34 6.76 7.20 26 2.0 2.0 2.1 2.2 2.3 27 63 6.13 2.2 2.3 6.56 7.00 7.46 7.93 8.42 27 2.1 2.2 2.3 2.3 28 62 6.34 7.72 8.71 2.4 2.5 6.79 7.24 8.20 2.3 2.3 2.5 9.6 28 2.4 2.5 29 61 26 2.7 6.55 7.01 7.48 7.97 8.47 9.00 29 2.4 2.5 2.5 2.6 2.7 2.8 30 60 6.75 7.23 7.71 8,22 8.74 9.28 30 2.6 26 2.7 9.8 20 2.7 2.8 2.9 32 58 8.72 9.26 9.84 3.0 3.0 3.1 3.3 7.15 7.67 8.17 32 2.9 3.1 3.2 3.2 34 56 9.78 10.39 9.20 3.3 3.4 3.7 7.55 8.09 8.63 34 3.3 3.4 3.5 3.6 3.6 9.67 10.28 10.92 36 54 7.93 8.50 9.07 36 3.6 3.7 3.7 3.9 3.9 3.8 4.0 4.1 9.51 10.13 10.78 11.42 38 52 8.31 8.90 38 3.9 4.0 4.1 4.2 4.2 4.3 40 50 9.93 10.58 11.26 11.92 40 4.4 4.5 4.9 8.67 9.30 4.2 4.6 4.6 4.7 4.8 12 48 4.8 9.03 9.68 10.34 11.02 11.72 12.44 42 4.7 4.8 5.0 5.2 5.3 4.9 5.1 44 46 9.38 10.05 10.74 11.44 12.17 12.92 5.2 44 5.0 5.1 5.3 5.4 5.5 5.6 5.7 46 44 9.72 10.41 11.12 11.85 12.61 13.38 48 42 10.05 10.76 11.49 12.25 13.03 13.83 4.6 5.4 5.5 5.6 5.7 5.8 5.9 6.0 6.1 48 5.8 5.9 6.0 6.1 6.2 6.3 6.4 6.5 50 40 10.37 11.10 11.85 12.63 13.43 14.25 52 38 10.67 11.42 12.19 12.99 13.82 14.66 50 6.1 6.3 6.4 6.5 6.6 6.7 6.8 6.9 52 6.5 6.6 6.7 6.9 7.0 7.1 7.2 7.3 54 36 10.95 11.72 12.52 13.34 14.19 15.06 54 6.9 7.0 7.1 7.2 7.4 7.5 7.6 7.7 56 34 11.22 12.01 12.83 13.67 14.55 15.44 56 7.2 7.3 7.5 7.6 7.7 7.9 8.0 58 32 1 1.48 12.29 13. 12 13.99 14.88 15.79 60 30 1 1.72 12.55 13.40 14.29 15.20 16.13 62 28 11.95 12.79 13.66 14.57 15.50 16.45 58 7.5 7.7 7.8 7.9 8.1 8,2 8.4 8.5 60 7.9 8.0 8.2 8.3 8.4 8.6 8.7 8.9 62 8.3 8.6 8.9 8.2 8.5 8.8 9.1 9.9 64 26 12.17 13.02 13.91 14.83 15.78 16.75 9.3 64 8.5 8.6 8.8 8.9 9.1 9.4 9.6 66 24 12.37 13.24 14.14 15.08 16.04 17.03 68 22 12.55 13.44 14.36 15.30 16.28 17.28 9.4 66 8.8 8.9 9.1 9.2 9.6 9.7 9.9 68 90 9.2 9.4 9.5 9.7 9.9 10.0 10.2 70 20 12.72 13.62 14.55 15.51 16.50 17.51 70 9.3 9.4 9.6 9.8 10.0 10.1 10.3 10.5 72 18 12.88 13.79 14.73 15.70 16.70 17.73 74 16 13.02 13.94 14.89 15.87 16.88 17.92 76 14 13.14 14.07 15 03 16.02 17.04 18.09 9.7 9.9 10.0 10.2 10.4 10.6 10.7 9.9 10.1 10.2 10.4 10.6 10.8 11.0 9.7 72 9.5 9.9 10.1 10.3 10.4 10.6 10.8 11.0 11.2 76 10.0 10.2 10.4 10.6 10.8 11.0 11.2 11.4 10.2 10.4 10.6 10.7 10.9 11.1 11.3 11.5 10.3 10.5 10.7 10.9 11.1 11.3 11.4 11.6 78 12 13.24 14 18 15.15 16.15 17.18 18.24 78 80 10 13.33 14.28 15.25 16.26 17.30 18.36 82 8 13.40 14.36 15.34 16.35 17.39 18.47 84 6 13.46 14.42 15.41 16.42 17.47 18.55 80 82 10.4 10.6 10.8 11.0 11.2 11.4 11.5 11.7 84 4 13 50 14 46 15 45 16 47 17 52 18 60 2 13 53 14 49 15 48 16 50 17 55 18 63 10.5 10.6 10.8 11.0 11.2 11.4 11.6 11.8 10.5 10.7 10.9 11.1 11.3 11.5 11.7 11.9 86 88

0/13.54/14.50/15.49/16.51/17.57/18.65

10.5 10.7 10.9 11.1 11.3 11.5 11.7 11.9

TABLE XXIV.

TABLE XXIII.

Logarithms of the Earth's Radii, in each Parallel of Latitude; the Equatorial Radius being Unity, and Compression 120.

Angles of the Vertical with the Radius; or Reduction of the Latitude, in each Parallel, the Compression being 3 to 3.

										-	
		Lat.	Log. R	Lat.	1	Lat.	Reduc.	Lat.	Reduc.	Lat.	Reduc
Lat.	Log. R	Lat.	Log. R	Lat.	Log. R	0	,-,	0	,-,		,-,
00	0.0000000	30°	9.9996402	60°	9.9989151	0	0.0	30	9 55.4	60	9 57.4
Ì	9.9999995	31	96181	61	88932	1	0 24.0	31	10 7.2	61	9 45.
2	9982	32	95957	62	88720	2	0 47.9	32	10 18-1	62	9 32.0
3	9960	33	95728	63	88512	3	1 11.8	33	10 28.3	63	9 18.
4	9930	34	95196	64	88308	4	1 35.5	34	10 37.8	64	9 3.6
5	9890	35	95261	65	88111	5	1 59.2	35	10 46.4	65	8 48.
6	9843	36	95023	66	87918	6	2 22.7	36	10 54.3	66	8 32.
7	9786	37	94781	67	87732	7	2 46.1	37	11 1.4	67	8 16.
8	9721	38	94537	68	87552	8	3 9.2	38	11 7.7	68	7 59.
9	9648	39	94291	69	87378	9	3 32.1	39	11 13.2	69	7 42.
10	9566	40	94044	70	87210	10	3 54.8	40	11 17.9	70	7 23.
11	9.9999477	41	9.9993794	71	9.9987050	11	4 17.2	41	11 21.7	71	7 5.
12	9379	42	93543	72	86896	12	4 39.3	42	11 24.7	72	6 45.
13	9273	43	93291	73	86750	13	5 1.0	43	11 26.9	73	6 26.
14	9158	44	93038	74	86611	14	5 22.4	44	11 28.2	74	6 6.
15	9037	45	92786	75	86479	15	5 43.4	45	11 28.7	75	5 45.
16	8909	46	92533	76	86356	16	6 3.9	46	11 28.4	76	5 24.
17	8771	47	92280	77	86240	17	6 24.1	47	11 27.3	77	5 2.
18	8627	48	92028	78	86131	18	6 43.7	48	11 25.2	78	4 41.
19	8476	49	91776	79	86031	19	7 2.9	49	11 22.3	79	4 18.
20	8318	50	91525	80	85940	20	7 21.6	50	11 18.6	80	3 56.
51	9.9998153	51	9.9991277	81	9.9985857	21	7 39.7	51	11 14.1	81	3 33.
22	7983	58	91030	82	85782	22	7 57.3	52	11 88	82	3 10.
23	7805	53	90785	83	85716	23	8 14.2	53	11 2.6	83	2 47.
24	7621	54	90542	84	85659	24	8 30.7	54	10 55.7	84	2 23.
25	7431	55	90302	85	85610	25	8 46.4	55	10 47.9	85	2 0.
26	7236	56	90065	86	85570	26	9 1.6	56	10 39.4	86	1 36.
27	7035	57	89831	87	85539	27	9 16.1	57	10 30.0	87	1 12.
28	6829	58	89600	88	85517	28	9 29.9	58	10 19.9	88	0 48.
59	6618	59	89374	89	85504	29	9 43.0	59	10 9.0	89	0 24.
30	6402	60	89151	90	85199	30	9 55 4	60	9 57.4	90	0 0.

TABLE XXV.

For determining the Latitude, at any time, by the Pole Star.

0	M	N	0	M	N	10	M	N	0	M	N	0	M	N	0	M	N
h.m.	"	"	h.m.	"	"	h.m.	"	"	h.m.	"	"	h.m.	"	"	h.m.	"	"
0 0	0.00	0.00	1 0	5.85	0.11	2 0	21.82	0.37	3 0	43.63	0.60	4 0	65.45	0.63	5 0	81.42	0.41
10	0.17	0.00	10	7.89	0.14	10	25.19	0.41	10	47.44	0.62	10	68.66	0.61	10	83.18	0.35
20	0.66	0.01	20	10.20	0.19	20	28.71	0.46	20	51.21	0.64	20	71.68	0.59	20	84.64	0.28
30	1.49	0 03	30	12.78	0.23	30	32.34	0.50	30	54.93	0.65	30	74.49	0.55	30	85.78	0.22
40	2.63	0.05	40	15.59	0.27	40	36.06	0.53	40	58.56	0.65	40	77.06	0.51	40	86.60	0.15
50	4.09	0.08	50	18.61	0.32	50	39.83	0.57	50	62.07	0.64	50	79.38	0.46	50	87.10	0.07
1 0	5.85	0.11	5 0	21.82	0.37	3 0	43.63	0.60	4 0	65 45	0.63	5 0	81.42	041	6 0	87.26	0.00

 $\psi=Z+p\cos t-M$ cotan. Z+N; where ψ is = the Latitude; Z= the Zenith Distance; $p=1^{\circ}40'$, or 100'; t= the Horary Angle; t= in the first Quadrant; $=12^{\circ}-t$ in the second; $=t-12^{\circ}$ in the third; and $=24^{\circ}-t$ in the fourth; M and N being the Tabular Quantities. The quantity M is $=\frac{1}{2}p^2\sin 2t$, and is always positive; but the quantity $N=\frac{1}{2}p^3\sin 2t$, becomes negative in the second and third Quadrants of t. When p (the Polar Distance) augments or diminishes 1', the Tabular Quantity must also be augmented or diminished by 0.02M; and for any other quantity of variation in the same proportion.

TABLE XXVI.

To find the Augmentation of the Moon's Semidiameter by the Altitude of the Nonagesimal, and the Apparent Distance of the Moon therefrom.

No. of Lot	-10	ART I			PART	. 1 PART III.								
Alt. no		pp. dis. N		nona,	Aggre-	111-	True	l n						
Alt. no	na. — a	pp. dis. I	Moon fr.	nona	gate of	Cor.	Lat. of	1000	-	200			in L	
-		I. VII.		-	No.from		the	0'	10'	\$0,	30'	40'	50'	60'
1	+ -	-	+ -	000	Part I.	+	Moon			_		_	_	=
1	0".00	4".10	7".10	300	1"	0".00	S. Lat.	"	"	"	11	"	"	"
2	0.29	4.31	7.23	28	3	0.01	60 0'	0.00	0.29	0.59	0.90	1.22	1.51	1.88
3	0.43	4.46	7.30	27	4	0.02	5 40	0.00	0.97	0.56	0.85	1.16	1.46	1.78
4	0.57	4.58	7.36	26	5	0.03	5 20						1.38	
5	0.72	4.70	7 42	25	6	0.04	5 0	0.00	0.24	0.49	0.76	1.02	1.30	1.59
6	0.86	4.93	7.48	24 23	7 8	0.05	4 40	0.00	0.23	0.46	0.71	0.96	1.22	1.49
8	1.14	5.04	7.59	22	8.5	0.07							1.14	
9	1.28	5.16	7.65	21	9.0	0.08	4 0	0.00	0.19	0.40	0.61	0.83	1.06	1.30
10	1.42	5.27	7.70	20	9.5	0.09							0.98	
11	1.56	5.38	7.74	19	10.0	010	AND RESIDENCE						0.90	
12	1.70	5.49	7.79	18	10 5	0.11	3 0	0.00	0.14	0.30	0 47	0.64	0.82	1.01
13	1.84	5.59	7.83	17	11.0	0.12	2 40						0.74	
15	2.12	5 80	7.92	15	12.0	0.14	2 20						0.66	
16	2.25	5.89	7.95	14	12.3	0.15	2 0	0.00	0.10	0.21	0.33	0.45	0.58	0.72
17	2.39	5.99	7.98	13	12.7	016	1 40						0.50	
18	2.53	6.09	8.02	12	13.0	0.17	1 20						0.42	
19	2.67	6.18	8.04	11 10	13.3	0.18		-	-	-				-
20	2.94	6.27	8.06	9	13.7	0.19	0 50						0.30	
22	3.07	6.45	8.11	8	14.3	0.21	0 40						0.26	
23	3 20	6.51	8 13	7	14.7	0 55	100000	100						
24	3.33	6.63	8.15	6	15.0	0.23	0 20						0.18	
25	3.46	6.71	8.16	5 4	15.3	0.24							0.10	
27	3.72	6.79	8.18	3	16.0	0.26	2 3 1	-	-					
28	3.85	6 95	8.19	2	16.3	0.27	N. Lat.	1	200	13	23	200	50	100
29	3.97	7.02	8.19	1	16.7	0.28	0 10	0.00	0.01	+	0.01	0.03	0.06	0.10
30	4.10	7.10	8.19	0	17.0	0.29	0 20	0.00	0.09	0.09	0.01	+	0.02	0.05
	XI. V		1x. III		Description of		0 20	0.00	0.00	0.02			+	0.00
	Jana V		RT I		1 2 2 4		0 30	0.00	0.09	0.03	0.01	0.03	0.05	+
P					e Moon.	To Kind	0 40						0.06	
Sum of preced.				15'	- diodi	116	0 50	0.00	0.04	0.07	0 09	0.10	0.10	0.10
Equa-	Married Street,	still plus	1 10"1 :	100000000000000000000000000000000000000	0" 40" .	50" 0"	1 0	0.00	0.05	0.08	0.11	0.13	0.14	0.15
tion.	-		-				1 20						0.22	
11	"	" "		" "		" "	1 40	0.00	0 08	0.14	0 20	0.21	0.30	0.34
1					06 0.04 0		2 0						0.38	
2					12 0.08 0 19 0.12 0		2 20						0.46	
4					25,0.170		2 40		200	-	-		0.54	THE REAL PROPERTY.
5					31 0.21 0		3 0						0.62	
6	1.00	0.88 0.75	0.620	.50 0.3	37 0.25 0	.12 0	3 20						0.70	
7	1.16	.02 0 87	0.73 0	58 0.	44 0.29 0	.15 0	Recipied and the least of the l				-		THE REAL PROPERTY.	
8	1.33 1	16 1.00	0 83 0	67 0.	50 0.33 0	.16 0	4 20						0.86	
10	1.67	46 1.9	1.040	830.	56 0.37 0 62 0.42 0	21 0	4 40	0.00	0.23	0.43	0.61	0.83	1.02	1.20
11					69 0.46 0		1 200	-					1.10	
12					75 0.50 0		5 0 5 20						1.18	
13	2.16	.89 1.69	1.35 1	.08 0.1	81 0.540	.27 0	5 40						1.25	
14					87 0.58 0		6 0	0.00	0.90	0.56	0.00	1.00	1.34	1 80
15					94 0.62 0		6 0	0.00	4/5/6	2000	No.	1		MARKET .
1000		+ + +	50"		0" 20"	+	7	0'	10	911	+	+	50'	60
	_	10 0	301	13	16'	10 10					LEGISTRE	ARCHIO SERVICE	in La	_
					10:	-	_	1 .	er all	N OI	one N	rodu	1.0	-

93	_		e Ho	-	- "	-		_	7-2-	nd D	_								me		
9'	T	8'	7'		6'		5'	1	4	3′	Ī	2'	1'	30'	7 3	20	10'		ioon	er N	
"	7	"	"	1	"	′	"	-1-	' '	"	" '		, "	"	" '	a c	, "	m.		m.	
0.0	30		2.9	1	2.5	0	2.1	60		0.0	.80		0.0	12.3	0.00		5 75	50	11	-	0
7.3	50		5.7		4.9	0	100	20		2.4	.60			24.3			7			20	
108	-		8.4		7.2	-	6.0	80		3.6	.40			100			0 12.0			30	= -
		12.6	C 700 70 10	0	9.4	0	7.9	30	0 6	4.7	.10	0 3	0 1 6	47.2	150	0 3	0 15.	20	11	40)
17.4	50	15 5	13.5	0	11.6	0	9.7	80	7	5.8	.90	0 3	0 1.9	58 2	8.8 0	0 3	19.4	100	11	50	0
		18.3			13.8		11.5			6.9	.60	0 4	0 2.3	87	5.8 1	00 4	92.	0	11	0	ī
		21.1									30					30 5	26.	50	10	10	1
		23.7									.90		2 . m. m.	28 9	20 had get	2 200	0 29.	-		20	
		26.3									60			38.4		200	0 32.	-		2.5	
		28.7											$03.6 \\ 03.9$		1.8 1		0 35.9 0 38.9			50	2
	_			-	_	-		-	_	_	-	-	0 4.2	_	3.3 2	-	0 41.	_	10	-	_
		33.5										To 15:	01/38/5	13.2	0.15 (3)		0 44		9	10	5
		37.6												21.0	004 22	45.00	0 47.	100	9	201	
		39.6															0 49.		9	30	
46.7	50	41.5	36.3	0	31.1	0	25.9	70	20	15.6	.40	0 10	0 5.2	35.5	3.7 2	914		50	9	40	5
48.7	30	43.9	37.9	0	32.5	0	27.1	60	21	16.2	80	0 10	0 5.4	42.3	8.22	1 1 4	0 54.	10	9	50	2
50.6		45.0												48.7			0 56.	0	9	0	3
		46.6															0 58.	150.00	8	10	
		48.1													0.43	212			8	20	_
		49.6													4.03			30	1.00	30	
		50.9																22	8	40	3
58.7	-	52.2	-	-	_	-	_	_	-	-	_	-	_	15.6	-	_	_	-	_	50	3
0.0			46.7											20.0	2012			0	8	0	4
4.9		55.4												27.6				10	7	40	•
5.6	12.	58.9	2 6 7 23 2				-			1200	200		4 1 1 1 1 1 1 1 1	0.000		100		0	7	0	5
6.7		59.9																40	6	20	_
7.9		59.8																50	6	40	
7.8	01	0.0	52.5	00	45.0	0	37.5	00	30	22.5	.00	0 15	0 7.5	45 0	0.03	02 3	1 15.	0	6	0	6
_	ation	Equa		_	-	-		_	_		_	Secon	-	-		_			me	T	-
ime		24 h.	9"	8"	7"	1 7	6"	5"	4"	3"	2"	1"	50"	40"	30"	20"	10"		look		
_	n.h.		"	"	_	-	"	"	"	"	"	"		"	"	"	"	m.	h.	mi	h.
	0 2		00	0.0	0.0	0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0	12	0	ø
3 40	20 2	0 20	0.1	0.1		0	0.0	0.0	0.0	0.0	0.0	0.0	0.3	0.3	0.2	01	0.1	50	11	10	0
3 20	10 5	0 40	0.1	0.1	.1 (0	0.1	0.1	0.0	0.0	0.0	0.0	0.7	0.5	0.4	0.3	0.1	40	11	50	0
	0 2		0.2	0.2	- E3 10-1	100	0.1	0.1	0.1	0.1	0.0	0.0	1.0	0.8	0.6	0.4	0.2	30	200	30	0
	50 5		0.2	0.2	0.7	100	0.2	0.1	0.1	0.1	0.1	0.0	1.3	1.0	0.8	0.5	0.3	20	11	40	0
_	10 5		0.3	0.3	-	-	0.9	0.2	0.1	0.1	0.1	0.0	1.6	1.3	1.0	0.6	03	10	11	50	0
	02		0.3	0.3		1 5	02	0.2	0.1	0.1	0.1	0.0	1.9	1.5	1.1	0.8	0.4	0	11	0	1
	505		0.4	0.4			0.3	0.2	0.2	0.1	0.1	00	2.2	1.8	1.3	0.9	0.4	50	10	10	!
	10 5		0.4	0.4			0.3	0.2	0.2	0.1	0.1	0.0	2.5	2.0	1.5	1.0	0.5	40	10		1
0 40			0.5	0.4			0.3	0.3	0.2	0.2	0.1	0.0	3.0	2.4	1.6	1.2	0.6	30	10	40	i
20	77.00	12 17	0.6	0.5			0.4	0.3	0.3	0.2	0.1	0.1	3.2	2.6	1.9	1.3	0.6	10	10	50	i
-	02		0.6	0.6	-	-	0.4	0.3	0.3	0.2	0.1	0,1	3.5	2.8	2.1	1.4	0.7	0	10	0	· ·
9 40			0.7	0.6		1	100.7	0.4	0.3	0.2	0.1	0.1	3.7	3.0	2.2	1.5	0.7	50	100	10	2
				0.6			0.5	0.4		0.2	0.2	0.1	3.9	3.1	2.3	1.6		40		20	
9 20	01	5 (0.7	0.7	0.6	0	0.5	0.4	0.3	0.2	0.2	0.1	4.1	3.3	2.5	1.6	0.8	30	9	30	2
3 40	20 1	5 20	0.8	0.7				0.4		0.3	0.2	0.1	4.3	3.5	2.6	1.7		20		40	S
3 20			0.8	0.7		-	-	0.4	_	0.3	0.2	0.1	4.5	3.6	2.7	1.8		10	_	50	
	0 1		0.8	0.7			0.6	0.5	0.4		0.2	0.1	4.7	3.8	2.8	1.9	0.9	0	9	0	3
		6 20	0.9	0.8			0.6	0.5	0.4	0.3	0.2	0.1	4.9	3.9	2.9	1.9		50		10	3
		6 40	0.9	0.8			0.6	0.5			0.2	0.1	5.0	4.0	3,0	2.0		40		20	
40	01		1.0	0.8			0.6	0.5	0.4		0.2	0.1	5.2	4.1	3.1	2.1		30		30 40	3
20			1.0	0.9			0.6	0.5	0.4	0.3	0.2	0.1	5.4	4.3	3.3	2.2		10		50	
	01	_	1.0	-	_			_				-		-	_		_	-	_	0	4
20			1.0	0.9			0.7	0.6	0.4	0.3	0.2	0.1	5.6	4.4	3.3	2.2	1.1	40	8	20	4
		9 20			0.8	0	0.7	0.6	0.5		0.2	0.1	5.8 5.9	4.8	3.6	2.4		20		40	4
4.0	10	10 6	1.1	1.0	.9 1	0	0.7	0.6	0.5	0.4	0.2	0.1	6.1	4.9	3.7	2.4	1.2		7	0	5
13 9	as	1.10	117	0.1	10.0	16	10.7	0.6	0.5	0.4	0.2	0.1	6.2	4.9	3.7	2.5	1.2			20	
alis	15	111	0/1.	11	10.9	11	9/0:	10.	0.5	0.4	0.2	0.1	6.2	5.0	3.7	2.5	1.2	20		40	
0/1	19	111	10.1	77	100	2	0/0	174	100	104	100		6.2	5.0	3.7	2.5	1.2	of	6	0	-

TABLE XXVIII.

Reduction to the Meridian. Part I.

1			-0-		1				TTO				-
5	Om	Im	2m	3m	4m	5m	-Gm	7m	8m	9m	10m	11m	12m
	1 "	"	"	"	"	"	"	"	101.01	1 ***	100.00	222	000
0	0.00	1.96			31.41							237.54	
1 2	0.00	2.03			31.68							238.26 238.98	
3	0.00	2.16			32 21							239.70	
4	0.01	2.23			32 47							240.42	
5	0.01	2.30			32.74							241.15	
6	0.02	2.38	8.66	18.87	33.01	51.07	73.06					241.87	
7	0.03	2.45	8.80	19.07	33.27	5,1.40	73.46	99.44	129.34	163.17	200.93	242.60	288.20
8	0.03	2.52			33.54			The second second			CONTRACTOR AND ADDRESS OF	243.33	Section 2015
9	0.04	2.60	Street, or other party of		STATE OF THE PERSON NAMED IN		MARKET PROPERTY.	Commence of the last			THE RESERVE OF THE PERSON.	244.06	THE REAL PROPERTY.
10	0.05	2.67										244.79	
11	0.07	2.75										245.52	
12	0.08	2.83										246.26	
13	0.09	2.91										246.99	
14	0.11	2.99										247.72 248.46	
16	0.12	3.15										249.19	
17	0.16	3.23										219.93	
18	0.18	3.32										250.67	
19	0.20	3.40										251.41	
20	0.22	3.49										252.15	
21	0.24	3.58										252.89	
22	0.26	3.67										253.63	
23	0.29	3.76										254.38	
24	0.31	3.85										255.12	
25	0.34	3.94										255.87	
26	0.37											256.62	
27	0.40	100000000000000000000000000000000000000										257.37	
28	0.43	4.32										258.12 258.87	
2000			-	-	-	The State of the S	-	Section 2			Maria Control	SCHOOL SECTION	THE RESERVE AND ADDRESS OF
30	0.49	4.42										259.62 260.37	
32	0.56	4 62										261.12	
33	0.59											261.88	
34	0.63	4.82										262.64	
35	0.67	4.92										263.39	
36	0.71	5.03	13.27	25.45	41.55	61.57	85.52	113.40	145.20	180.93	220.58	264.15	311.65
37	0.75											264.91	
38	0.79	5.24										265.67	
39	0.83	5.35				-				-		266.43	SERVICE AND ADDRESS.
40	0.87	5.45										267.20	
41	0.92	5.56										267.96	
42	0.96	5.79										268.72 269.49	
44	1.06	5.90										270.26	
45	1.10	6.01										271.03	
46	1.15											271.79	
47	1.20	6.24	15.21	28.10	44.92	65.67	90.34	118.94	151.46	187.91	228.27	272.57	320.78
48	1.26	6.36										273 34	
4.9	1.31	-		100000000000000000000000000000000000000		200	-			Access to the last of the last	Contract of the Parket	274.11	PROPERTY AND ADDRESS OF
50	1.36											274.88	
51	1.42											275.66	
52	1.48	6.84	16.14	29.36	46.50	67.58	92.57	121.50	154.35	191.12	231.81	276.43	324.97
53	1.53											277.21	
54 55	1.59											277.99 278.77	
56	1.71											279.55	
57	1.77											280.33	
58	1.83											281.11	
59	1.90											281.89	
.2	10.01		0.03						0.11	0.12	0.14	0.15	0.16
.4	0.01	0.04	2000	1000000	0.12	0.14		0.20	0.22	0.25	0.28	0.30	0.33
.6	0.02	0.06	0.10		0.18	0.21	0.26		0.34	0.37	14.0	0.45	0.49
8	0.02	0.08	0.13	0.18	0.24	0.28	0.34	0.40	0.45	0.50	0.55	0.60	0.66
S 81	STATE OF		100	1				STORY.	SINIO.	2112	LILBI	TIP	1

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T. XXVIII TABLE XXIX.—Reduction to either Solstice. 95 PART II. Obliquity of the Ecliptic 23° 27' 40". Diff. Variation in 100" change of obliquity. Diff. change of obliquity. in 100 Reduc. Reduc. Reduc. Arg. Arg. hange of 7, 11 m. + 0 1 11.71 2.41 0.0651 00 0 0 0000.020.0000 10 50 46.83 4.80 0.2606 " 100 0.02 0.06 0.0000 101 14.12 2.45 0.0673 51.63 4.84 0.2650 10 0.08 0.10 0.0001 0.18 0.14 0.0002 0 0 200 20 16.57 2.49 0 0695 20 56 47 4.88 0.2694 1.35 4.92 0.2738 0.00 0 30 300 30 1 19.06 2.53 0.0717 30 0.00 0.00 400 0.320.180.0003 40 1 21.59 2.57 0.0740 40 6.27 4.96 0.2783 30 0.00 50 0 0.50 0.22 0.0005 50 1 24.16 2.61 0.0763 50 5 11.23 5.00 0.2828 0 26.77 2.65 0.0787 16.23 5.04 0.2873 0.00 0.0 0.72 0.26 0.0007 2 30 0.00 100 0.98 0.29 0.0009 10 1 29.42 2 69 0.0811 10 5 21.27 5.07 0.2919 26.34 5 12 0.2965 0 0.00 200 1.27 0.34 0.0011 20 1 32.11 2.72 0.0836 20 5 8 30 0.00 300 1.61 0.38 0.0014 30 1 34.83 2.77 0.0860 30

40.0 40 1 37.60 2.81 0.0886 0 0.00 40 30

1.99 0.42 0 0018 500

50 1 40.41 2.85 0.0911 50 5 41.82 5.21 0 3106

5 31.46 5.16 0 3012 5 36.69 5.20 0.3059 01 43.26 2.89 0.0937 0 5 47.06 5.28 0.3154

101 46.15 2.93 0.0963 10 5 52.34 5.32 0.3202 20 1 49.08 2.96 0.0990 90 57.66 5.35 0.3250 30 1 52.04 3.01 0.1617 30

40

40 1 55 05 3.05 0.1044

6 3.01 5.40 0.3299 6 8.41 5.44 0.3349 6 13.85 5.48 0.3398 50 1 58 10 3.09 0.1072 50 n

2.41 0.46 0.0022 2.87 0.50 0.0026 12 3.37 0.54 0.0031 3.91 0.57 0 0036 4.48 0.62 0.0041 5.10 0.66 0 0046 19.33 5.51 0.3448 03 1.19 3.12 0.1100

1012 4.31 3.17 0.1125 24 84 5.56 0 3498 10

202 7.48 3.21 0.1157 20 30.40 5.60 0.3549

30 2 10.69 3.25 0.1186 30

40 2 13.94 3.28 0.1216 40

50 2 17.22 3.33 0.1246 50

6 36.00 5.64 0 3600 6 41.64 5.67 0.3651 6 47.31 5.72 0.3703

400 500 5.76 0.69 0.0053 6.45 0.74 0.0059 13 00 100 7.19 0.78 0.0066 200 7.97 0.81 0 0073 30.0 8.78 0.86 0.0080 9.64 0.89 0.0088 400 50 0 10.53 0.94 0.0096 53.03 5.75 0.3755 0.0 11.47 0.97 0.0104 14 0 2 20.55 3.36 0.1276 0 10 2 23.91 3.41 0.1307 100 12.44 1.02 0.0113 10 58.78 5.80 0.3807 200 13.46 1.06 0.0122 20 2 27.32 3.45 0.1338 4.58 5.84 0.3860 20

20 0.01 30 0.02 40 0.02 50 0.02 0 0.02 10 0.02 20 0.03 30 30 0 14.52 1.09 0.0132 0.03 30 2 30.77 3.48 0.1369 30 10.42 5.87 0.3913 16.29 5.92 0.3967 22.21 5.95 0.4021 40 0.03 40 0 15.61 1.14 0.0142 40 2 34.25 3.53 0.1401 40 50 50 2 37.78 3.56 0.1433 0.04 50 0 16.75 1.18 0.0152 50 7 0 0 04 17.93 1.21 0.0163 0 2 41.34 3.61 0.1465 0 7

28.16 6.00 0.4075 34.16 6.03 0.4130 100 19.14 1.26 0.0174 10 102 44.95 3.64 0.1498 10 0.04 7 20 0.05 200 20.40 1.29 0.0185 20 2 48.59 3.69 0.1531 20 40.19 6.08 0.4185 30 0.05 30

30 2 52.28 3.72 0.1564 300 21.69 1.34 0.0197 46.27 6.11 0.4240 400 23.03 1.37 0 0209 500 24.40 1.42 0.0221 40 2 56.00 3.77 0.1598 50 2 59.77 3.80 0.1632 52.38 6.15 0.4296 40 0.05 40 7 50 0.06 50 58.53 6.20 0.4352 0.06 0 0 4 73 6.23 0.4408

0 0 25.82 1.45 0.0234 10 0 27.27 1.49 0.0247 3.57 3.85 0.1667 7.42 3.88 0.1702 10 0.07 103 10 10.96 6.28 0.4465 20 0 28.76 1.54 0.0261 20 3 11.30 3.92 0.1737 17.24 6.31 0.4522 20 0.07 20 30 0.08 30 0 30.30 1.57 0.0274 30 3 15.22 3.97 0.1773 30 23 55 6.35 0.4579

40 3 19.19 4.00 0.1809 40 0.08 40 0 31.37 1.62 0 0289 40 29.90 6.40 0.4637 50 0.09 50 0 33.49 1.65 0.0303 50 3 23.19 4.05 0.1845 50 36.30 6.43 0.4695 () 0.09 00 35.14 1.69 0.0318 0 3 27.24 4.08 0.1882 0 8 42.73 6.47 0.4754 10 0.10 100 36.83 1.73 0.0333 103 31.32 4.12 0.1919 10

20 3 35.44 4.16 0.1957 20 0.11 20 0 38.56 1.78 0.0349 20 30 30 011 300 40.34 1.81 0.0366 30 3 39.60 4.21 0.1994 40 0.12 40 0 42.15 1.85 0.0381 40 3 43.81 4.24 0.2033 40 50 0.13 500 44.00 1.89 0.0399 50 3 48 05 4.28 0.2071 50 9 0 0.14 0 3 52.33 4.33 0.2110 0 00 45.89 1.94 0.0416 18 28

49.20 6.52 0.4813 55.72 6.55 0.4873 2.27 6.59 0.4932 8.86 6.63 0.4993 15.49 6.68 0.5053 22.17 6.71 0.5114 10 0.15 100 47.83 1.97 0.0434 103 56.66 4.36 0.2149 10 28.88 6.75 0.5175 20 35.63 6.79 0.5237 42.42 6.83 0.5299 0.15 200 49.80 2.01 0.0452 204 1.02 4.40 0.2189 20 30 5.42 4.44 0.2229 0.16 30 0 51.81 2.05 0.0470 304 30 40 0.17 40 0 53.86 2.09 0.0489 404 9.86 4.48 0.2269 49.25 6.87 0.5361 40 50 4 14.34 4.53 0.2310 50 0.18 500 55.95 2.13 0.0508 56.12 6.91 0.5424 50 9 D 12 0.19 9 00 58.08 2.18 0.0527 3.03 6.95 0.5487 0 10 10 0.21 101 10 10 20 0.22 201

0 4 18.87 4.56 0.2351 29 10 4 23.43 4.60 0.2393 9.98 6.99 0.5550 0.26 2.21 0.0547 20 4 28.03 4.64 0.2435 30 4 32.67 4.68 0.2477 2.47 2.25 0.0567 20 10 16.97 7.04 0.5614 4.72 2.29 0.0587 30 10 24.01 7.07 0.5678 40 4 37.35 4.72 0.2520 7.01 2.33 0.0608 40 10 31.08 7.11 0.5743 9.34 2.37 0.0629 50 4 42.07 4.76 0.2563 50 10 38.19 7.15 0.5808 11.71 0.0651 20 04 46.83 0.8606 0/10 45.34

TABLE XXXI. TABLE XXX. To change mean Solar into Sidereal Time. To change Sidereal into mean Solar Time. Sider. Subtract Seconds. Solar Min. Add Seconds. Subtract 0.164 3 55.908 0.164 56.556 0.003 1 1 0.003 1 1 0 3 51.816 0.328 53.112 2 2 2 0.005 9 7 2 0.329 2 0.006 3 11 47.724 3 0.491 3 0.008 3 0 11 49.668 3 0.493 3 0.008 4 15 43.632 0.655 4 0.011 15 46.224 4 0.011 0.658 5 0 819 19 39.540 5 5 5 0 19 42.780 5 0 822 5 0.014 0.014 0.983 6 23 35.448 6 6 0.016 6 23 39.336 6 0.986 6 0.017 1.147 27 35.892 31.356 1.150 7 0.019 7 27 0.019 1.311 31 27.264 8 8 0.022 8 8 31 32 448 8 1.315 0.022 1.474 9 Q 25 23.172 9 9 0.025 0 35 29.001 0 1.479 0.025 10 39 19.080 10 1.636 10 0.027 0 39 25 560 10 1.643 10 0.027 14,988 1.802 0 43 0 030 43 22.116 11 1.807 11 0.030 12 47 10.896 1.966 12 19 0.039 12 0 47 18.672 12 1.972 19 0.033 13 0 51 6.804 13 2.130 13 0.035 13 0 51 15.228 13 2.136 13 0.036 14 0 55 2.712 2.294 14 14 14 0 55 11.784 14 2.300 14 0.038 0.038 0 59 8.340 15 15 0 58 58.620 15 2.457 15 0.011 15 15 2.464 0 041 16 2 54.528 2.621 16 16 16 3 4.896 16 2.629 16 0.044 0.014 17 50.436 2.785 1.452 17 17 17 0.046 17 17 0.047 2.893 46.344 18 10 2 949 10 58 008 18 18 0.049 18 18 3.057 18 0.050 19 42.252 19 3.113 19 0.052 19 14 54.564 19 19 3,221 0.053 18 51.120 20 90 18 38,160 20 3.277 50 0.055 20 20 3 286 0.055 21 34.068 3.450 18 0.058 22 21 3.440 21 21 92 47.676 21 22 26 29.976 3.604 22 0.050 23 26 44 232 22 3.614 92 0.061 22 23 30 25.884 3.768 23 23 0.063 23 30 40.788 23 3.779 23 0.064 24 34 21.792 21 3 932 24 24 3.943 24 24 0.066 34 37 341 0.066 38 25 17.700 25 4.096 25 25 38 33.900 25 4 108 25 0.069 0.058 26 42 13.608 26 1 259 26 42 30.456 26 4.272 26 0.072 26 0 071 27 46 9.516 27 46 27.012 27 4.436 27 0.075 27 4.423 27 0.074 28 50 5.424 28 50 23.568 28 4.587 98 28 0.076 28 4.600 0 077 29 54 29 54 20.124 4.764 29 1.332 29 4.751 90 0.080 29 0.079 30 57 57 240 30 30 58 16.680 30 4.928 30 0.082 4 915 30 0.032 31 53.148 13 236 п 31 2 31 5.092 31 0.085 31 5 079 31 0.085 32 2 9.792 49.056 32 6 32 5.257 29 0.088 32 5.242 32 0.087 33 2 33 2 10 6.348 33 Q 44 964 5.406 33 5.421 0.091 33 33 0.090 34 34 2 9.004 13 40.872 14 34 5.585 34 0.094 34 5.570 34 0.093 35 17 59.460 35 5.750 35 0 097 35 17 36.780 35 5.734 35 0.096 5.898 36 5.914 36 0.100 26 36 0.098 id. Hrs. Sol. Hrs. 9.829 9,8565 6.078 0.103 0 37 6.062 27 37 37 0.101 A 19.713 6.242 2 0 19.659 38 6.225 38 38 0 106 38 0.104 3 29.488 39 0 39 39 3 0 29,569 6.407 39 0.108 6.389 0.106 39.426 4. 0 39.318 40 4 0 40 6.571 40 0.111 6.553 40 0.109 41 6.735 41 5 49,147 5 0 49.282 0.114 0 41 6.717 41 0.112 6 6 59.139 42 6.900 42 0.116 58.977 42 6.881 42 0.115 7.064 43 8.995 0.119 7 8.806 43 7.044 43 43 0.117 7.228 18.852 44 44 0.122 8 18,636 44 7.208 0.130 9 28.708 45 7.393 45 0.125 0 1 28.465 45 7.372 45 0.123 7.557 10 38.565 46 46 0 128 10 1 38.295 46 7.536 46 0.126 11 48.421 47 7.722 47 0.131 11 48.124 4.7 7.699 47 0.128 57.954 0.133 12 12 1 58.278 7.886 48 48 48 7.864 48 0.131 13 8.134 49 8.050 49 0.136 13 7.783 49 8.027 49 0.134 2 17.991 14 8.214 0 138 14 17.613 50 8.191 50 50 50 0.137 8.355 15 27.847 51 8.378 51 0.141 15 2 27.442 51 51 0.139 2 37.704 2 37.272 16 52 8.543 52 0.144 16 52 8.519 52 0.142 2 47.560 17 53 8.707 53 0.147 17 47.101 53 8.683 53 0.145 18 2 57.417 54 8.872 54 0.150 18 2 56.931 54 8.616 54 0 147 19 55 9.036 0 152 19 3 6.760 55 3 7.273 55 9.010 55 0.150 17.130 56 9.200 20 3 56 0.155 20 8 16.590 56 9.174 56 0.153 57 9.364 0.157 26.419 0.156 21 3 26,987 57 21 3 57 9 338 57 22 36.844 58 9.528 58 0.159 3 36.249 58 9.502 3 22 58 0.158 3 46,700 59 9.692 59 23 0.162 59 9.666 23 3 46.078 59 24 3 56.556 9.856 60 60 0.164 24 3 55.908 60 9.829 60 0.164

> This Table may be used to shew the Sun's Right Ascension also, in Sidereal Time.

EXPLANATION OF THE TABLES.

TABLE I.—The Miles and Parts of a Mile in a Degree of Longitude at every Degree of Latitude, supposing the Earth to be a Sphere.

The first column of this table contains degrees of latitude, the second the miles and hundredth parts of a mile in a corresponding degree of longitude,—of these the remaining columns are a continuation. If the given latitude consists of degrees and minutes, a proportional part of the difference between two contiguous degrees, the one greater and the other less than the given latitude must be applied to the miles, &c. corresponding to either of the adjacent degrees, by addition or subtraction, according as it is greater or less than the given latitude.

Example 1.—Required the number of miles in a degree of longitude

at the Isle of May, in latitude 56° 11' 22" N.

Miles in a degree of longitude in latitude 56°=33.55 in latitude 57 =32.68

Then 60': 11' 22":: 87: 165, which, subtracted from 33.55, gives 33.385; the measure of a degree of longitude in latitude 56° 11' 22".

Ex. 2.—Suppose the error of a chronometer to be half a minute, after a voyage from Leith to the West-Indies and back, how many geographical miles would that amount to at the mouth of the frith of Forth, near the Isle of May?

Since 1° of longitude is equal to four minutes of time, then half a minute will be the eighth part of a degree, and \(\frac{1}{2}\) of 33.385=4.178,

or about 41 miles.

Ex. 3.—What is the distance in geographical or nautical miles between Stockholm in longitude about 18° E., and Petersburgh in longitude 30° E., the common latitude being 60° N. nearly?

 30° — 18° = 12° , and 12×30 =360 miles nearly, since at 60 one

degree is 30 miles.

TABLE II.—Logarithms of Numbers.—Part I. contains the logarithms of all numbers from 1 to 100, inclusive, with their proper indices prefixed. Part II. contains the decimal part of the logarithms of all numbers from 100 to 10,000, without their indices. The indices are easily supplied by the computist, being always one unit less than the number of integers in the given natural number. The index of the logarithm of a number in which there are any integers is always positive; but, if the number be properly a fraction, the index is negative, usually marked by the sign—either

before, or more generally above the index. If the first effective figure of the decimal fraction be adjacent to the decimal point, the index is $\overline{1}$; if there be one cipher between them, the index is $\overline{2}$; if two ciphers, the index is $\overline{3}$; and, in general, the number denoting the place of the first significant figure from the decimal point will be the negative index. Instead of negative indices, their arithmetical complements are frequently used, especially by those unacquainted with the first principles of Algebra.

The decimal parts of the logarithms of numbers consisting of the same figures are the same whether the number be integral, frac-

tional, or mixed, which may be illustrated as follows:

Numbers 546800 Logarithms 5.737829

546800		Logarithm	ns 5.737829
54680	100	- Brand	4.737829
5468	100	12,-	3.737829
546.8		- INC.	2.737829
54.68	11 12	15000	1.737829
5.468	7.4		0.737829
0.5468		01	1.737829, or 9.737829
0.05468	1 100	-	2.737829, or 8.737829
0.005468		all all o	3.737829, or 7.737829
0.000546	8	all .	4.737829, or 6.737829

PROBLEM I.—To find the Logarithm of any given Number. RULE.—If the given number be under 100, its logarithm is found

in the first page of the table immediately opposite to it.

If the number consist of three figures, find it in the first column of the following or second part of the table, opposite to which, and under or above 0, is its logarithm.

If the given number contains four figures, the three first are to be found, as before, in the side-column; and under the fourth at the top, or above it at the bottom, will be found the logarithm required.

To this prefix the proper index, and the whole is completed.

If the given number exceeds four figures, find the difference between the logarithm answering to the first four figures of the given number, and the next immediately following; multiply this difference by the remaining figures in the given number, point off as many figures to the right hand as there are in the multiplier, and the remainder added to the logarithm, answering to the first four figures, will be the logarithm required nearly. The logarithm of a vulgar fraction is found by subtracting the logarithm of the denominator from that of the numerator; and that of a mixed quantity is found by reducing it to an improper fraction, and proceeding as before; or the vulgar fractions may be reduced to decimals, and the logarithms found as usual.

Ex. 1.—What is the logarithm of 56?

In the first part of the table, opposite to 56, and under N. is 1.748188.

Ex.—What is the logarithm of 366?

In the second part of the table, opposite to 366, and under 0, is 2.563481, supplying the index. The first two figures are understood to be supplied in the blank space, till the change takes place at 57; and this must be attended to throughout the whole of this table, as well as several others that follow.

Ex. 3.—Required the logarithm of 7854? Opposite to 785, and under 4 is 3.895091

Ex. 4. Required the logarithm of 100176? The log. of 1001 is 000434 1002 is 000868

The difference is 434

Then 434×76 is 32984. From this cut off two figures, because the difference has been multiplied by two figures, 76, and it becomes 329.84. If the figure next the decimal point is less than 5, the whole may be rejected; but, if greater, increase the figure before the point by unity, and consequently, in the present case, 329.84 would become 330. Whence to 000434

Add 330, and supply the index 330

And the log. of 100176 will be 5.000764

In general the difference may be taken from the right-hand column, under D, unless the logarithms vary very rapidly, which happens only near the commencement of the table, as in the preceding example, where the difference under D is 432, the mean difference of the whole line, instead of 434 by actual subtraction. This would cause a difference of two units, in the last decimal place, less than that found above, or the logarithm would turn out to be 5.000762, instead of 5.000764.

To facilitate the method of obtaining proportional parts, there has been added to these tables an additional column on the left-hand side of the page, under P. P. In the column under N, the two first figures are omitted, and the third alone retained, by which means a regular series of the arithmetical digits, beginning with 1 and ending with 9, are obtained between each bar, or line across the page. Hence the proportional parts corresponding to the mean difference within the space marked out by each pair of cross bars, answering to any of the nine digits, can be placed opposite to each, which, in these tables, has been accordingly done. By this means the logarithm corresponding to any number extended to five or six places of figures, may be very readily obtained with sufficient accuracy, excepting, perhaps, when it falls in the second and third pages, where the differences vary rapidly.

Ex. 5.—Required the logarithm of 546876.

Log. of 546800	is 5.737829 ,	or	5.737829
Prop. part for 70			
for 6	48,		
		or	

Log. of 546876 is 5.7378898, or 5.737890

If the number consists of one figure more than four, or five figures altogether, the proportional part may be added at sight.

Log. of $\frac{1}{2}$ is therefore . . $\overline{1.945642}$ or 9.945642 Required the log. of $7\frac{5}{8}$, or $\frac{6}{8}$, or 7.625?

Log. of 7.625 is 0.88224

Required the logarithms of 24, 56, 102, 546, .7854, 78653, 54.4768, 97685.46, 0.001546, 0.176804, 0.00043689, 31, \$\frac{4}{3}\frac{4}{3}, 39766\frac{4}{3}\frac{4}{3}, 8546\frac{1}{16}\frac{1}{3}.

PROBLEM II.—To find the Number answering to any given Logarithm.

Find the logarithm next less than that given in the column marked 0 at the top, and continue the sight along that horizontal line till a logarithm the same as that given, or as near as possible, be found; then the three first figures of the corresponding natural number will be found opposite to it in the side-column, and the fourth immediately above at the top or below at the bottom of the page. If the index of the given logarithm be 3, the four figures thus found are integers; if the index be 2, the three first figures are integers and the fourth is a decimal, and so on, as may be easily understood by consulting Problem I. If the given logarithm cannot be exactly found in the table, and if more than four figures be wanted in the corresponding natural number, then find the difference between the given and the next less logarithm. To this annex on the right-hand as many ciphers as there are figures required above four in the natural number. Divide the whole by the difference between the next less and next greater logarithm, and the quotient annexed to the four figures formerly found will be the natural number required. The same thing may be done by the table of P. P. by subtracting a part corresponding to each unit from the difference between the given logarithm and the next less, and annexing these units successively in order to the number previously found.

Ex. 1.—Required the natural number corresponding to the loga-

rithm 2.495544?

This logarithm is found opposite to 313 and under 0, and, as the

index is 2, then 313 is the number required.

Ex. 2.—What is the number answering to the logarithm 3.828338? The logarithm is found 673, and under 5, therefore, since the index is three, the natural number is 6735. If the index had been 2, then it would have been 673.5, or the natural number must always consist of one integer (if there are integers) more than the index expresses.

Ex. 3.—Required the natural number answering to the logarithm

2.627980?

The natural number corresponding to this is 4246; but the index being $\overline{2}$, one cipher must be prefixed, from what has been said in Prob. I., and it becomes 0.04246.

Ex. 4.—What is the number answering to the logarithm 5.687956? The nearest less logarithm than this is 687886, corresponding to which will be found the number 4874. The difference between 687956 and 687886 is 70, to this annex two ciphers, and it becomes 7000, which being divided by 89, the difference of the columns found under D gives 79. This being subjoined to 4874 gives 487479, the number required. Or the same may be performed thus:

	48	7400	corresponds to				5.687956
gives		70	Diff. in P. P.	10	-0		70 63
gives	1	8	remainder as diff.	(40)	100	13.57	7 72

or in all 487478, differing only one unit in the last place from the former number.

LOGARITHMIC ARITHMETIC.

PROBLEM III .- To perform Multiplication by Logarithms.

RULE.—Add the logarithms of the factors, and the sum is the lo-

garithm of the product.

If there are both negative and affirmative indices, their sum is taken according to the rules of algebra; or the arithmetical complements of the negative indices may be used, rejecting the tens in their

The arithmetical complement of the logarithm of any number is . found by subtracting the given logarithm from 10, or by subtracting each of its figures beginning at the left-hand from 9, and the last effective figure from 10. When the arithmetical complement of the index alone is wanted, it is found by subtracting it from 10.

Ex. 1.—Multiply 6564 by 836.

Factor	$ \begin{array}{c} -\text{Multiply} \\ 6564 \\ \text{ors} \\ 836 \end{array} $	logarithm logarithm .	•		٠.		7169 2206
	5487000	sum . corresponds to	•				9375 9335
gives	500	diff. in P. P. for		•		•	40 40

or in all 5487500, which agrees as nearly with the real product 5487504, as tables extending to six places of decimals will give.

Ex. 2. Multiply the numbers 43.68, 0.534, and 0.007685 together

logarithmically.

Factors
$$\begin{cases} 43.68 & \text{log. } 1.640283, \text{ or } 1.640283 \\ 0.534 & \text{log. } \overline{1.727541 - 9.727541} \\ 0.007685 & \text{log. } \overline{3.885644 - 7.885644} \end{cases}$$

0.179254 1.253468 9.253468 Product

PROBLEM IV.—To perform Division by Logarithms.
RULE.—From the logarithm of the dividend subtract the logarithm of the divisor, the remainder is the logarithm of the quotient. Ex. 1.—Divide 5486 by 96.

Dividend Divisor	5486 le 96 le	og. 3.5 og. 1.9	739256 982271
Quotient		_	
0.07856 by	0 009A	00	45
nd 0.07856	v.vu34		$\log.$ $ ilde{2}$

Ex. 2.—Divide

Dividend Divisor	0.07856 0.003482	•	•	log. 2.895201 log. 3.541829

Quotient 22.5617	1.35337 2 39
------------------	------------------------

PROBLEM V.—To perform Proportion by Logarithms.

Rule.—From the sum of the logarithms of the second and third terms, subtract the logarithm of the first term; the remainder will be the logarithm of the answer. Or, instead of subtracting the logarithm of the first term, its arithmetical complement may be added to the other two, which, in many cases, is more convenient.

Ex.—A merchantman distant twenty miles, going at the rate of 5 knots or miles an hour, is pursued by a privateer, sailing at the rate of 7 miles; after three hours chase the breeze freshened, the merchantman's rate was increased to 6 knots, and the privateer's to 10. In what time will the privateer come up with the merchantman?

As the privateer gained 2 miles an hour on the merchantman, at the end of the first 3 hours, the distance between them is obviously 14 miles. During the remainder of the chase the hourly gain of the

privateer was 4 knots. Hence,

As the hourly gain 4^{m} ar. co. log. 9.397940 Is to the distance 14^{m} log. 1.146128 So is 1^{h} log. 0.000000

To the time required 3^h.5 or 3^h 30^m 0.544068 Consequently, from the time the breeze freshened, the privateer would come up with the merchantman in three hours and a half, or in six hours and a half from the commencement of the chase.

PROBLEM VI.—To perform Involution by Logarithms.

Rule.—Multiply the logarithm of the given number by the index of the power, and the product will be the logarithm of the power required.

Ex. 1.—What is the square of 64?
Given number 64
Index of the power
Square 4096.

3.612360

Ex. 2.—What is the third power of 24?

Given number 24 log. 1.380211 Index of the given power 3

Third power 13824 4.140633 508

PROBLEM VII.—To perform Evolution by Logarithms.

RULE.—Divide the logarithm of the given number by the index of the root, supposed to be expressed by an integer, as, for example, the square root by 2, the cube root by 3, and the quotient will be the logarithm of the root.

If the given number be a decimal, and the arithmetical complement of the negative index be used, then prefix 1 to that index for the

square root, 2 for the cube root, 3 for the fourth root, &c.

If the index of the root be expressed by a fraction of which the numerator is not unity, then multiply the logarithm of the given number by the numerator, and divide it by the denominator of that index.

Ex. 1.—What is the square root of 1296?

Given number 1296 log. 3.112605 Square root 36 1.556302 Ex. 2.—Required the cube root of 0.0009261?

Given number 0.009261 log. 3.966658, or 7.966658 Cube root 0.21 1.322219, or 9.322219

What is the fourth root of 0.00007634?

Given number $0.00007634 \log \overline{5}.882752$ Given index . . . $\frac{1}{4}$

Log. of the root 0.0934734 $\overline{2}.970688$

In this example, because the index of the root 4 is not contained in the negative index $\overline{5}$ a certain number of times exactly, the logarithm $\overline{5}.882752$ is resolved into its equivalent $\overline{8}+3.882752$, and the product of this by $\frac{1}{4}$ is $\overline{2}.970688$ the logarithm of the root required.

TABLE III .- The Angles which every Point and Quarter Point of

the Compass makes with the Meridian.

This table is useful for reducing the points of the mariner's compass to degrees, and conversely. It is divided into seven columns; in the two first and two last columns are contained the names of the several points; the third and fifth contain the corresponding points and quarter points reckoned from the meridian; and the fourth the degrees, minutes, and seconds, answering to them. Its use is obvious.

TABLE IV.—Logarithmic Sines, Tangents, and Secants, to every

Point and Quarter Point of the Compass.

In performing calculations relative to navigation, it will be found convenient to take the logarithmic sines, tangents, and secants, from this table, thereby saving the trouble of reducing them to degrees, &c., by the preceding table. The manner of using it is easy, and will be readily understood from the explanation of the table which immediately follows.

TABLE V.—Logarithmic Sines, Tangents, and Secants.

This table contains the logarithms of the natural sines, tangents, and secants, to each degree and minute of the quadrant in the usual manner. To facilitate calculations in which time is involved, the degrees and minutes have been converted into time at the rate of 15° to an hour, and annexed at the top and bottom of the page and in two additional side-columns.* These, together with proportional parts to each second of time, or to every fifteen seconds of a degree, at the bottom of each page, will, it is hoped, render this table still more easy and general in its use than those of a similar kind usually given.

The degrees are numbered at the top of the table, in a direct order, from 0° to 45°, and, at the bottom of the table, in a retrograde order, from 45° to 90°. The minutes are contained in two of the marginal columns. The minutes in the left-hand column belong to the degree at the top of the page, and those in the right-hand column belong to the degree at the bottom. In like manner, the minutes and seconds of time in the first left-hand column belong

[•] This table will therefore convert degrees into time, and conversely.

to the hour at the top, and those in the right-hand column belong to the hour at the bottom. To promote perspicuity, it is recommended to mark minutes and seconds of the circle always by accents, and those of time by m and s, as is done in the tables.

PROBLEM I .- To find the Sine, Cosine, &c. answering to any given

Degree or Minute.

Rule.—Find the given degrees at the top of the page if less than 45°, and the minutes in the left-hand column; opposite to which, and under the word sine, cosine, &c. is the number required. But if the given degrees be greater than 45° and less than 90°, find them at the bottom, and the required sine, cosine, &c. will be found above the word sine, cosine, &c. opposite to the given number of minutes in the right-hand column. If the given arc exceed 90°, find the sine, cosine, &c. of its supplement, or, which comes to the same thing, and will be more easy in practice, to find the sine of an arc above 90°, reject 90°, and take the cosine of the remainder. To find the cosine of an arc above 90° reject 90°, and take the sine of the remainder. The same method may be pursued for the tangents and secants both for arcs and time, recollecting that 90° corresponds to 6h.

Ex. 1.—Required the log. sine of 23° 28'?

Under the word sine in the page marked 23° on the top, and opposite to 28' in the left-hand column, is 9.600118, the sine required.

Ex. 2.—What is the cotangent of 55° 57'?

In the page marked 55°, at the bottom and opposite 57' in the right-hand side-column, is 9.829805, the cotangent of 55° 57'.

Ex. 3.—Required the secant of 125° 40'?

The supplement of 125° 40' is 54° 20', the secant of which is 10.234280, or, which comes to the same thing, the cosecant of 35° 40' the excess of 125° 40' above 90° is 10.234280, the secant required. Hitherto the given arc has been supposed not to exceed 180°; but, in several astronomical calculations, it frequently happens that arcs through the whole circle are employed; consequently, if the arc lie between 180° and 270°, diminish it by 180°; if between 270° and 360°, take its explement to 360°, and take the logarithmic sines. &c. as before. Otherwise, for the log. sine, &c. of an arc between 270° and 360°, take the log. cosine, &c, of its excess above 270°, and for the log. cosine, &c. of an arc between 270° and 360°, let the sine, &c. of its excess above 270° be taken. And for the log. sine, &c. of an arc between 180° and 270° let the log. sine of its excess above 180° be taken. Thus the log. sine of 300° 28' is the log. sine, &c. of 30° 28', the excess above 270°; and the log. sine of 220° 18' is the same as that of 40° 18', and so on. The same may be done when time is employed, recollecting that 6h corresponds to 90°, 12h to 180°, 18h to 270°, and 24h to 360°.

PROBLEM II .- To find the Sine, Tangent, &c. of an Arc expressed in

Degrees, Minutes, and Seconds.

RULE.—Find the sine, tangent, &c. corresponding to the given degree and minute, and also that answering to the next greater minute, multiply the difference between them by the given number of seconds, and divide the product by 60; then the quotient added to the sine, tangent, &c. of the given degree and minute, or subtracted from the cosine, cotangent, &c. will give the quantity required nearly. To facilitate this process the difference, to 100", has been given in the column marked D. Multiply this difference by the

number of seconds, cut off two figures from the right, and add the remainder to the sine, tangent, &c. of the given degree and minute, or subtract it from the cosine, &c., and the quantity required will be obtained nearly.

Ex. 1.—Required the log. sine of 23° 27′ 40″? Log. sine of 23° 27′ is 9.599827
23 28 is 9.600118

Difference 291 Seconds 40

194

Log. sine of 23° 27′ 9.599827 Proportional part for 40″ 194

Striking off two figures on the right gives 194,00 The same as before.

If no very great precision is required, then the proportional part for the nearest fifteen seconds may be taken from the small table at the bottom of the page.

Ex. 2.—Required the logarithm tangent of 2^h 24^m 46^e?

Log. tangent of 2^h 24^m 44^s is 9.864180 Proportional part for 2^s is 132

Log. tangent of 2^h 24^m 46^h is 9.864312 Ex. 3.—Required the secant of 9^h 45^m 36^h?

The cosecant of its excess above 6^h, or 3^h 45^m 36ⁿ, gives 10.079396. Required the sine of 20^h 44^m 56^e?

The cosine of 2 44 56 is 9.876236 being the sine of $20^{h} 44^{m} 56$.

PROBLEM III.—To find the Sine or Tangent of a small Arc, less than three Degrees.

1. To find the size.

To the logarithm of the arc reduced to seconds, with the decimal annexed, add the constant quantity 4.685575, and from the sine subtract the third of the arithmetical complement of the log. cosine, or, which comes to the same thing, one third of the secant; the remainder will be the logarithmic sine of the given arc.

2. To find the tangent.

To the logarithm of the arc in seconds and constant quantity 4.685575, add two-thirds of the secant, the sum is the log. tangent of the given arc.

Ex. 1.—What is the log. sine of the sun's mean horizontal paral-

lax, supposed to be 8".68?

Logarithm of 8".68 is 0.938520 Constant . 4.685575 One-third of sec. 8".68 is 0.000000

Log. sin of 8",68 is 5.624095

Or, since in very small arcs the sine and tangent are each very nearly equal to the length of the arc, when it does not exceed 10, and the length of an arc of one second is 0.0000048481368; multiply the length of one second by the number of seconds and parts of a second making the index positive by the former rules, and the sine or tangent, will be obtained, thus,—

 $0.0000048481368 \times 8''.68 = 0.0000420818274$; the log. of this is

5.624094, the log. sine or tangent required.

Ex. 2.—Required the tangent of 1° 24' 36".46?

To the constant logarithm . 4.685575

Add log. of 1° 24' 36".46=5076.46 3.705561

And $\frac{2}{3} \times 0.000132=$. 88

Log. tang. of 1° 24′ 36″.46 . 8.391224

PROBLEM IV .- To find the Degrees, Minutes, and Seconds answer-

ing to any given log. Sine or Tangent.

RULE.—In its respective column find the nearest sine, tangent, &c. to that given; and take the degrees from the top or bottom of the page, according as the quantity is found in a column, with the proper title at the top or bottom; and the minute is found in the same horizontal line, in the left or right hand marginal columns, according as the quantity is found in a column titled at the top or at the bottom of the page.

Ex. 1.—Required the arc, or degrees and minutes corresponding

to the log. sine 9.584665?

This is found in a column marked sine at the top under 22 degrees, and opposite 36 minutes, or I hour, 30 minutes, and 24 seconds of time.

Ex. 2.—What is the arc in degrees or time answering to the logtangent 10.358430, making use of the tables of proportional parts at the bottom of the page.

Given log. tangent 66° 20′ 0′′ corresponds to	10.358430 10.358253
And 0 0 30 to	177 173
Hence 66 20 30 is the arc required. Or, 4 ^h 25 ^m 20 ^s answer to	10.358253
And 2 to 173, or nearly	177

Hence 4 25 22 is the time nearly.

Or to 177 add two ciphers, and divide by 572, the number under D. and opposite to 10.358253, or rather by 573, the number above it, as the form in which the tables are printed requires, and we have

66° 20′ 31" very nearly; and this method must be followed in all similar cases.

Problem V.—To find the Degrees, Minutes, and Seconds answering

to the Logarithmic Sine or Tangent of a very small Arc.

Rule.—To the given log. sine add the constant 5.314425 and onethird of the corresponding secant, the sum, rejecting 10 in the index, will be the logarithm of the number of seconds in the required arc.

To the given log. tangent add the constant 5.314425, and from the sum subtract two-thirds of the corresponding secant, rejecting 10 in

the index, the result will be the logarithm of the seconds of the required arc.

Ex. 2.—What is the arc whose log. tangent is 7.164440?

Constant . 5.314425

Given log. tangent . 7.164440

§ of 0.000000 is . 0.000000

Log. arc 301".207 . 2.478865

Or 5' 1".207

TABLE VI.—Natural Sines, Tangents, Secants, and versed Sines to every Degree of the Quadrant.

The method of taking out the numbers required from this table will be readily comprehended from what has already been said relative to the preceding. When minutes or seconds occur, proportional parts must be taken by means of the differences found by actual subtraction.

TABLE VII.—Meridional Parts to every Degree of the Quadrant. The degrees are found under the letter D, and the meridional parts under M. P., and when minutes and seconds occur, proportional parts of the difference must be taken in the manner shewn above.

Ex.—Required the meridional parts answering to 45° 36′?

Meridian parts to 45°

Prop. part of diff. 85.7 to 36′ is

50.6

Meridian parts to 45° 36′ is . 3080.5

TABLE VIII.—Traverse Table, or difference of Latitude and Departure.

This table contains the measures of the sides and angles of rightangled plane triangles, the distance being represented by the hypotenuse, and the difference of latitude and departure by the legs or sides about the right angle, and the course and its complement by the acute angles. Hence, if any two of these be known, except the two acute angles, the rest are found by inspection. The course is given in degrees or points in the two exterior marginal columns, the distance is found at the top or bottom of the page, according as the course is less or greater than four points or 45°; and the difference of latitude and departure is found in columns under or above these words respectively.

If there are minutes in the course, proportional parts may be taken where great accuracy is required, otherwise they may be omitted if

less than 30′, but, if more than 30′, the degrees in the course must be increased by 1°. The distances 1, 2, 3, 4, &c. at the top and the bottom may be accounted 10, 20, 30, &c., or 100, 200, 300, &c. if the difference of latitude and departure be increased in the same proportion by removing the decimal point a corresponding number of places to the right. If the distance consist of several effective figures, the difference of latitude and departure must be found for each figure separately, and the sum of the results taken.

PROBLEM I.—The Course and Distance being given, to find the Dif-

ference of Latitude and Departure.

Find the course in right or left hand column, and in a line with it, under or above the given distance, the difference of latitude and departure will be obtained.

Ex. 1.—A ship sails N. N. E. 60 miles, what difference of latitude

and departure has she made?

Course. Dist. Diff. Lat. Departure. 2 points . 60 . 55.433 . 22.961

Ex. 2.—A ship sails S. E. b. S. \(\frac{1}{2}\) S., or S. S. E. \(\frac{1}{2}\) E. 244 miles, re-

 quired her difference of latitude and departure?
 Dist.
 Diff. Lat.
 Departure.

 2½ points
 200
 176.38
 94.28

 40
 35.277
 18.856

 4
 3.5277
 1.8856

244 215.1847 . 115.0216

Ex. 3.—A ship sails 300 miles S., 54° 30′ W., what is her difference of latitude and departure?

Course. Dist. Diff. Lat. Departure. 300 . 176.34 . 242.71 . 245.75

Mean 541 . 300 . 174.20 . 244.23

When several courses and distances are given, the results must be placed in a table, the sum of the several northings and southings, eastings and westings taken, and placing the less sums under the greater, the differences will shew how much the ship has, upon the whole, changed her situation, and in what direction she has moved.

TABLE IX.—Diurnal Logarithms.

This table, to which I have ventured to give the title of Diurnal Logarithms, is useful for making computations in which time is concerned, particularly for reducing the right ascension and declination, &c. of the sun or moon to any intermediate time between those times given in the Nautical Almanac, where the proportional parts to daily differences are required. It has two sets of arguments, the one answerto 12h, since the moon's place is given in the Nautical Almanac for every noon and midnight; the other corresponding to 24h for the sun.

Rule.—To the logarithm from this table corresponding to the Greenwich apparent time add the proportional logarithm (Table X.) of the variation on the given day for 24^h or 12^h, as the case may be, the sum will be the proportional logarithm of the part of it for the given time, which, added to or subtracted from the number corresponding to the preceding noon or midnight, according as it is increasing or decreasing, will give its value at the instant required.

Ex. 1.—Required the sun's right ascension March 20th, 1826, at `20h 46m 40' apparent Greenwich time.

Greenwich time . 20h 46m 40 D. L. 0.06262

Change of R. A. in 24^h 3 38.2 P. L. 1.69457

Prop. part for 20° 46° 40° 3 9.0 1.75719 R.A. at preceding noon 23 57 42.0

R. A. at 20^h 46^m 40^t 0 0 51.0

Ex. 2.—Required the moon's declination September the 15th, 1826, at 7^h 48^m 30^s P. M. apparent time on the meridian of Greenwich?

Moon's declination at noon . 2° 7′ 8″S. at midnight 0 9 19 N.

Sum = diff. in 12 hours . 2 16 27

App. time 7^h 48^m 30^p diurnal log. . 18662

Change of dec. in 12^h, 2° 16′ 27″ prop. log. 12030

Change in 7^h 48^m 30^s+1° 28 47 prop. log. 30692 Dec. at noon . —2 7 8

Dec. at 7^h 48^m 30^s —0 38 21 S.

When the differences are very irregular, a correction on that account becomes necessary. This will be exemplified in the explanation of Table XXVII.

TABLE X .- Proportional Logarithms.

This table is chiefly useful for facilitating the method of finding the apparent time at Greenwich, answering to a given central distance between the moon and the sun, a fixed star or a planet, by the assistance of the Nautical Almanac. It is extended to three hours on account of the distances being given in various ephemerides to every three hours of time. As degrees and hours are similarly divided, it answers equally well for either, and is marked accordingly. To this table proportional parts have been added at the bottom of each page to every tenth of a second, which may be useful where great accuracy is required. The table is very useful in calculations where sexagesimal divisions are employed. The method of taking out the log. of any quantity will be readily understood from what has already been said.

TABLE XI.—Depression or Dip of the Horizon.

The dip of the horizon is an angle contained between a horizontal line passing through the eye of the observer, and a line from his eye to the visible horizon, when these lines are in the same vertical plane. This table contains the dip answering to a free unobstructed horizon, and the numbers corresponding to the height of the eye are to be subtracted from the observed altitude when taken by the fore observation, but added to it in the back observation.

TABLE XII.—The Dip at different Distances from the Observer. If the land is not sufficiently distant to afford a free horizon, it may be sometimes necesary to obtain an altitude referred to the surface of the sea at some known or estimated distance. Under such circumstances the dip may be taken from this table.

TABLE XIII.—Correction to be added to the observed Altitude of the Sun's lower Limb when taken by a fore Observation to find the true Altitude.

This table was computed by the author a good many years ago for the purpose of combining the usual corrections, namely, dip, refraction, parallax, and semidiameter. The variation of the sun's semidiamenter from 16'. is given at the bottom of the table, which, unless considerable accuracy be required, may be neglected. The arithmetical complement of the numbers from this table to 32', will be the correction to be subtracted when the upper limb is observed.

TABLE XIV .- Correction to be subtracted from the observed Al-

titude of a fixed Star to find the true.

This table is similar to the last, and contains the sum of the two corrections, dip and refraction, to be subtracted when the fore observation is employed.

TABLE XV.—This table, taken from the Nautical Almanac for 1826, will answer for most purposes for a considerable number of years to come. It contains the time of the sun's semidiameter passing the meridian, the sun's semidiameter, hourly motion in longitude, and the log. of the sun's distance from the earth, for every sixth day

in the year.

The time of the sun's passing the meridian is useful for reducing an observation of a passage of the preceding or subsequent limb over the meridian taken with a transit instrument, to that of the centre. The semidiameter of the sun is necessary to reduce an observation of the limb to that of the centre, whether in altitudes or angular distances. It is also useful for determining the index error of a sextant, or the exactness of the scale of micrometers.

The hourly motion is useful for computing eclipses. The log. of the sun's distance is requisite in the calculation of the places of the

planets and comets, and for some other purposes.

TABLE XVI .- The Sun's Parallax in Altitude and Zenith Dis-

The author computed this table from a mean of the determinations of Delambre from the observations of the transit of Venus over the sun's disk in June 1769. He found the mean horizontal parallax to be 8".68. It is hoped it will prove useful where great accuracy is required.

TABLE XVII.—Mean Refractions.

For the elements of this table the author is indebted to the liberality of Mr Ivory, the most distinguished mathematician in the British islands. On comparing it with that given in the Transactions of the Royal Society of London, it will be seen that it has been expanded considerably, so as to render its application more easy by giving the mean refraction, and its logarithm for every 10' from the zenith to the horizon, subjoining the differences of the logarithms for the purpose of computing proportional parts more readily.

TABLES XVIII, XIX, and XX.—These tables are employed to correct the preceding according to the state of the barometer and thermometer, as shown in the explanation at the bottom of page 89

of the tables. In the seventh line from the bottom of that page, after thermometer, there should have been added, " or 0.002083 for one degree of Fahrenheit," that used in the construction of the table.

Ex. 1.—Required the mean refraction for 21° 40' of zenith distance

or 68° 20' of altitude?

Opposite to 21° 40′ in table XVII., and under 36, will be found 0′ 23°.21, the refraction required when the barometer stands at 30 inches, and the thermometer at 50°, and this is sufficient for most purposes when great accuracy is not required.

Ex. 2.—Required the true refraction when the zenith distance is

70° 41'.7, the barometer 30.045, and thermometer 34	
Zenith distance 70° 40′ log. 30 Table XVII.	2.21752 . 68
Thermometer 34° Table XVIII.	0.01472
Barometer 30.0 Table XIX.	0.00000
.045	6
Thermometer 34 Table XX.	. 70
Log. r . 2' 51".27 = 171"27 . Observed refraction 2 51 .50	2.23368
Error of the table — 0.23	
	J hansmater 00 5
Ex. 3.—Let $\theta = 87^{\circ} 42' 10''$, thermometer 35°, and in the second in	a parometer 29.5
inches, what is the true refraction?	2.00400
$\theta = 87^{\circ} 40' 0'' \log_{\circ} \delta \theta \qquad .$	3.00466
	390
Ther. 35°	0.01379
Bar. 29.5	9.99270
Ther. 35	. 65
Log. r' . 17' 16".81 = 1036".81 .	3.01570
$\frac{a\delta b}{d\tau} \times (35^{\circ}-50^{\circ}) =$	
$-0.606 \times -15 = +9.09$	
$\frac{\partial d\theta}{\partial p} \times (29.5 - 30.0) =$	
$\times 1.04 \times -0.5$. = -0.52	

	-,		
	-		
Error of the table		1	.12

				Example	s for .	Exercise			
	Z .	\boldsymbol{L}).	Bar.		ierm.	0	bs. Ref.	Error.
				In.	In.	Out.		•	
ı.	70°	46′	30′′.0	29.686	46 9	44.17	2′	44".83	+ 1".51
2.	76	55	31 .2	29.686	40	37.10	4	8 .98	+ 1 .86
3,	81	27	18 .6	29.924	61	58.19	6	1 .90	
4.	83	58	6 .7	29.810	36	29.95	8		+0.53
5.	86	14	42 .0	29.174		47.75	12		+ 0 .28
6.	87	23	44 .0	30.000	60	56.08	15		<u> </u>
7.	88	39	32 .0	29.800	38	34.40	23		-15 .70
8.	89	26	51 .4	29 907	39	33.46	30	16 .60	

Hence at moderate zenith distances the error of the table is small, sometimes + and at other times -. From 70° to about 85°, the error is generally +, but from 85° to 90° it becomes -, and is considerable near the horizon. We may therefore infer that the horizontal refraction, 34' 17".5, given by the table in a mean state is, in general, too small, though, from the uncertainty and irregularity to which it is subject, it is very difficult to estimate accurately its true quantity. Perhaps from the irregularity of temperature in various parts of a line near the surface of the earth through which the ray of light must pass to reach the eye of the observer, it will be impossible ever to assign the true quantity of the horizontal refraction under given circumstances. In fact, no instrument, as yet, has been employed to ascertain the effects of aqueous vapour floating in the atmosphere, on the exact quantity of the horizontal refraction; and we suspect that the barometer and thermometer alone are inadequate to that purpose.

TABLE XXI.—Augmentation of the Moon's Semidiameter in Al-

titude and Zenith Distance.

The apparent magnitude of any object being in the inverse ratio of its distance, and as the moon is nearer the observer in the zenith than in the horizon, by the earth's radius her apparent semidiameter must be greater in the former situation than in the latter. This table contains that increase corresponding to six different values of the semidiameter, at different degrees of altitude. If the quantity is not found to the accuracy required by inspection, it may be determined by proportional parts in the usual manner.

TABLE XXII.—Reduction of the Moon's Parallax in the Spheroid.

As the earth differs somewhat considerably from a sphere, the eccentricity being about $\frac{1}{3}\frac{1}{10}$, it follows that the equatorial parallax must be greater than that at the various intermediate latitudes from the equator to the pole. This table contains the quantity to be subtracted from the equatorial parallax given in the Nautical Almanac to reduce it to what it ought to be at any other latitude.

TABLE XXIII.—Logarithms of the Earth's Radii in each Parallel of Latitude; the Equatorial Radius being Unit, and Compression 300.

This table will be found useful in some nice observations in astronomy, where the spheroidal figure of the earth must be taken into

account

Example. To Greenwich in latitude 51° 28′ 38″ the radius is 9.9991121.

TABLE XXIV.—Angles which, the vertical to any point of the Earth's surface, makes with the Radius drawn from that point to the centre, or, as it is usually called, the Reduction of the Latitude to $\frac{1}{2}$ of compression.

This table is useful in several astronomical observations, such as

the computation of eclipses, occultations, &c.

Example.—The apparent latitude of Greenwich is 51° 28' 38".4, required that reduced to the centre?

Latitude . 51° 28′ 38″.4 Reduction . — 11 10 .8

Reduced latitude 51 17 27 .6

From this table the reduction of the altitude may be obtained by the

following rule:

To the secant of the azimuth reckoned from the meridian of an opposite name from the latitude, add the proportional logarithm of the reduction of latitude, the sum will be the reduction of the altitude, to be reckoned positive when the azimuth is less than 90°, and negative when greater.

Example.—Required the reduction of altitude corresponding to an

azimuth of 36° 42' in the latitude Greenwich 51° 28' 38" N.

Latitude 51° 28′ 38″ Secant 0.20563 Reduction of alt. 11 10.8 Prop. log. 1.20683

Reduction of lat. 6 57.8 Prop. log. 1.41246

In computing time, &c., if the reduced latitude be used, the reduced altitude must be employed also; but, in general, unless absolutely necessary in such computations as that of time, it is easier not to employ either of these reductions.

TABLE XXV.—For determining the Latitude at any time by the Pole Star.

This table was computed by Mr Littrow of Vienna, and will be found very useful for determining the latitude of a place by the pole star. A full explanation is given at the bottom of the page immedi-

ately under the table.

Ex 1.—In latitude 56° N. nearly, the zenith distance (Z) of the pole-star, by an astronomical circle, was found to be 35°. 20′ 50″, when its apparent polar distance (p) was 1° 36′.7, and the star just $14^{\rm h}$ 26° 56° from the time of upper culmination; required from these data the exact colatitude of the place of observation.

data the exact colatitude of the place of observation. Now $14^h 26^m 56^s$ gives M = 3''.23, and N = - 0° 0′ 0′'.48 And $31''.23 \times -3'.3 \times 0.02 = -2''.06 = -3.3 \times .02 M$ Then 31''.23 - 2''.06 = 29''.17 = M', log. 1.4649 Cot. $Z 35^9 21'$ 0.1491

1.6140 = -0 0 41 .12

Cos. t. 14^h 26^m 56ⁱ=9.9039 p 96'.7 log. . 1.9854

Colatitude 34 ·2 38 ·40 Latitude 55 57 21 ·60 Edinburgh, 10th January, 1826.

On the Caltonhill, near the Observatory, with one of Troughton's reflecting circles on a stand, and an artificial horizon, the author, at about ten o'clock, r. m. observed the following double altitudes of the polar star, when the symplesometer stood at 29.86 inches, and

thermometer at 42° Fahrenheit; required the latitude of the place of observation.

	derial Tin		Double				
	After Transi	t.	With A				
ill and homesto 4			113°				
	1 23 3		113	10	55		
m la millione 4	1 24 30	Donosla.	113	10	55		
I millional Got	4 25 40	Out them	113	10	50		
	1 26 4		113	1000			
ma . '00 mail and	20 1		110	44			
	24 36		113	10	54		
or of math ones	1 10			0.5	-		
App. alt. or	half		56				
			90	0	0		
-1 - COMP			11	-	-		
App. zenith d	list. or co	mp.		24			
Now by table	s 17, 18,	19, and 20), compi	ite th	e refra	ction.	
Zenith di	ist. $=33^{\circ}$	24' 33" log	;. de (17)	1.58	60	
Thermor	neter 42°	Fah. (18)	varalities.	9.56 1	0.00%	73	
Baromet	er 29.8	6 inches (19)	(COL	9.998	80	
Thermor	meter 420	Fah. (20)			0.000	03	
A Hermor	Hetel 12	ran. (20)	Seat Carrie		0.00	00	
Lan w	20// 05				1.59	16	
Log. r=	39 .00			-			
App. zenith d		- 1 1	18	- 2		24' 33"	
Refraction	THE RES	SELECTION OF		7711	-	0 39.0)5
					1	-	To the last
Now 4h 24m 3	listance	of soil less	ALC: N	Carlo	33 2	25 12.0	5
Now 4h 24m 3	36' gives	M = 72''.97	3.	and M	V = +0	° 0' 0"	57
Then 72".973	×-3'.3	× 0.02=-	4.816-	3/3 >	02 M	A. Commercial	1
And 72".973-	4" 816-	68" 15710	c 1 833	510		200	
Cot. Z=33° 2							
Cot. 2=35 2	10 12	100 (6)	0.100	000			
THE PERSON NAMED IN COLUMN	The state of	100// 0/	001	0.45	4 11 2	15-10	00
Natural numb			=2.014		- 0	1 43.	29
Cos. t=4 ^b 24 ^b			0.606751	10.0			
p 96'.7 log.	1 201 SCE	I PURT	.985426	$\Omega = B$			
		1		D			
Natural numb	per	39'.19=1	.592177	=	+ 0	39 11.	40
		-		100	1		A STATE OF
Sum .					10	37 28.	68
Z .	-	7	-			25 12.	
4	2			SPACE AND	00	20 12.	03
1	2			SOUTH T	04	0.10	70
\$\psi\$ or colatitud	le .	The same		-		2 40.	
Latitude			100 - 10		55		
From a trigor	nometrica	l measurer	ment he	also f	ound th	ne latitu	ade 55°

From a trigonometrical measurement he also found the latitude 55° 57′ 20″.7 N., supposing with Captain Kater the latitude of the flag-staff in Leith fort to be 55° 58′ 39″ N.

TABLE XXVI.—Delambre first calculated this Table for finding the augmentation of the semidiameter of the Moon in solar Eclipses and occultations, without computing the altitude. It is used as follows:

To the altitude of the nonagesimal in signs, add the distance of the

To the altitude of the nonagesimal in signs, add the distance of the moon from it, and from that altitude subtract the moon's distance from it; then take the equations from this table, Part I. answering to the sum and difference, and take the sum of these, regard being had to the signs. To this add the equations corresponding from Part II. If the observation be that of an occultation, the equation answering to

the true latitude and parallax in latitude of the moon is to be taken from Part III. In a solar eclipse this part vanishes. Then enter Part IV. with the sum of the former equations in the first vertical column, and the horizontal semidiameter at the top; and take out the corresponding number, which being applied to the former aggregate, according to its sign will give the augmentation of the moon's semidiameter.

Ex.—Let the altitude of the nonagesimal be 55° 18′, the apparent distance of the moon from it 14° 42′, the moon's true latitude 24' 2″ S., the parallax in latitude 35' 40″, and the horizontal semidiameter 15' 30″; what is the augmented semidiameter?

Altitude of nonagesimal 1° 25° 18′ App. dist. of moon from it 0 14 42

Sum	2 10 0 1 10 36	Part I. +7".70
Remainder	1 10 36	I. +5.33
		+13.03
		Part II. + 0.17
NF 14 14 04/0// 9 1	1-4 95/ 40/	D III 010
Moon's true lat. 24' 2" S., and pa	ar. in lat. 35' 40'	Part 111.— U.12
Q		. 19.00
Sum · · ·		+ 13.06
Sum To moon's semidiameter 15' 30"	. and Sum 13".08	Part IV 0.82
20 1110011 0 00111111111111111111111111	,	3.00
Augmentation		. 12.26
Semidiameter		. 15′ 30.00
Semidianieter	• •	. 15 50.00
		15 40 00
Augmented semidiameter .	• •	. 15 42.26
U		

TABLE XXVII.—Equations of Second Differences for twelve Hours.

In computing the moon's place from the nautical almanac for any given time by proportion, a correction resulting from the moon's unequal motion must be applied to the proportional part of the moon's motion in longitude or latitude, answering to the given time after noon or midnight. This correction is contained in the table, the arguments of which are the mean of the two second differences of the moon's motion at the top, and the apparent time after noon or midnight in the respective side column. This equation must be added to, or SUBTRACTED from, the proportional part of the first difference of the moon's motion in twelve hours, according as that difference is decreasing or INCERASING.

Hence the correct change, corresponding to the given interval, will be obtained.

If the given second difference is not found in the table exactly, the sum of the equations answering to the several terms, which make up the second difference collectively, is to be taken.

This table may be applied in the computation of the place of a planet. And as the sun's declination varies somewhat irregularly about the solstices, a column has been added to the lower half of the table on the right side for differences in twenty-four hours, to determine the exact declination for any given time where great accuracy is required.

Ex. 1.—Required the moon's declination on the 15th of September,

1826, at 7h 48m 30 P. M. apparent time on the meridian of Green-

wich?

In the explanation of Table IX. this is found to be 0° 38′ 21″ S. by proportion; it is only now required to find the correction depending on second differences. For this purpose two declinations must be taken out preceding the given time, and two after it, from which the mean second difference must be found.

The Moon's declination,

1826, First Diff. Sec. Diff. Mean.

Sept. 14th at midnight is 4° 23′ 24″ S. 2° 16′ 16″

15th at noon 2 7 8 S. 2° 16′ 16″

15th at midnight 0 9 19 N. 2 16 17

16th at noon 2 24 27 N.

10th 2 24 27 N.

If the first differences first increase and then decrease, or vice versa, half the difference of the two second differences is the mean, instead of half the sum, as would have been the case had the differences regularly increased or decreased.

In this case the equation must be added or subtracted, according as the first difference is greater or less than the third first differ-

ence.

Now to 30'' and 7^h 48_2^{hm} the equation is 0.4The whole equation is 3''.4 0.4

The true declination is 0.000. 0.000. 0.000. Unless the declinations are all north or all south, it is almost unnecessary to use the equation of second differences.

Ex. 2.—Required the moon's right ascension on the 20th Novem-

ber, 1826, at 9h 36m 30s p. m.?

The Moon's right ascension,

Prop. part 4' 56'.12 Prop. log. 1.56196 Or 4° 56' 7".2

In this example we have considered the degrees minutes, the minutes seconds, and the seconds have been converted into a decimal by dividing by 6, since the change of declination exceeds the limits of the table. This comes to the same thing as dividing by 60; but any other aliquot part might have been taken,—such as a half, a

third, &c. provided the proportional part be doubled, trebled, &c. as derived from this table.

Amoun	t of the	whole e	qua 10 F	tion	is '' 2: he	Canse	the	7	.2 diffe	rc
		and	0	41/2	•		•	0	.4	
Now to	9" 30"	30° and and			quation	1 18		U 4 2	".o .3	

Which must be added to 4° 56′ 7″.2, because the first differences are decreasing, consequently the corrected proportional part is 4° 56′ 14.″4.

The true right ascension required is . . . 127 28 1 .4 Ex. 3.—Required the sun's declination at noon, on the 20th of

June, 1826, at Otaheité, in longitude 9^h 58^m W.?

Sun's declination at noon

23° 27′ 11″ N.

Time 9^h 58^m diurnal log. 0.38166 Var. 0' 25" prop. log. 2.63548

P. P. 0 10".4 3.01714 10 .4 First Diff. Second Diff. Mean. Diff. for 19th 51 26 25 20th 25 3 .0 24 21st 1 True declination 23 27 24.4

In this example the argument in time is found in the right-hand column in the lower half of the table. In lunar distances the approximate time found by proportion after the hour given in the nautical almanac must be quadrupled, which, being used as an argument, will give to the mean second difference the true equation, amounting, in some cases, to about 6" in distance, or 3' of longitude.

TABLE XXVIII.—Reduction to the Meridian, Parts I. and II.

In the course of the great trigonometrical survey lately performed in France, the repeating circle was much used in the determination of latitudes and other operations. Latitudes were determined by observing repeatedly, near noon, the altitudes or zenith distances of a celestial object, reducing those taken off the meridian by appropriate formulæ or tables to what they would have been on the meridian. This method may be successfully practised by smaller instruments,—such as Troughton's reflecting circle, or even a good sextant; and Dr Brinkley, with his large eight-feet circle in the observatory at Dublin, takes three or four observations each day as near noon as possible, which are afterwards reduced to noon.

To facilitate these operations, this table has been computed, Part

I. by Delambre, and Part II. by Schumacher.

Ex. 1.—Application of the preceding table to observations of the star Arcturus at the observatory of Dublin, on May 12th 1820, made with the eight-feet circle, having three microscopes, one on the right side of the instrument, one at the bottom, and one on the left.

The latitude of the observatory from numerous observations of Dr Brinkley, corrected by his own very accurate table of refractions,

which are peculiarly adapted to his observatory, is 53° 23′ 13″.46 Mean N. P. D. of Arcturus for 1820 69 52 31 .89 Mean right ascension 211 51 51 .6 Place of moon's node 11° 29 26

Time by Clock.	Left Micros	Z. D. Bottom Microscops.	Right Micros.	Mean of Micros	the three	Refraction
h. m. s.	40.77	33 19 50.5 E.	4.3	33 19	54.83	2700
13 56 28	49.7					37.82
14 0 28	31.7	33 17 32.6 E	47.1	17	37 .13	37.77
14 9 51	50.6	33 14 54.5 W.	45.0	14	50.03	37.74
14 14 52	38.0	33 16 41.0 W.	31.7	16	36.90	37.77
Barometer 2	9.67	Inter. Ther. 52.5 Ext. — 48.0	Mean.	33 17	14.72	37.773
Time of Star's				Redu	ction.	
Pransit by Clock-	h. m.	a h m a	Part	1.	Par	t II.
14 7 3.3		28 0 10 35.3	220	.10	0".	12
14 7 3.3	14 0	28 0 6 35.3	85	.22	0.	.02
14 7 3.3	14 9	51 0 2 47.7	15	.32	0 .	.00
14 7 3.3	14 14	52 0 7 48.7	119	.80	0.	04
		Sum's	440	.44	0	18
			110 .	11	0 .	045

Now, if the tabular quantity in Part I. be called m, and that in Part II. be called n, the latitude λ , the declination λ , the approximate zenith distance z, the declination and zenith distance being + if north, and - if south, and the true zenith distance Z;

then
$$Z = z - \frac{\cos \lambda \cos \lambda}{\sin Z}$$
. $m + (\frac{\cos \lambda \cos \lambda}{\sin Z})^2 \cot Z \cdot n$
or $Z = z - \frac{\cos \lambda \cos \lambda}{\sin Z} (m - \frac{\cos \lambda \cos \lambda}{\sin Z}) \cot Z \cdot n$ nearly.

In the formula it is supposed that the latitude of the place and declination of the star, and consequently its zenith distance, are previously known; but in all cases where the latitude alone, or the declination alone, is known, z must be substituted for Z in the formula, and then the resulting reduction, which will not differ materially from the truth, when applied to s will give Z and a very nearly correct; after which, the operation pointed out by the formula, must be repeated with Z and λ as if they had been previously known. This repetition which, as appears by the following example, is easily performed, will give the reduction correct enough for all observations made near the meridian; but, if the horary distance be great, a second repetition may be necessary, though scarcely when the observations are kept within the extent of our table, and, unless from necessity, they should not be taken more distant, as in that case, a small error in the time will produce a considerable error in the senith distance. On this account observations very distant from the meridian are not to be recommended, as they may tend to vitiate those made near it.

```
λ 53° 23′ 13″ cos.
                                9.775544
   20
           28
                                9.972541
                COS.
  z 33 · 17
           15
                                0.260554 (a) cot.
                                                         0.182722
                cosec.
                               0.008739 \times 2 =
                                                         0.017478
  m 110.11 log
                               2.041787 n 0.045 log.
                                                         8.653213
                                     38\ 2d, cor. +.0713 8.853413
                                2.050564 (c)
1st, Cor. — 112".35 (e)
    or — 1' 52 .35
                                    380
2d. Cor. +
              0 .071
                                     134
            52 .279
     339 17
            14 .720
        15 22 .441
     33
Ref. +
             37 .775
              0.216(f) cosec. 0.260794(b)
     33 16
                                     240 (b-a)
                                2.050804 \{c+(b-a)\}
        -112.41 (d)
              0.06 (d-e)
                                     766
                                      38
```

z''' 33 16 0 .156 $\{f-(d-e)\}$ 38 This result scarcely differs from Dr Brinkley's, which is 33° 15′ 0″.17, to which the aggregate of precession, aberration, and nutation, amounting to -13''.53, being applied, gives 33° 15′ 46″.64 for the mean zenith distance on January 1, 1820.

Ex. 2.—At Maranham, August 28, 1822, Captain Sabine took the following observations of the star & Lyræ with a repeating circle of six inches in diameter, the barometer being 29th .95, the thermometer 80° Fahrenheit, the chronometer, No 423, fast 2th 55th 59th; the star, whose right ascension was 18th 30th 57th.4, was on the meridian, at 8th 4th 35th mean time, and at 11th 1th 34th by the chronometer.*

This example is extracted from Captain Sabine's work on the determination of the length of the seconds pendulum at various points of the earth's surface, lately published at the expense of the Board of Longitude. It is a work highly to be recommended, for perusal, to those likely to be employed in such experiments in future, as it contains valuable examples of all the requisite operations likely to occur in such researches.

Chronometer. Horary Angles	Reduction. P. I. P. II. Level.	Readings.
h. m. s. m. s. 10 49 6 12 28 10 49 40 8 54 10 52 50 5 44 10 55 44 3 50	64.54 0.01 _4 _ 6 2	First Vernier 167° 11′ 50″ Second . 11 30 Third . 12 10 Fourth . 11 40
11 0 49 0 45 11 3 42 2 8 11 6 52 5 18	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Mean 167 11 47 5 First Vernier 136° 35′ 0″ Second . 34 30
1	736.07 0.34 16.5	Third . 35 30 Fourth . 35 0
Means	92.01 0.0425	Mean . 136 35 0 Index + 192 48 12 .5 Level — 16 .5
# 41° 10′ 22′ Ther. 80 F. Bar. 29.95 Ther.	' log. 3# 1.70813 9.97367 9.99926 9.99870	8)329 22 56 Obs. Z D 41 10 22 + 47 .84 Cor 1 49 .01
of observa- our be ob- chies, taken	from a meah of a manner every near the truth. It latitude from Delamber's b	True Z D 41 9 20 .83 Star's dec. 38 37 37 .60
38 37 38 6	os. 9.999578 os. 9.892776 osec. 0.181555 (a) cot.	Latitude 2 31 43 .23
m 92".01 log.	$ \begin{array}{c} 0.073909 \times 2 = \\ 1.063835 & n, 0.0425 \end{array} $	0.147818 5 log. 8.628389
1st cor.—109".0 or — 1' 49 .0 2d cor. + 0 .0	08 426	Teles, Marches Bilds of the large to the lar
- 1 49 .0	1	

It is unnecessary to repeat the operation in this case, as the difference in the result would only be 0".04, making the latitude 2° 31' 43."19

TABLE XXIX .- Reduction to either Solstice, the Obliquity of the

Ecliptic being 23° 27' 40".

The obliquity of the ecliptic is determined by a number of meridian altitudes, or zenith distances near either solstice. If the sun's longitude were three or nine signs exactly at noon, the operation would be very simple; but as that seldom happens, it is necessary to reduce the actual observations to which they would have been under these circumstances. To accomplish this object, this table has been constructed. In the table the obliquity is supposed to be 23° 27′ 40″, and the reduction is the difference between this quantity and the sun's declination at the several points of the ecliptic corresponding to the observed right ascensions. With the differences and variation for 100" change of obliquity the table may be adapted to any time within the limits of the table's variation of obliquity. Both quantities will thus be additive till the year 1835. The table is extended to 30^m, and consequently observations may be reduced by it for about seven days before and as many after the solstice.

Ex. 1. On the 15th of June, 1826, the sun's declination was observed to be 23° 18′ 51″.7, when the right ascension was 5^h 25^m 51.4, and the obliquity 23° 27′ 39″, what was the reduction to the

solstice?

6 h	•	0 0 1]	Cabu Estir	ılar nate	obliq d obl	uity iqui	ty S	23°	27' 27	40' 39
	<i>52</i>	51.4		Exce							1
	27 27	0.0 8.6	= di gives gives var. c		•		8′	42	.73 .56	3 34	
		duction's de	on clim a t	ion	•	23°	8 2 8	48 51		99	

True obliquity . 23 27 39 .999

By operating in this way for several days near either solstice, the true obliquity may be obtained from a mean of a number of observations, and consequently likely very near the truth. It may be observed, however, that the sun's latitude from Delambre's tables, taken with a contrary sign, should be applied to the obliquity determined in this manner.

Es. 2.—I had commenced to determine the obliquity of the ecliptic from the totality of the Greenwich observations by Dr Maskelyne, and had proceeded so far when I was anticipated by Dr Brinkley. I used the French table of refractions, Delambre's table of reduction depending on the sun's longitude instead of the R. A., which, being rather more convenient in practice, is made the argument here. The longitude and latitude of the sun were computed from Delambre's Tables, and, as the methods are analogous, any one who can compute by the longitude can readily also use the right ascension, and the following example is given as an illustration of either.

2 2 3 4 d				1	96,73	5			,		
	Dec. year:	0.468	- 23		n 24"==57 12."96			٠.	1		<i>:</i>
- 10 m 14	Z	26	62		ion in 24	-14					
1765.	ßą.	16	186	1.01	.04 Mot.	••					•
ECLIPTIC, JUNE 1766.	田	375	354	15' 45".67	64 65 &					٠	
IPTIC,	Q.	37 246	286	meter	motion rallax		e. 13,′	52 	81 E	42	٠.
	၁	2019 704	276	. O's semidlimeter	Horary motion Hor. parallax	•	Longitud	888	30 - 33 0	4 64 60	
OF THE	Ä,	88	1	0			in's]	90.5	8	83	ije.
QUITY	• 3	. 3 .8	₩,	2	35		S June]	:-	• •	. e . e . s 	
	¥	\$ 3	. GB E	7.		:			,	ar organi Property	Y
CALCULATION DE DE	Perigee	0.0°0°0°0°0°0°0°0°0°0°0°0°0°0°0°0°0°0°0	9 8 63 25	2 29 54 36 "	5 21 1 13 or 5 21 1.2	s mean anom.		*.			
CALCUL	mgitude 🔾	0' 0'.3 21 50'.3 32 44 .4	3.1	38 .1	42 L 64 L 12 .		6 6 .8 .7		12 .2 5 .8	00	18.3
	Longit	9 0 0 9 11 21 5 18 32		2 29 54	++	++	++	+	3 0 12	- +	8 0 12 18
	Argum.	Sec. equa. 1765 June 21st	1m 15	Mean lon.	Equ. cen. Sec. var.	Lun. equ. B, C	ପ୍ରଥ ପ୍ରଥ	B, F	Lun. nu.	Sol. nu. Aberra.	O's T. lon. 3

App. Obliquity. 23°-28' 10''.9 17 .2 11 .6 17 .8 15 .5 16 .2	23 28 15 .9 23 28 7 .1 23 28 7 .1 23 28 7 .1 24 29 8 6 5. 25 28 7 .1 26 29 28 6 5. 27 20 1/1 less 28 20 N., or 1/1 less 28 20 N., or 1/1 less 29 .6 N.
Declination. 23° 23′ 33′.1 27′ 37′ :6 28′ 3 :9 28′ 17′ :2 27′ 55′ :2 27′ 55′ :2 27′ 55′ :2 27′ 55′ :2 27′ 55′ :2 27′ 55′ :2 27′ 55′ :2 27′ 55′ :2	In these examples the English baremister and Fahrenheit's themometer have been reduced to the French measures. This might have been avoided by using proper faqtors now usually given with the French tables. In this computation we have made the latitude of Greenwich Elevant I." or 14". The error of the line of Collimation has been applied to the French refractions, which amounts to +1". In Thomas Henderson has found the latitude of Greenwich, by Ivory's Refractions, to be still less from Mr Pond's late very accurate observations. If my estimation, 51°-28' 38'. 4, prove right, the obliquity would be 22' 38' 6'.
Reduction. 4, 43″.8 39 .6 7 .7 7 .7 1 8 .3 1 0 .2 2 8 .8	moter en re- en re- might Sles. settors bles. he latitude of: gree nearly ror of the line "J. Mr Tho fo be still les
# # # # # # # # # # # # # # # # # # #	ish bare i have be i. This proper from talk reach talk is we a ghe erruit to +1 tractions, a, 51°28
Reffe. 30	In these examples the English baremeter and Fahrenheit's themometer have been reduced to the French measures. This might have been avoided by using proper factors now usually given with the French tables. In this computation we have made the latitude. Dr. Maskelyne, and in this we agree to great by about 1" or 14". The error of renith diagrams, which amounts to +1".1. I of Greenwich, by Ivory's Refractions, 80 be observations. If my estimation, 51°28'38".4,
Cent. 18.38 17.22 17.52 17.50 19.58 19.77 19.30	e example the Frenchet's the Frenchet's the Frenchet mayorded ally given computs Maskelyn stences, wich, by wich, by ions. If n
Metr. 7508 7627 7627 7627 7627 7630 7690 7585 7610	In these exa and Fahrenhe duced to the I have been avo gow usually given than Dr Mask than Dr Mask too great by a renith diagan. of Greenwich, observations.
66.44.48.88.88.88.88.88.88.88.88.88.88.88.	ं ं 4 ं धं 4 ं धं 4 ं धं थं
Thermometer. 188	28288288288288288288288288288282828282
Ber. 289.57 (19.89.99) (19.89.99) (19.89.99) (19.89.99) (19.89.99) (19.89.99) (19.89.99) (19.89.99) (19.89.99) (19.89.99) (19.89.99) (19.89.99) (19.89.99)	2
# # # # # # # # # # # # # # # # # # #	Obs. June 16 19 20 21 22 23 23 24

TABLE XXX .- To change Mean Solar into Sidereal Time.

As a clock regulated by sidereal time is inclispensable in every observatory, it is necessary to convert solar into sidereal time in order to know by the clock when any phenomena, such as eclipses, occultations, &c., calculated in mean solar time should take place. This table is employed for that purpose, as will appear by the following example.

An immersion of Aquarii by the moon took place on January 5, 1824, at 3° 46° 56°, apparent solar time by the meridian of Greenwich; what will be the time by a sidereal clock which show 0 °0° when the point Aries is on the meridian, and her error that

day 36 .54 fast ?

In this case the clock would be a right-ascension clock; and if she went true would show the right ascension of the celestial bodies a they passed the meridian when observed by a transit instrument. Now on the 5th of January, 1824, the sun's right ascension at noon is 19^h 1^m 37.0, the same as would be shown by a clock truly regulated.

But as the clock was 36°.54 fast on that day this must be added to give the time shown by the clock, that is, she shows 19° 2° 13.54 at noon. As the immersion happened at 3° 46° 50° P. M. this must be converted into sidereal time, and added to the preceding to give the time shown by the clock, so that an astronomer may be prepared to observe it.

This operation may be accomplished by the table.

Time.	Acceler	ation.
3° 0° 0° 46 0 50		.5 69 .557 .138
3 46 50 Hence to the time show There must be added And		.264 19h 2m 13r.54 0 0 37 36 3 46 50 .00
Whence the time shows	will be .	22 49 40 80

TABLE XXXI.—To change Sidereal into Mean Solar Time. This table may be useful for finding the rate of a clock or chronometer. As the transit of a fixed star advances 3^m 55^s.908:daily on mean solar time, if the passage of a star be observed with a transit instrument each day for several successive days, or the disappearance of a star during several successive nights behind a fixed object, such as the vane of a steeple or the body of the steeple itself, nearly in the meridian, the position of the eye of the observer being also fixed, the rate of the clock becomes known on sidereal, and consequently, by this table, on mean solar time.

Required the retardation on 10⁴ 5⁵ 48^m 56⁵ of sidercal time?

For 10 days we have 04 5h 0m 00 48 0 56		100 mg/s			49.147	
1 5 48 56		• • • •	· 0	40	16.944 56.000	
Mean solar time	•	• :			39.756	

TABLE XXXII.—To convert Mean Time into Parts of the Equator.
This table may be useful for converting into degrees, &c. the hours, minutes, &c. shown by a clock or chronometer regulated according to mean time; and the method of using it will be readily understood from the examples to the two preceding tables, and that of Captain Kater's in the appendix.

TABLE XXXIII.—Lengths of circular Arcs.

The method of using this can be no difficulty to those acquainted with the preceding tables, as they are employed in a similar manner.

TABLES XXXIV., XXXV., XXXVI., XXXVII., XXXVIII., XXXIVII., XXXIV., XLI., and XLII. are abridged from a series of tables, by Mr Fallows, astronomer at the Cape of Good Hope, and were transmitted to the Admiralty, along with an approximate catalogue of stars which he had formed there, and are very convenient for finding at once the amount of the corrections for precession, aberration, and nutation for any given observation, both in right ascension and declination. In addition to these, however, another table must be computed annually. Since the tables are only given to every ten minutes of right ascension, proportional parts are added for every single minute as far as 6 indicated by the figure in the place of tens in the side column. If the odd minutes exceed 6, the proportional part must be taken at twice, or the complementary proportional part to the next minute of even tens, must be applied with a contrary sign when necessary.

To understand the method of applying these tables is premised

the following

```
Synopsis:—
                      =- 1.3362 sin. R. A. tan. dec. +3.0678 \stackrel{\text{Constants.}}{=} a
Table XXXIV.
       XXXV.
                      = 1.3500 sin. R.A. = p, and p \times sec. dec. = b
                      = 1.2390 cos. R.A. = q, and q \times sec. dec. <math>= c
       XXXVII. = + 0.6430 \cos R.A. = s, and s \times \tan . dec. = d
       XXXVIII. = 20.0436 cos. R.A. = annual precession = a'
                    = -20.2550 cos. R.A. = p', and p' \times \sin. dec. = b'
= +18.5800 sin. R.A. = q', and q' \times \sin. d.+r' = c'
       XXXIX.
       XL.
                     = + 8.0659 cos. dec. =
= - 9.6480 sin. R.A. = s'
       XLI.
       XLII.
                                                                             =d'
                                       sin. 2 sin. 2 🔾
   Annual Table, part 1st = t - \frac{31111}{3}
                                                <del>- 40</del>
                     part 2d = 0.93046 (cos. & -cos. 2 & +
                      \frac{2}{31} cos. 2 \odot)
```

where t is the time elapsed since the commencement of the year when the sun's mean R. A. is supposed to be 18^h 40^m.

Table of sines of sun's longitude at the time of culmination = B Table of cosines of the same \vdots = C. Then the whole correction in R. A. = A a + B b + C c + D d (1) in dec. = A a' + B b' + C c' + D d' (2)

Ex.-Required the corrections of Fomalhaut in right ascension and declination for July 20th, 1824, at the time of his passing the meridian of Greenwich, the R. A. of the star being 22h 48m, and declination 30° 33' South.

The sun's longitude for this time is 118° 12', of which the natural sine is .881 = B, and the cosine is .473 = E. A and D must be taken from an annual table, or computed from the formulæ given above for that purpose.

Then from table XXXIV., &c. take the proper numbers for the R. A. of the star, and complete the multiplications indicated by formula (1) the sum of the results will be the total correction in R. A., and those by formula (2) will be that in declination.

or elitticity to the electric and adjusting to	all out to come a	STATE GROUP	to boiling	T.MILE.
Thus Table XXXIV414 590	Balan	C	proAnie	D
207	.881 .418	.473— 1.178—	.901+ 3.312+	.112+ .616+ .061
244+ Constant . 3.068	.352 . 9 . 6	471 82 3	2.981	061
Prec. in R. A. 3.312	.367+ .556+	THE SELECT	2.984+ Tan. dec.	·068+
Nat. sec. dec.	.923+ 1.161	ner the to spoted.	e dhis cont chilify con	.590
LAVIE NEVISION NEW NEVISION OF SECTION OF SEC	923	Wicking pur	Res No. 11	040+
they are convenient and very fer any single cur.	92 55 1	ting the	the comp	anutiler scourase
med A man of them	1.071 + 2.984 + 0.040 +		Dept de	10, 40, Yan
rections in right ascension.	4.095+	=x+y+	the sun	of cor-

BESTERNEY OF THE STATE OF THE S No. of the Alan Alan William of the State of

Declination of 26 maggin ag = 0.03016 (M. 20 - one C = +

Perduct, or part his ______ res. ___ + 0.000 Long, moon's 0000, partitions. + 2.14

Nucleaco de Realisment II. Il in any and an angel and the series

terested as don't may the man applicable to the man applicable to applicable to the second to the se

may after in James with the wife and the party with a little and a second

9 0 00 cm

Annual precession for 22^h 48^m, table XXXVIII. is = 19".062.

	В	C	C	. A .	D
	-881 ± 19.264	.473+ 6.945+	.472 — 6.945 +	901 + 19.02	.112+ 2.981+
19 49 हैं खेर राज्या है जिस्	15.411 1.541 .019	2.778 .486 .021	2.778 .486 .021	17.156 019	0.298 30 6
ant to the state of the state o	16.971 - 2.716+	3.285	8.285	17.175—	.040+
sin. dec.	14.255 — .508 +			- 51. 196	r 913-44 + +4
(1)	7.127 .114		r ;		
	7.241 — 3.285 — 17.175 — 0.334 +	= x' = y' = z			;
2 1543	27".366—	= sum of	correction	ns in decli	nation.

And in this manner the total corrections for any number of stars may be readily computed. Commission of the Marketine

TABLES XLIII., XLIV., XLV., XLVI., XLVII., and XLVIII. are general for the same purpose as those above. By the former are computed more readily the corrections of a number of stars near one another than by the present, though they are convenient and very accurate for computing the corrections for any single star.

Ex.—Required the true apparent right accession and declination of Aquille on the 1st of January, 1828; the mean R. A. being 19^h 42^m 23.6 and declination 8^c 25′ 15′′ N.?

Lon. moon's node 7 1 54

1st, To find the Nutation in R. A. and Declination. R. A. of star 9 25 36

2 23 42 tab. XLIII. - 0'.97, 5 23° 42 tab. XLIII.+8'.72 Remainder 4 27 30 tab. XLIV. + 1.09, 7 27 30 tab. XLIV. +0.89 Sum + 0.12 nut. in dec.+9 .41

Declination 8° 25' tangent +0.018Product, or part first Long. moon's node, part second +9.14

Nutation in R. A. + 9.158 = 0.61

To find the Aberration in R. A. and declination.

ON IN SECTION	CONTRACTOR AND AND ASSESSED ASSESSED.	and the properties are
R. A. of star	r 9° 25° 36′	dalsi rang man panda
Sun's lon.	9 10 8	T
Ramaindar	0 15 28 Tab. XLVI.	19"79 30 4
Sum	7 5 44 Tab. XLVII	0.68
THE RESERVE AND ADDRESS OF THE PARTY AND ADDRE	AND THE PERSON OF THE PERSON OF THE PERSON OF	THE PERSON NAMED IN COLUMN
30 30 30		19 .40 log. 1.2878
Declination	of star 8° 25' secant	. 0.0047
Abometion i	n R.A. — 1°.3 = — 19″.51	log. 1.2925
Remainder	+ 3° - 3° 15° 28′ Tab. XI	LVI. +5".18
Sum	$+ 3^{\circ} = 3^{\circ} 15^{\circ} 28' \text{ Tab. XI} $ + 3 = 10 5 44 Tab. XI	VII. +0 .48
TENEDONE STORY	Company of the Personal of Little	2 32 March 40
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TABLE XLIX. contains the mean obliquity of the ecliptic for the beginning of the year, which I have determined from all the most accurate observations I could obtain, together with the annual and monthly diminutions for the purpose of computing it at any other time.

TABLES L. and LI. give the necessary corrections to determine the apparent obliquity at any given time, which will be easily applied, and the mode of application is obvious.

TABLES LII. and LIII. contain the Lunar and Solar Equations of the Equinoxes in time, which are sometimes more convenient than in space.

TABLE LIV. contains the mean right ascensions and declinations of a few of the principal fixed stars for 1828, together with their annual variations for reducing them to any other time required.

TABLE LV.—Decimal Numbers for each Day in the year. It is useful wherever the fraction of the year is wanted, as in reducing the places of stars, &c. to any given day in the year. This is accomplished by multiplying the annual variation by the number of

years and decimal for the given day. The result applied with its proper sign will give its mean place after the given time to which the corrections for precession, nutation, and aberration, being also applied with their proper signs, will give the apparent place at that time.

TABLE LVI.—The Right Ascension of the Sun.

This table is adapted to leap year, particularly the year 1828, and is only intended to enswer the purposes of instruction when no great degree of accuracy is required, and the Nautical Almanac not at hand.

In order to adapt it to common years, one-fourth of the difference between the given and preceding days is to be subtracted from the right ascension in the table for the first after leap year, one-half for the second after leap year, and three-fourths for the third; and in the months of January and February, the right ascension is to be taken for the day following that given.

This table may be employed in finding the apparent time by the altitude of a star, for finding the time of a star's transit when that is required, for obtaining the latitude by a meridian altitude, &c.

I. To find the Time of Transit.

Rule.—From the R. A. of the star, increased by 24° if necessary, subtract that of the sun; the remainder will be the approximate time of transit. To this time apply the longitude of the given place in time by addition or subtraction, according as it is mest or east; the result may be called the reduced time. To this reduced time compute the right ascension of the sun, which will be the sun's true R. A. at the time of transit. Now from the star's right ascension for the given time subtract the sun's true R. A.; the remainder will be the apparent time of transit.

II. To find the apparent time of rising and setting of a known star the latitude and longitude of the place, and the year and day

of the month, being known.

Rule.—Find the apparent time of the transit of the star by the preceding rule; then find half the time of the continuance of the star above the horizon, by the method shown in Problem VI. of Spherical Trigonometry in the Introduction, page 72 and 73, which, being applied to the time of transit by subtraction and addition, will give the apparent times of the rising and setting of the star respectively.*

TABLE LVII.—Declination of the Sun.

This table contains the sun's declination for the noon of each day, on the meridian of Greenwich for the year 1828, or leap year. By this table the declination, sufficiently correct for many purposes, may be found for other years. For the first year after leap year, take one-fourth of the difference between the declinations for the given

^{*} Mr Thomas Lynn has given, in his extensive collection of Nautical Tables, the times of transits of 60 principal stars for every day in the year, which, in many calculations, are very useful.

and preceding days, which is to be added to the declination for the given day, if at that time the declination is decreasing, but subtracted if increasing. In the second after leap year take the half, in the third take three-fourths of the difference, and apply this correction in the same manner as before; the result will be the declination required. And in the months of January and February the declination is to be taken for the day following that given.

TABLE LVIII.—The Equation of Time.

This table contains the equation of time for 1828, or leap year; and is to be found for any other year in the same manner as the de-

clination above explained.

Time, deduced from observations of the sun, is called apparent time, to which the equation of time, being applied according to its title in the table, gives mean time. Since a clock or chronometer is constructed upon the supposition of a uniform motion, this table will be useful for ascertaining the rate and error on mean solar time. Also, if a clock be regulated to mean solar time, the instant when the sun's meridian altitude ought to be observed to find the latitude, is known by applying the equation of time to 12h, with a contrary sign to that in the table. These applications will be more readily understood by consulting the article on finding the longitude by chronometers in the introduction.

TABLE LIX.—Correction of the Longitude by Chronometers. This table is on the same principles as that given by Rossel in the third volume of Biot's Astronomie Physique, only substituting for the natural numbers their logarithms, as being more convenient in

practice. Ex.—At Tongatabou, on the 6th April, 1793, at 19h 53m 311.44, the daily rate of a chronometer was + 5.24, with an original error of + 1^m 20.93. The ship sailed from Tongatabou, and arrived at Ballade harbour, on the 22d of April, when, by observation, the daily rate was + 8.56, and the error 1^h 24^m 23.71 fast for mean time.

Daily rate	at Tongatabou at Ballade	of the same relative to the same of the	+ 5.24 + 8.56
THE PARTY	Sum .	PART AND THE STATE OF	13.80

Half, or mean daily rate Difference of longitude between Tongatabou and Ballade by the 20° 24′ 34′ 20° 17′ 55 first daily rate of 5.24

Difference of longitude by the mean rate of 6.9 Difference easterly 6 39 E.

because the difference of longitude ought to be diminished. From these data, what is the correction of the observed longitude, on the 17th of April, at 7h 34m?

Correction of the longitude of Ballade for 16 days 6′ 39″=399″ log. Log. for 16 days, Table LIX., ar. co.

2,60097 7.86646 From 6th April to the 17th, or 11 days, log. Table LIX. 1.81954

3' 14' = 194" log. 2.28697 Correction

The correction of the longitude of the 17th gives the place of observation more easterly, because Ballade ought to be to the east of the position calculated by the daily rate determined at Tongatabou.

Since the first two logarithms are constant, the correction of the longitude for other days in the same run, is easily obtained by substituting for the last logarithm that from Table LIX. for the given number of days elapsed from the time at which the rate was originally determined, and in this manner ought all longitudes to be corrected in a long run, where the rate of the chronometer has experienced considerable alterations.

The same thing may be done without the table, as in the following example taken from Captain Hall's observations on the coast of South America:—

" San Blas, West Coast of Mexico."

"Corrections to be applied to chronometrical measurements of the longitude of places between Acapulco and San Blas."

"The rate of the chronometer, by which the differences of longitude was obtained, of places between Acapulco and San Blas, was

that determined at Acapulco, or ± 0.0 per diem."

"On arriving at San Blas, however, after an interval of 18 days from Acapulco, the rate was found to be +2.6 per day. It became necessary, therefore, to make a proportional allowance at intermediate places for the increase of rate, which increase may be taken as uniform during the interval. This is effected by computing the whole difference of longitude by the mean of the two rates ±0.0 and 2.6, namely 1.3, and taking the difference between this determination and that by the first rate, whence are obtained 351" for the accumulated error in longitude in 18 days' interval."

"Now the sum of a series of 18 terms in Arithmetical progression, having 1" for the first term, and 1" for the common difference, is 171, consequently $\frac{351"}{171} = 2".053$ nearly for the daily increase in the error of longitude, and this multiplied by the sum of the terms in the series before designed, according to the number of the days elapsed since the rate was first determined, will give the respective corrections in longitude, to be applied to those deduced by chronometer, with the Acapulco rate. Whence we get 2' 15", for an interval of 11 days, to be deducted from the longitude of Colima, west of Acapulco; and the correction for an interval of $15\frac{1}{2}$ days is 4'21", to be taken from the longitude of Cape Corrientes, west of Acapulco.

TABLE LX.—Latitudes and Longitudes of Places.

This table contains the latitudes and longitudes of a few of the principal places in the world, given with all the accuracy in my power. It also contains the time of high water at the times of new and full moon, and the depth of the water at spring and neap tides, which are necessary to find the time of high water at any particular place on a given day, as well as the depth of the water of any tide, and at any hour of the tide, which may sometimes be necessary. The height of the neap tides is seldom given in tide tables, though for these purposes the one should be given as well as the other.

Indeed, it were to be wished that officers of the Royal Navy, as well as others, should carefully mark all these circumstances; so

fourth differences. Then to the proportional part of the middle first difference, corrected by the equation of mean second difference, by Table XXVII. apply the correction of the third difference from Table LXVII. answering to the middle third difference, and the correction in Table LXVII. answering to the mean fourth difference, and the result will be the correct moon's place. These corrections must be made according to the following rules.

If the third difference be positive and the time from noon or midnight less than six hours, the correction is positive; but if greater than six hours, the correction is negative. If the third difference be

negative the rule must be reversed.

The equation of fourth difference has the same sign as the fourth

difference itself.

These tables and rules were given by Mr Henderson in the 38th No. of the London Journal of Science; but we have not room to examplify them here, though to those well acquainted with the application of the equation of second differences there will be little difficulty.

TABLE LXVIII. was drawn up by Captain Kater, and, being easy in its application, it will be found very convenient at sea, for which it is chiefly intended.

Ex.—On the 23d of June, 1826, in longitude 30° W., the following altitudes of the pole star were taken, the height of the eye being 20 feet; required the latitude?

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		39	0	•		0 40			
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M. T. G.	10	38	3		50	29	11		:
Eq. T.	_	1	37	Refract	ion —	•	48		٠.
App. T.	10	36	26 -	T. alt.	50	28	23	tang.	0.0835
Sun's R.A.	6	6	6	1st cor.	+	54	23	log. A"	1.7584
R. A. mer.	16	42	32	2d cor.	+	1	10	log.	1.8419
R. A. star	0	58	44		· _				12 14
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that a complete tide table, embracing all the necessary data, might at last be formed.

TABLES LXI. and LXII. serve to convert space into time and conversely, and their use is so easy to those acquainted with many of the foregoing tables that any farther explanation is unnecessary.

TABLE LXIII. contains a selection of useful numbers frequently wanted in calculation, which have their logarithms and arithmetical complements subjoined.

TABLES LXIV. and LXV. are given for the purpose of computing the time and height of high water, as well as its height at any particular time of the tide, at such places where the heights at spring and neap tides are known. It is to be hoped that our navy officers will be enjoined to give, not only the time and height at new and full moon, but also at the quarters, to furnish data for these tables.

Ex.—Required the time and depth of high water at Leith, on the 12th of December, 1826; and also the depth 2^h before or after high water, or about 4^h from the nearest low water?

As the time of high water would be that on the following morning, half the sum of the transits on the preceding and given days must be taken, thus:

Moon's transit on the 11th	10 ^h 3 ^m 3
Mean 19 00 00. 0 00 00 Equation to 3° west longitude . 10 00 .	10 27 + 1
Reduced transit Time of high water at new and full moon Equation, Table LXIV.	10 28 2 20 + 10
True time Or 58 ^m , part noon of the 12th.	12 58

To transit 10^{b} 27^{m} and parallax 54' (Table LXV.) in which a is the height of the spring tide, and b that of the neap, the multipliers respectively are $0.676 \ a = 0.676 \times 16 = 10.816$ feet and $0.176 \ b = 0.176 \times 8 = 1.408$ feet

Total height in feet = 12.224

Now, with the time 2^h after the nearest high water, the multiplier in the right-hand part of the table is 0.779. This multiplied by 12.224 gives 9.5 feet at that time of the tide.

TABLES LXVI. and LXVII. contain the equation of third and fourth differences, which must be applied in order to obtain the moon's apparent place with great accuracy, especially in occultations, in determining the longitude by the moon's transit over the meridian, &c. They are used in the following manner:—Take out of the Nautical Almanac the three right ascensions, &c. preceding, and the three following the given time, and deduce their first, second, third, and fourth differences, also the mean of the two second differences standing on each side of the given time, and the mean of the two

fourth differences. Then to the proportional part of the middle first difference, corrected by the equation of mean second difference, by Table XXVII. apply the correction of the third difference from Table LXVI. answering to the middle third difference, and the cor-rection in Table LXVII. answering to the mean fourth difference, and the result will be the correct moon's place. These corrections must be made according to the following rules.

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M. T. G.	10	38	3		50	29	11	:	2.4
Eq. T.		1	37	Refracti	on —		48		
App. T.			26	T. alt.	50	28	23	tang.	0.0835
Sun's R.A.	6	6	6	1st cor.	. +.	54	23	log. A"	1.7584
R. A. mer.	16	42	32	2d cor.	- +	1	10	log.	1.8419
R. A. star	0	58	44	•	` <u>-</u>				- 14-117-
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Moon's transit on the 11th Sabul and off background 12 and	10 ^h 3 ^m 10
Mean 19 00 00. O 08 Equation to 3° west longitude . A 00 .	10 27 + 1
Reduced transit Time of high water at new and full moon Equation, Table LXIV.	10 28 2 20 + 10
True time	12 58

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Mean 102 0b 0d. 0 00 00 00 00 00 00 00 00 00 00 00 00	10 27 + 1
Reduced transit Time of high water at new and full moon Equation, Table LXIV.	10 28 2 20 + 10
True time 84 . — manager A . 18 1 . —	12 58

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App. T.	10	36	26		50)	28	23	tang.	0.0835
Slin's R.A.	6	6	6	1st co	r +		54	23	log. A'	1.7584
R. A. mer.	16	42	32	2d cor		•	1	10	log.	1,8419
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APPENDIX.

On the Minute Corrections of Lunar Distances.

In lunar observations the corrections for the spheroidal figure of the earth have been applied according to the method of Professor Lax of Cambridge, Dr Inman of Portsmouth, Mr Riddle of Greenwich, &c. by diminishing the equatoreal horizontal parallax by the reduction for the latitude; but unless the latitude and altitudes are in like manner reduced, which leads to a complex calculation, the results are still inexact. The method here proposed is similar to that of Mendoza Rios, requiring only a small table to facilitate its application. The table has been computed by my ingenious friend,

Mr Thomas Henderson, for an ellipticity of $\frac{1}{300}$, which seems to

agree well with the latest measures, and to the mean horizontal parallax 57', which is sufficiently accurate for practical purposes, as the greatest error can hardly exceed 1", and at a mean not above half that quantity. This is within the limits of uncertainty arising

from an error in the ellipticity, which seems to vary between and

 $\frac{1}{305}$ even from the best measures, the mean between which, $\frac{1}{300}$

has been here adopted. No doubt such refinements are unnecessary in the usual sea practice; but as the lunar method, which is still capable of improvement, can be practised with great success at land, it was thought necessary to correct an erroneous rule, which I believe has been generally acted upon. For illustration we shall give Example 4th, page 97 of the introduction, corrected in this manner as explained by Mr Henderson in the 40th No. of the London Journal of Science.

Rule.—When computing the parallax in altitude; to the logarithm of the earth's radius (Table XXIII.) add the secant of the moon's apparent altitude, and the proportional logarithm of the moon's equatoreal horizontal parallax, the sum of these will be the proportional logarithm of the moon's parallax in altitude to be employed in computing the true distance. Now from half the sum of the moon's polar distance, the sun's or star's polar distances, and the distance of the moon from the sun or star, subtract the moon's polar distance, and the distance from the sun or star respectively. Then to the constant logarithm 0.30103, add the cosecant of the moon's distance from the sun or star, the sines of the two remainders, and the logarithm of the number from the table (I.) here given; the sum of these is the logarithm of the number of seconds to be always subtracted from the computed distance, while the number from the table itself is always to be added to it to give the true distance on

the hypothesis of the earth being a spheroid of $\frac{1}{300}$ of ellipticity.

Ex. 1.—Latitude Moon's alt. Hor. par.		0" S. log. radi 0 secant 14 P. log.	ius .	9.99900 0.07190 0.49010
Par. in alt.	. 49 2	28 P. L.	•	0.56100
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Corrected altitude	• **	•		33 3 31
Observed distance Moon's aug. semidian Gerrection for oblique	neter e semidiam	eter	•	61 56 30 + 16 1.
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tude and the moon's cusual, which in this which the corrections by the foregoing rule Moon's polar dist. Star's polar distance	corrected a example, we for the sp., must be a 68° 59′ 59 28	ltitude, compu- ill be found to heroidal figure applied.	te the true be 62° 1	distance as 6' 17 g'', to h, obtained 0.05320 0.30106
tude and the moon's usual, which in this which the corrections by the foregoing rule Moon's polar dist. Star's polar distance Apparent distance	corrected a example, we for the sp. , must be a 68° 59' 59 28 62 13 190 40 95 20 26 21 33 7	ltitude, compu- ill be found to heroidal figure applied. cosecant	te the true be 62° 1	distance as 6' 17\forall', to h, obtained 0.05320 0.30108 9.64724 9.73747 1.27646
tude and the moon's usual, which in this which the corrections by the foregoing rule Moon's polar dist. Star's polar distance Apparent distance Sum Half First remainder Second remainder Number from Table I.	corrected a example, we for the sp. , must be a 68° 59' 59 28 62 13 190 40 95 20 26 21 33 7	ltitude, compuill be found to heroidal figure applied. cosecant const. log. sine sine	te the true be 62° 1	distance as 6' 17\forall', to h, obtained 0.05320 0.30108 9.64724 9.73747

Confine the polyment of

of his section have Tellinery employed to Service of service of of real enterpolar teem surfaces.

Site of the state of	1 ^h 29 ^m 34 ^s 12
Equation of sec. diff.	13 29 34 - 11
App. Greenwich time App. ship time	13 29 23 7 1 6

Long. in time . 6 28 17 = 97° 4' 15" W.

The earth being a sphere, it is = 97 12 30

According to Lax's method = 97 13 30

So that the error on the spherical hypothesis, without allowing for the equation of second difference in three hours, is +8'15' By Lax's method it is +9 15

Ex. 2.—On the 28th of August, 1823, on the east coast of Greenland, in latitude 74° 32′ 19″ N., longitude 18° 40′ W., Captain Sabine observed the distance of the sun and moon's limbs to be 100° 39′ 4″, the apparent altitude of the moon's centre 29° 54′ 48″, the sun's 19° 52′ 34″; the barometer 30.03; the thermometer 39°.4; and the apparent time at the place of observation 20° 44° 35°. Required the true longitude?

Calculating on the foregoing principles, Mr Henderson has found the apparent central distance to be 101° 15′ 5″, and the true distance came out to be

100° 47′ 25″
Captain Sabine makes it

100° 47′ 33′

The apparent time at Greenwich, corrected for the equation of second difference to the true distance 100° 47′ 25″ is 21^h 59^m 45^s Time at the place of observation, 20 44 35

If the true distance be calculated by diminishing the equatoreal horizontal parallax only, as directed by some authors, the true distance becomes 100° 47′ 29″, but allowing it to remain uncorrected for the latitude, the distance is 100° 47′ 24″. In general the correction of lunar distances for the earth's ellipticity, is small, seldom amounting to 10″ of distance or 5′ of longitude, in any case that can occur in practice; and in any place within the tropics, the results on the spherical hypothesis, may be considered almost perfectly correct. On this subject Mr Henderson has remarked to me, that " the

On this subject Mr Henderson has remarked to me, that "the method prescribed by most authors, of allowing for the effects of the earth's spheroidal figure upon the lunar distances, by diminishing the equatoreal parallax, is not altogether exact, but leaves an error uncorrected, which, at its maximum under any particular latitude, is nearly one-sixtieth of the reduction of latitude, or angle of the vertical with the radius. The greatest error therefore which can possibly happen in any part of the globe, is under the parallel of 45°, where it may amount to 12". Under the equator and poles the error is nothing.

"If the equatoreal parallax be employed in the computation of the true distance, the result is liable to a greater error. The maximum error under any particular latitude, may be expressed by the hypothenuse of a right-angled plane triangle, in which one side is equal to the sixtieth part of the reduction of latitude, and the other to the correction of the equatorial partillax. Under the parallel of London, the maximum error is 14"."

When this work was nearly ready for publication, the author learned that Captain Kater, whose skill and experience as an able practical man command the utmost respect, was in the habit of using the direct method of obtaining the latitude by the pole star, as much shorter and simpler than by the use of tables, and upon application being made by a friend, who has interested himself in the success of this work, Captain Kater was so obliging as to ferward to the author, the following example computed by the tables in this volume, which had been submitted to his inspection in their progress through the press. Captain Kater transmitted, at the same time, a small table containing the tangents and secants to every 10" of the polar distance of polarls, which will answer for some years to come, and will be found to save the computer some trouble.

to save the computer some trouble. The solution depends upon the following formulæ:— Tan. $u = \tan p \times \cos t$ (A.) cos. u × cos. z = cos. u × cos. z × sec. p. Cos. (4-4)= cos. p "At York Gate, Regent's Park, London, on the 29d of Kebruary, 1826, at 7 42 49, mean time, the altitude of the pole star was observed by Captain Kater to be 51° 58' 11"; required the latitude? First to find the mean solar time when the star was upon the meridian. *s App. R. A. 0_p 58^m 15.2 App. alt. 51° 58′ 11″ O's R. A. at noon, 21 22 18.3 Refrac. 45.4 36 **56.9** True alt. 51 *57* **25.6** Difference from Table XXXI. 25.7 2 34.4 = 3836 31.2 13 Equation of time for noon, 50.7 * Upon the Meridian, 50 21.9 Time of Observation, 42 49.0 $= 73^{\circ} 18' 47'' = t$ by Distance of Star from the **52 27**. 1 Table XXXII. Meridian in mean time, $p=1^{\circ} 36' 48''$. tan. 8.449716 cos. co. ar. 0.000172 $t = 73 18 47 \cos$ 9.458097 7.907813 cosine 9.999986 u=027 48 .2 †tan. 8° 2' 34.4" 9.896278 cosine -×)=38 **58 .2** cosine 9.896436 -38 28 46 .4 31 13 .6

⁺ Found by precept, page 10 of Explanation of the Tables."

Were the author permitted to add any thing to what Captain Kater approves, it would be to employ the constant log. 5.314425, the log. of an are=R'', Table LXIII. and the sum of these logs. would be the log. u in seconds, which would save the trouble of finding the value of the log. tangent of small arcs.

To those not very familiar with such Computations it may be useful to show the Manner of Calculation.

As a rule in words at length might be serviceable in the solution of this problem, to those who are little conversant with formulæ, it has been added.

To the constant log. 5.314425, add the log. tangent of the star's polar distance p, and the log. cosine of the meridian distance t, in degrees, the sum of these will be the log. of the arc u in seconds. Now, to the log. secant p add the log. cosine u, and the cosine of the zenith distance z, the sum will be the cosine of $(\psi \pm u)$, an arc which, being increased or diminished by the arc u, will be the colatitude ψ , whence the latitude λ is readily obtained.

Constant logarithm, p= 1° 36′ 48″ tangent, t=73 18 47 cosine,	12/10	5.314425 604 8.449117 9.458097	secant,	0.000172
u= 0 27 48.2=1668".2 -		3.222243		9.999986 9.896278
(ψ—u)=38 0 58.2 .	1 13	5 de 22	cosine,	9.896436
ψ =38 28 46.4 =51 31 13.6	松かし		AT US	10 07 20 05

In the application of u, attention must be paid to the sign of the arc t, according to its situation in the circle which the star describes round the pole, in its diurnal revolution. If t is in the first or fourth quadrant, it is additive; but if in the second or third, it is subtractive.

PERSONAL AND PURE PROPERTY OF SECTION 1.00 1719 11.10 TOTAL SECTION IN STATES IN SEPTEMBER OF SE 241 EAR (421 (211) 21 8411 0.41 (41) 88 Carlings on other art new OR TAILERING IN A PROPERTY BO TAPEN CONTRACTOR OF THE PARTY O THE BUILDING White the first attack by the Role disco-Try Caresaw Water MARKET NO. Brownston TOWNS Y - TERRES OF STREET OF THE ACTION OF THE STREET OF THE NO HARDWAY THE LAND OF THE OWNER. Salansal = 10 Cocoolar 400-(Aaddeut) OEI THEOGRAPHICAL PROPERTY OF COMMONSTREE PARTIES OF on all layers - Region (pa) CHEROLOGIC -APTHOO IN THE PROPERTY OF Sellonie Ske a proposa son OTTOGODOW - V STANDAR OL OTHER SOURCE OF STREET FB100000/810000 TYTOOONTO - O'MONTH! SHOULD BE Dennike in squ 0,000179

TABLE I.

Corrections for Mean Horizontal Parallax, to be added to the Lunar Distances on account of the Spheroidal Figure of the Earth, its Ellipticity being 1850.

By MR HENDERSON.

La t.	L.	Mo	on's	Dec	linati	ion,		Lat.		M	oon's	Dec	linati	on.	
	ő	5	io	15	20	25	30	4	0-	5	10	15	20	25	30
00	00	0.0	í.	"	00	".	00	469	104	100	101	150	"	14.0	"
2	0.0	0.0	100 100	0.0	0.0	0.00	1000	48					$15.4 \\ 15.9$		
4	1.6	1.6	1000		1.5		1.4	50					16.4		
6	2.4	2.4					2.1	52					16.9		
8	3.2	3.2			3.0	2.9		54					17.3		
10	4.0	3.9			3.7	3.6	3.4	56					17.8		
12	4.7	4.7	4.7	4.6	4.4	_	4.1	58		_	-	_	18.2	-	
14	5.5	5.5	5.4	5.3	5.2		4.8	60					18.6		
16	6.3	6.2	6.2	6.1	5.9		5.4	62					18.9		
18	7.0	7.0	6.9	6.8	6.6	6.4	6.1	64					19.3		
20	7.8	7.8	7.7	7.	7.3	7.1	6.7	66	20.8	20.8	20.5	20.1	19.6	18.9	18
22	8.5	8.5	8.4	8.2	8.0	7.7	7.4	. 68	21.2	21.1	20.9	20.5	19.9	19.2	18
24	9.3	9.2	9.1	8.9	8.7	8.4	8.0	70	21.5	21.4	21.1	20.7	20.2	19.5	18
26	10.0	10.0	9.8	9.7	9.4	9.1	8.7	72					20.4		
28	10.7						9.3	74					20.6		
30	11.4	11.3	11.2	11.0	10.7	10.3	9.9	76	22.1	22.1	21.8	21.4	20.8	20.1	19
32	12.1	12.0	11.9	11.7	11.4	11.0	10.5	78	22.3	22.3	22.0	21.6	21.0	20.2	19.
34	12.7	12.7	12.5	12.3	12.0	11.5	11.0	80	22.5	22.4	22.1	21.7	21.1	20.4	19
36	13.4							82					21.2		
38	14.0							84					21.3		
40	14.7	14.6	14.4	14.2	13.8	13.3	12.7	86		1	and the same of	STATE OF THE PARTY.	21.4		
42	15.3	15.2	15.0	14.7	14.3	13.8	13.2	88	22.7	22.6	22.4	22.0	21.4	20.6	19.
44	15.8	15.8	15.6	15.3	14.9	14-3	13.7	90	22.8	22.7	22.5	22.1	21.5	20.7	19.

TABLE II.

For Finding the Latitude by the Pole Star .- By CAPTAIN KATER.

D	Polar istance.	Tangent.	P. P. +	Cosine Co. Ar. or Secant.	Polar Distance	Tangent-	P. P. +	Cosine Co. Ar. or Secant.
10	33' 0"	8.432315		0.000159	1° 35′ 0′′	8.441560		0.000166
	10	8.433093	1"= 77	0.000159	10	8.442322	1"= 75	0.000166
	20	8.433870	2 = 154	0.000160	20	8.443082	2 = 151	0.000167
	30	8.434645	3 = 231	0.000161	30	8.443841	2 = 226	0.000168
	40	8.435419	4 = 308	0.000161	40	8.444599	4 = 302	0.000168
	50	8.436191	5 = 385	0.000162	50	8.445355	5 = 377	0.000169
[a	34' 0"	8.436962	6 = 462	0.000162	19 36' 0"	8.446110	6 = 453	0.000169
	10	8.437732	7 = 539	0.000163	10	8.446864	7 = 528	0.000170
	20	8.438500	= 616	0.000163	20	8.447616	8 = 604	0.000170
	30	8.439267	=693	0.000164	30	8.448368	9 = 679	0.000171
	40	8,440033	(- 1	0.000165	40	8.449117	100	0.000172
	50	8.440797		0.000165	50	8.440866		0.000179

ERRATA AND ADDITIONS.

INTRODUCTION.

For H = 799.32 feet, read H = 801.16 feet. Defect, for 3.34 feet, read

HOVE DAY ONCE

Second line from the top, for his assistant, read an officer of the Griper who assisted him in making the observations.

For sum, read sun, in the fifth line from the top. For -3' 27".02, read -2' 27".02, in the third line from bottom. 84

88

For Dip section, read dip sector.
For 67° 12' 12", read 67° 18' 12", line 20.
Table IV. to var. 1° 38' and 2" of second difference, for 2.7, read 3".7. 102

For a Leonis, read A Leonis, 116

For z, from Parry's last Journal, I suspect a Geminorum must be read. 119

For sun's dec. 22° 35′ 40″, read 22° 35′ 45″, on account of having applied the equation of second difference with a wrong sign. Long. 9" 55° W. 126

128 For 18° 1′ 0".0, read 18h 1m 0a.0.

159 Ex. 2. Captain Hall reduced both his experiments to 68° F., and therefore my correction is erroneous; it may, however, serve as an example of the manner in which such a correction should be made.

For cos 2 L., read cos 2 L.

EXPLANATION.

Example for reduction of altitude is wrong, but may be easily corrected by the rule.

Line 11, for 4° 65' 14".4, read 4° 56' 14".4. 21

For 33° 15' 0".17, read 33° 16' 0".17, in 11th line from the bottom.

For 23° 28' 51".7, read 23° 18' 51".7.

In the tables not stereotyped there are two or three errors.

Table XLIV., for R. A. Star-Lon. Moon's Node, read + 101

Table L., for Moon's true Long. read Sun's.

\$ 40 CON BE 1000

THE RESIDENCE AND ADDRESS OF THE PARTY OF TH

104 Declination Fomalhaut, for 30° 34' 24", read 30° 31' 54". Appendix to Explanation of the Tables, page 39, line 3d from bottom, for 92° 26' 26", read 62° 26' 26".

TABLE XXXII.

To convert Mean Time into Parts of the Equator.

TAB. XXXIII. 97 Lengths of Circular Arcs.

Mean Time.	Parts of the Equator.	Mean Time.	Parts of the Equator.	Mean Time.	Parts of the Equator.		Arc.
h.	0 1 11	m.	0 / "	В.	, "		
1	15 2 27.847	1	0 15 2.464	1	0 15.041	10	0.01745329
2	30 4 55.694	2	0 30 4.928	2	0 30.082	2	0.03490659
3	45 7 23.541	3	0 45 7.392	3	0 45.123	3	0.05235988
4	60 9 51.388	4	1 0 9.856	4	1 0.164	4	0.06981317
5	75 12 19.235	5	1 15 12.321	5	1 15.205	5	0.08726646
6	90 14 47.081	6	1 30 14.785	6	1 30.246	6	0.10471976
7	105 17 14.928	7	1 45 17.249	7	1 45.287	7	0.1221730
8	120 19 42.775	8	2 0 19.713	8	2 0.328	8	0.1396263
9	135 22 10.622	9	2 15 22.177	9	2 15.369	9	0.15707963
10	150 24 38.469	10.	2 30 24.641	10	2 30.411	10	0.17453293
11	165 27 6.316	11	2 45 27.105	11	2 45.452	20	0.3490658
12	180 29 34.163	12	3 0 29.569	12	3 0.493	30	0.5235987
13	195 32 2.010	13	3 15 32.033	13	3 15.534	40	0.69813170
14	210 34 29.857	14	3 30 34.497	14	3 30.575	50	0.8726646
15	225 36 57.703	15	3 45 36.962	15	3 45.616	60	1.0471975
16	240 39 25.550	16	4 0 39.426	16	4 0.657	70	1.2217304
17	255 41 53.397	17	4 15 41.890	17	4 15.698	80	1.3962634
18	270 44 21.244	18	4 30 44.354	18	4 30.739	90	1.5707963
19	285 46 49.091	19	4 45 46.818	19	4 45.780	100	1.7453292
20	300 49 16.938	50	5 0 49.282	20	5 0.821	110	1.9198621
21		21		-		120	
22	315 51 44.784 330 54 12.631	22	5 15 51.746	21	5 15.862	130	2.0943951
23		23	5 30 54.210	22	5 30.903		2.2689280
24		24	5 45 56.674	23	5 45.944	140	2.4434609
44	360 59 8.325	25	6 0 59.138	24	6 0.985	150	2.6179938
_		_	6 16 1.603	25	6 16.027	160	2.7925268
		26	6 31 4.067	26	6 31.068	170	2.9670597
Decimals	Parts of the	27	6 46 6.531	27	6 46.109	180	3.1415926
of Mean	Equator.	28	7 1 8.995	28	7 1.150	210	3.6651914
Time.	and annual.	29	7 16 11.459	29	7 16.191	240	4,1887902
		30	7 31 13.923	30	7 31.232	270	4.7123889
8.	"	31	7 46 16.387	31	7 46.273	1'	0 0002908
0.1	1.504	32	8 1 18.851	32	8 1.314	2	0.0005817
0.2	3.008	33	8 16 21.315	33	8 16.355	3	0 0008726
0.3	4.512	34	8 31 23.779	34	8 31.396	4	0.0011635
0.4	6.016	35	8 46 26.244	35	8 46.437	5	0.0014544
0.5	7.521	36	9 1 28.708	36	9 1.478	6	0.0017453
0.6	9.025	37	9 16 31.172	37	9 16.519	7	0.0020362
0.7	10.529	38	9 31 33.636	38	9 31.560	8	0.0023271
0.8	12.033	39	9 46 36.100	39	9 46.601	9	0.0026179
0.9	13.537	40	10 1 38.565	40	10 1.643	10	0.0029088
8.	"	41	10 16 41.029	41	10 16.684	20	0.0058177
0.01	0.150	42	10 31 43.493	42	10 31.725	30	0.0087266
0.02	0.301	43	10 46 45.957	43	10 46.766	40	0.0116355
0.03	0.451	44	11 1 48.421	44	11 1.807	50	0.0145444
0.04	0.602	45	11 16 50.885	4.5	11 16.848	60	0.0174532
0.05	0.752	46	11 31 53.349	46	11 31.889	1"	0.0000048
0.06	0.903	47	11 46 55.813	47	11 46.930	2	0.0000097
0.07	1.053	48	12 1 58.277	48	12 1.971	3	0.0000031
0.08	1.203	49	12 17 0.741	49	12 17.012	4	0.0000143
0.09	1.354	50	12 32 3.206	50	12 32.053	5	0.0000212
s.	"	51	12 47 5.670	51	12 47.094	6	0.0000390
0.001	0.015	52	10 0 0 104	6.0			2 222222
0.003	0.030	53	13 17 10.598	53	13 2.135	8	0.0000339
0.003	0.045	51	13 32 13.062	54		9	0.0000387
0.001	0.060	55	13 47 15.526		13 32.217 13 47.259		0.0000436
		-	the same of the sa	55		10	
0.005	0.075	56	14 2 17.990	56	14 2.300	20	0.0000969
0.006	0.090	57	14 17 20.454	57	14 17.341	30	0.0001454
0.007	0.105	58	14 32 22.918	58	14 32.382	40	0.0001939
0.008	0.120 0.135	59 60	14 47 25.382 15 2 27.847	59 60	14 47.423 15 2.464	50	0.0002124
						60	0.0002908

Annual Precession of a Star in R. A. in Time.

Argument, R. A. of the Star in Time.

S.	100	+	-	to	1	to	-	mt)		(total	-	+	S.
	Op	12h	1h	13h	2h	14h	3h	15h	4h	16h	5h	17h	
N.	+		+	15	+	1		-	+	100	SI THE	1	N.
P. P.	m.	8.	P. P.	S.	P. P.	S.	P. P.	5.	P. P.	S.	P. P.	S.	m.
+	0	0.000	+	0.346	Wat a	0.668	11 + 1	0.945	+	1.157	estant.	1.291	60
6	10	0.058	5	0.402	5	0.718	3	0.985	2	1.185	1	1.305	50
12	20	0.117	11	0.457	9	0.766	7	1.024	4	1.211	-1	1.316	40
17	30	0.174	16	0.511	14	0.813	10	1.060	6	1.235	2	1.325	30
23	40	0.232	22	0.565	18	0.859	14	1.095	8	1.256	2	1.331	20
29	50	0.289	27	0.617	23	0.903	17	1.127	п	1.274	3	1.335	10
35	60	0.346	32	0.668	28	0.945	21	1.157	13	1.291	4	1.336	0
N.	4	-	+	-	+	_	+	-	+	-	+	7-5	IN.
100	11h	23h	10h	22h	9h	21h	gh	20h	7h	19h	6h	18h	100
S.	-	+	-	+	-	+		+	-	+	-	+	S.

Multiply the number found from the Table, with its proper sign, by the natural tangent of the Star's declination, to which add the constant quantity $3^4.068$ for the annual precession, = a in the Synopsis.

TABLE XXXV.

THE OWNER OF THE PARTY OF THE

Argument, R. A. of the Star in Time.

-	do	12h	46	+		+	Sh	+	4h	+	5h	17h	9
100	Op	13"	14h	13h	2h	14h		15h	All Control	16h	On	144	10.
P. P.	m.	S.	P. P.	S.	P. P.	8.	P. P.	S.	P. P.	S.	P. P.	5.	m.
+	0	0.000	111	0.349	11143	0.675	7.5	0.954	2373	1.168	NOTE:	1.304	60
6	10	0.059	5	0.406	5	0.725	3	0.995	2	1.197	1	1.318	50
12	20	0.118	11	0.462	90	0.774	7	1.034	4	1.222	2	1.329	40
18	30	0.176	16	0.516	14	0.821	10	1.071	7	1.247	2	1.339	30
24	40	0.234	22	0.571	19	0.868	14	1.106	9	1.269	3	1.345	20
30	50	0.292	27	0.623	24	0.912	17	1.138	11	1.287	4	1.349	10
36	60	0.349	33	0.675	28	0.954	21	1.168	13	1.304	5	1.350	20
1211	11h	23h	10h	22h	9h	21h	Sh	20h	7h	19h	6h	18h	
22.6	-	+	-	+	-	+	-	+	-	+ 11	-	+	

The number from the Table = p, and $p \times \sec$ dec. = b.

TABLE XXXVI.

Argument, R. A. of the Star in Time.

-	200100				100	
1	0h 12h	1h 13h	2h 14h	3h 15h	4h 16h	5h 17h
P. P.		P. P. s.	P. P. s.	P. P. s.	P. P. s.	P. P. s. m.
0	0 1.239	2 1.181	3 1.045	4 0.837	- 0.619 5 0.572	5 0.268 50
0	20 1.234	4 1.164	7 1.015	9 0.796	10 0.523	11 0.215 40
11	30 1.228 40 1.220	6 1.144 8 1.123	10 0.983	13 0.755 18 0.710	20 0.424	16 0.162 30 22 0.108 20
1	50 1 209	10 1.099	17 0.913	22 0.666	25 0.373	27 0.054 10
1	60 1.196	13 1.073	20 0.876	26 0.619	30 0.321	32 0.000 0
1	11h 23h + —	10h 22h	9h 21h	8µ 50p	7h 19h	6h 18h
-		A STATE OF THE PARTY OF	THE PERSON NAMED IN	A SHE WAS ARREST.	SHOW THE RESERVE TO SHOW	Compression Sections nor

The number from the Table = q, and $q \times \sec$ dec. = c.

Argument, R. A. of the Star in Time	Argument.	R.	A. of	the	Star	in	Time.
-------------------------------------	-----------	----	-------	-----	------	----	-------

S. N.	0h	12h	1h	13h	2h	14h	3h	15h	+ 4h	16h +	+ 5h	17h	S.
P. P.	m.	s.	P. P.	8.	P. P.	S.	P. P.	8.	P. P.	8.	P. P.	S. 0.100	m.
0	10	0.643	1	0.621	2	0.557	2	0.435	3	0.322	3	0.166	60 50
1	20 30	0.641	2 3	0.604 0.594	6	0.527	5 7	0.413	5 8	0.272	6 8	0.112	40 30
2	40	0.633	4	0.583	8	0.493	9	0.369	10	0.220	11	0.056	20
3	50 60	0.628	7	0.571	15	0.474	11	0.346 0.322	13	$0.193 \\ 0.166$	14	0.000	10
N.	+ 11h	- 23h	+ 10h	22h	+ gh	21h	+ gh	20h	+ 7h	19h	+ 6h	- 18h	N.
S.	=	+	_	+	-	+	_	+	-	+	-	+	S.

The number from the Table gives s, and $s \times \text{tang. dec.} = d$.

TABLE XXXVIII.

Annual Precession of a Star in N. P. D.

Argument,	R.	A.	of	the	Star	in	Time.
-----------	----	----	----	-----	------	----	-------

S. I	_	+	-	+	-	+	-	+	-	+ 1	1	+	S.
6	OF	12h	1h	13h	2h	14h	3h	15h	4h	16h	5h	17h	~
N.	+	-	+	_	+		+	-	+	-	+	-	N.
P. P.	m.	"	P. P.	"	m.								
-	0	20.044	-	19.361	-	17.358	-	14,173	-	10.022	-	5.188	60
13	10	20.025	35	19.116	55	16.904	70	13.542	81	9.255	87	4.338	50
27	20	19.968	71	18.835	110	16.419	140	12.884	162	8.471	174	3.481	40
40	30	19.872	106	18.518	164	15.902	210	12.202	243	7.670	261	2.616	30
53	40	19.739	141	18.165	219	15.354	280	11.497	324	6.855	348	1.747	20
66	50	19.569	176	17.779	274	14.778	350	10.769	405	6.027	435	0.874	10
80	60	19.361	212	17.358	329	14.173	420	10.022	486	5.188	255	0 000	0
N.	-	+	-	+	-	+	-	+	_	+	_	+	N.
0.03	11h	23h	10h	55µ	9h	21h	gh	200	7h	19h	(h	18h	1
S.	+	_	+	_	+	-	+		-1-	-	4		8

The number from the Table = a'.

TABLE XXXIX.

Aberration in N. P. D. to find p'.

Argument, R. A. of the Star in Time.

	0h	12h +	1h	13h +	2h	14h +	3h	15h +	4h	16h +	5h	17h +	
P. P.	m.	"	P. P.	"	P. P.	"	P. P.	"	P. P.	"	P. P.	"	m.
-	0	20.255	-	19.595	-	17.541	-	14.322	-	10.128	-	5.243	60
12	10	20.236	34	19.318	54	17.083	70	13.684	85	9.353	88	4.384	50
24	20	20.178	68	19.033	108	16.592	140	13.019	161	8.560	176	3.517	40
36	30	20.082	102	18.713	162	16.069	210	12.330	246	7.751	264	2.644	30
48	40	19.947	136	18.357	216	15.516	280	11.618	328	6.928	352	1.764	20
60	50	19.775	170	17.966	270	14.934	350	10.884	410	6.091	440	0.883	10
72	60	19.565	224	17.541	324	14.322	420	10.128	492	5.243	528	0.000	0
	+ 11h	23h	+ 10h	25p	+ 9h	21h	+ gh	80µ	+ 7h	19h	+ 6h	18h	

Multiply the number found in the Table by the natural sine of the Star's declination; the result will give b.

0.00 8.88

HER HAD B

45-21 040 TE

ILAL SET LAND

12 674 (2.7)

· 中华中国 (100 B)

15.21

1.50 950 1575 1.50 10,14 (575

Taue

TABLE XL.

Aberration in N. P. D. to find q'.

Argument, R. A. of the Star in Time.

	Oh	12h	1h	13h	2h	14h	3h	15h	4h	16h	5h	17h	
	+	-	+	-	+	- 10	+	-	+	1 to 1	*	1000	
P. P.	m.	"	P. P.	"	P. P.	11-	P. P.	"	P. P.	"	P. P.	"	m.
+	0	0.000	+	4.809	+	9.290	+	13.138	+	16.090		17.947	60
80	10	0.810	75	5.588	64	9.984	50	13.700	30	16.480	10	18.140	50
160	20	1.619	150	6.355	128	10.657	100	14-233	60	16.839	20	18.298	40
240	30	2.426	225	7.110	192	11.311	150	14-740	90	17.166	30	18.420	30
320	40	3.226	300	7.852	256	11.943	200	15.220	120	17.460	40	18.509	20
400	50	4.022	375	8.579	320	12.552	250	15.669	150	17.720	50	18.562	10
480	60	4.809	450	9.290	384	13.138	300	16.090	180	17.947	60	18.580	0
	+		+	-	+	-	+	-	+	-	+	15	
	11b	23h	10h	22h	gh	21h	8h	20h	7h	19h	6h	18h	9

The number from this Table, multiplied by the natural sine of the Star's declination, gives a product, to which r' being added, the result will be c'.

TABLE XLI.

1745

ST.D

WING SPEN

merrera.

Argument, Declination of the Star.

Dec. North - South +

D.	No.	D.	No.	D.	No.	D.	No.	D.	No.	D.	No.	D.	No.	D.	No.	D.	No.
0	11	0	11	0	11	90	761.0	0	11	P	11	0	11	D	111-1-0	0	11
															2.759		
															2.626		
															2.493		
3	8.055	13	7.859	23	7.425	33	6.765	43	5.900	53	4.854	63	3.662	73	2.358	83	0.983
4	8.046	14	7.826	24	7.369	34	6.687	44	5.803	54	4.741	64	3.536	74	2.223	84	0.843
5	8.035	15	7.791	25	7.311	35	6.607	45	5.703	55	4.626	65	3.409	75	2.088	85	0.703
6	8.021	16	7.753	26	7.250	36	6.526	46	5,603	56	4.510	66	3.281	76	1.951	86	0.563
7	8.005	17	7.713	27	7.187	37	6.442	47	5.501	57	4.393	67	3.152	77	1.814	87	0.423
8	7.987	18	7.671	28	7.122	38	6.356	48	5.397	58	4.274	68	3.022	78	1.677	88	0.282
9	7.967	19	7.626	29	7.055	39	6.268	49	5.292	59	4.154	69	2.891	79	1.539	89	0.141
9	7.987	18 19	7.671	28 29	7.122 7.055	38 39	6.356 6.268	48 49	5.397 5.292	58 59	4.274	68 69	3.022 2.891	78 79	1.677	88 89	0.28

The number from this Table is r'.

TABLE XLII.

ALON DESCRIPTION OF THE PERSONS

Lunar Nutation in R. A. to find s' = d'.

Argument, R. A. of the Star in Time.

1	3.	Oh	+ 12h	-Ih	+ 19h	9h	+	- oh	+	-	+	-	+	S.
N	ī.	2+2	-	2+	13h	+	14h	3h	15h	4h +	16h	5h	174	N.
P.	P.	m.	141	P. P.	"	P. P.	"	P. P.	"	P. P.	"	P.P.	"	m.
	+	0	0.000	+	2.497	+	4.824	+	6.823	+	8.355	+	9.319	60
	42	10	0.421	40	2.901	34	5.185	26	7.113	17	8.558	4	9.419	50
	84	20	0.841	80	3.300	68	5.534	52	7.391	34	8.744	9	9.501	40
	26	30	1.260	120	3.693	102	5.874	78	7.655	51	8.914	14	9.566	30
1	68	40	1.675	160	4.077	136	6.202	104	7.903	68	9.066	18	9.611	20
2	10	50	2.088	200	4.455	170	6.518	130	8.137	85	9.202	22	9.639	10
2	52	60	2.497	240	4.824	204	6.823	156	8.355	102	9.319	27	9.648	D
1	٧.	114	23h	+ 10h	22h	+ 9h	21h	+ gh	200	一去。	CONTRACT.	1	Inca	N.
S.	1	ا النا	4014	100	1 54 11	ga	+	-	20h	117h	19h	6h	184	8

FOR COMPUTING THE NUTATION OF A STAR IN RIGHT ASCENSION AND DECLINATION.

TABLES

	TAE	TABI	OR	LIII.	f.	TAI	TAB	OR	LIV-	N.		JATION		LV. QUINOXI	
F	For	the Notar.— the Notar.—	Lon. I	in R. A Moon's N in Decl gns — L	ode.	R.A.	star—I star—I the N	Lon. Nutation	n in R. A Moon's N n in Dec	ode. lin.	L		le of th	e Moon'	
Ī				s. s. 11 VIII	1				S. S. IIVIII — +	Ī			I VII	S. S. 11 VIII — +	Ī
ŀ	0	-11	"	"	0	0	"	"	"	0	0	- "	- "	"	0
١	0	8.77	7.60	4.39	30	0	1.29		0.64	30	0	0.00	8.62	14.93	30
۱	1	8.77	7.52	4.25	29	1	1.28			29	1	0.30	8.88	15.08	29
۱	2	8.77	7.44	4.12 3.98	28 27	2	1.28			28	2	0.60	9.14	15.23	28
ı	3	8.75		3.84	26	4	1.28		0.58	26	3	0.90	9.39 9.64	15.36 15.50	27 26
۱	5	8.74		3.71	25	5	1.28			25	5	1.50	9.89	15.63	25
ı	6	8.72	11.5/5/5	3.57	24	6	1.28			24	6		10.14	15.75	24
ı	7	8.71	7.00	3,43	23	7	1.28	1.03		23	7	2.10	Control of the Control	15.87	23
ı	8	8.69	6.91	3.29	22	8	1.27	1.01	0.48	22	8		10.62		22
t	9	8.66	6.82	3.14	21	9	1.27	1.00	0.46	21	9	2.70	10.85	16.10	21
١	-10	8.64	6.72	3.00	20	10	1.27	0.98	0.44	20	10	2.99	11.08	16.20	20
1	11	8.61			19	11	1.26			19	11	3.29	11.31	16,30	19
1	.12	8.58	W		18	12	1.26			18	12		11.54	16.40	18
1	13	8.55		2.56	17	13	1.25			17	13		11.76		17
1	14	8.51		2.42	16	14	1.25			16 15	14	4.17	11.98	16.58	16
١	16	8.43			14	16	1.24	A		14	15 16		12.19	16.66	15
1	17	8.39		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	13	17	1.23			13	17		12.61	16.88	13
١	18	8.34			12	18	1.22			12	18		12.81		12
١	19	8.29	5.75	1.67	f1	19	1.22			11	19	5.61			11
1	20	8.24	5.64	1.52	10	20	1.21	0.83	0.22	10	20	5.90	13.21	16.98	10
J	21	8.19			9	21	1.20			+9-	21		13.40	17.03	9
1	22	8.13			8	22	1.19			8	22		13.59		8
١	23	8.07			7	23	1.18			7	23		13.77		7
ı	24	8.01			6	24	1.17			6	24	7.01			6
	25 26	7.94	100		5	25 26	1.16	1000000		5	25	7.29	14.13		5
1	27	7.81			3	27	1.14			3	26 27		14.46		4
	28	7.74			2	28	1.13			2	28		14.62		2
1	29	7.67	1 1 1 1 1 1		1	29			1 2 3 5 5 7 6 7	ĩ	29	8.36	1 2 2 2 2		ĩ
	30	7.60	4.39	0.00	0	30				0	30		14.93		0
			S. 8				S. S.	. S. S				s. s XI V		8. S.	

To find the Nutation of a Star in Right Ascension.

To the log of the sum or difference of the equations from Tables XLIII. XLIV. answering to their proper arguments, add the log. tangent of the Star's declination; the sum will be the log. of part first of nutation, and if the declination is south, change the sign—to which apply the equation from Table XLV. answering to the longitude of the Moon's node, and the sum or difference will be the nutation in right ascension.

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To find the Nutation of a Star in Declination.
Increase the arguments of Tables XLIII. and XLIV. each by the three signs, and the sum or difference of the corresponding equations will be the nutation in declination. If the declination is south change the sign of the second equation.

FOR COMPUTING THE ABERRATION OF A STAR IN RIGHT ASCENSION AND DECLINATION.

ı	-		_	_						_		_	-	_	
ı		TAI	BLE 2	XLVI.			TAB	LE X	LVII.		-	TAB	LE X	LVIII.	
ı			OR	1171	100			OR					OR		_
ı	TAD		-	ERRATI	ON.	TAR	LE II.	OF AL	BERRAT	TON.	TABI	LE III.	OF A	BERRAT	TION.
ł	TAB	LE I.	JI AB	LARALI		- 440		-	-		-	-	-	-	
ı		AR	GUMI	ENT.			AI	GUM	ENT.			AB	GUMI	ENT.	
ı	For	the Al	berrat	ion of	R.A.	For	the A	berrat	ion in	R.A.	Ror			ber. in	Daci
ı				n. Sun.		1000			n's Lor			5. YES			mon
ı	1			ion in l							Su	in's Lo	on.+S	tar's D	ecl.
ı						100000					For	part :	3d Ab	er. in I	Decl.
ı	R.As	cen. St		signs—	oun s	H.A	scen. 5			Sun's		m's Le	n. +S	tar's De	loc
1			Lon.		-1			Deci			- 50	III S LI	711.10	tur a De	
I	1			5. 5.		1		S. S.		1				S. S.	
ı		1	-	11 VIII			0 VI	+ -	11 VIII			100000	-	II VIII	4.1
ı		-+	-+	"	- 0	-	T -	+-	T -	0	- 0	-+	-+	-+	-
1	0	The state	16,82	9.71	30	0	0.84	200	1 1000 5	30	0	4.03	Contract.	2.02	30
ı	1		16.64		29	1	0.84		A DECEMBER OF	29	1	4.03		1.96	29
1	2	19.40	16.47		28	2	0.84	0.71	0.39	28	2	4.03	3.42	1.89	28
1	3	The second second	16.29		27	3	0.84	100000		27	3	4.03	The second second	1.83	27
1	4		16.10		26	4	0.84			26	4	4.02		1.77	26
ı	5	Part of the Part o	15.91		25	5 6	0.83		10000	25	5 6	4.02	120000	1.70	25
1	7		15.51	10000	23	7	0.83		I SCOTTON	23	7	4.00	20000	1.58	23
ł	8	19.23			22	8	0.83	100000	100 100	22	8	3,99	200000	1.51	22
۱	9	19.18	15.09	6.96	21	9	0.83	0.65	0.30	21	9	3 98	3.13	1.45	21
١	10		14.88		20	10	0.83	0.64		20	10	3.97	3.09	1.38	20
1	11		14.66		19	11	0.82		100000000000000000000000000000000000000	19	11	3.96	10000	1.31	19
1	12	The second second	14.43	40.766.270	18	12	0.82	95.5	PROPERTY.	18	12	3.95	35.90		18
ı	13	18.84	35000	5.35	16	14	0.82	100000	0.25	16	13	3.93		1.18	17 16
ı	15		13,73	100000000000000000000000000000000000000	15	15	0.81	0.59	100000000000000000000000000000000000000	15	15	3.90	1000000	1.04	15
ı	16	18.67	13,49		14.	16	0.81	0.58		14	16	3.88	2.80		14
۱	17		13.24		13	17	0.80		100 200	13	17	3.86	2.75	0.91	13
۱	18		12.99		12	18	0.80	100000000000000000000000000000000000000	100000000000000000000000000000000000000	12	18	3.84	2.70		12
1	19	1	12.74	-	11	19	0.79	0.55	-	11	19	3.81	2.65	0.77	11
1	20 21		12.48 12.22		10	20	0.79	0.54	0.15	10	20	3.79	2.59	0.70	10
ı	22	Marie Control	11.96	20.53	8	22	0.78	1000 1000	700.000	8	22	3.77	2.48	0.56	9 8
1	23	0.000	11.69	-	7	23	0.77	0.50	200	7	23	3.71	2.43	0.49	7
1	24	17.74	11.41	2.03	6	24	0.77	0.49	0.09	6	21	3.68	2.37	0.42	6
1	25	17.60		1.69	5	25	0.76	3/20/00/5	0.7.0	5	25	3.66	2.31	0.35	5
1	26	17.45	10.86		4	26	0.75	ECH REG	0.06	4	26	3.63	2.26	0.28	4
1	27 28	And the last of the	10.35	1 July 20	3	27 28	0.75	100000		3 2	27 28	3.59	2.20	0.21	3 2
1	29		10.00	and the second	î	29	0.73	BOOK 50-3	337 C.Ft.	î	29	3.53	2.08	0.07	I
1	30	A STATE OF THE STA					0.73		100000	0	30	3.49	2.02	0.00	Ô
1		-+	-+	- +	11 17	174	+ -	+-	+ -			- +	-+	-+	
1		-	S. S.	-	01)	080	A COLUMN TO A STATE OF THE PARTY OF THE PART	S. S.	S. S.	-		S. S.	S. S.	S. S.	4.0
1		XIV	XIV	IX III	1.	200	XIV	XIV	IX III	1		XIV	XIV	IX III	2

To find the Aberration of a Star in Right Ascension.

To the log. of the sum or difference of the equations from Tables XLVI. XLVII. answering to their arguments, add the log. secant of the Star's declination, the sum will be the log. of the aberration in right ascension.

To find the Aberration of a Star in Declination.

Find the sum or difference of the equations answering to the former arguments, increased by 111 signs, to the log. of which, add the log. sine of the Star's declination; the sum will be the log of part 1st of the aberration. Take parts second and third of aberration from Table XLVIII. which, applied to the former, will give the aberration in declination. If the Star's declination is south, change the sign of parts 2d and 3d.

-	_	_					_								103
	2010	660	145		_			_			1	TA	BLE	LII.	
		quity	of the								Lu	n. Nut.		Equi	noxes
·		ptic,	71			mi	nr r				Long				Long
Year 1800	23	27	56.24			TA	BLE	LII			Moon Node	o v	ī vn	II VIII	,IN OUE,
1810	100	27	51.83				- 10		-			S	S	8	0
1820 1830		27 27	43.00	Sol. I	Nut.	of th	ne E	quino	xes in	R.A	0 2	0.00	0.55	0.97	30
	nual D			Sur	's l	-	-		. Su	n's	4	0.04	0.59	0.98	28
		,		tru			VII		1 +		6	0.11	0.65	1.01	24
		413		Lor	ig.		1112		Lor	ng.	8	0.15	0.69	1.02	22
-	thly I	_	-	- 0	_	_	T	+ +		-	10	0.19	0.71	1.04	20
Jan.			0.00	0		0.0	00	0.06	1	30	12	0.23	0.75	1.05	18
Feb. Marc		2 1 1 1 1 2	0.04	5	1	0.0	3.57 U	0.07		25	14	0.26	0 78	1.06	16
Apri			.11	10	- 1	0.0	3.50	0.07		20	16	0.30	0.81	1.07	14
May			.14	15		0.0	4(0.07		15	18	0.34	0.83	1.09	12
June			.18	20		00		0.07		10	22	0.41	0.88	1.09	8
July			.22	25		0.0		0.06	- 1	5	24	0.44	0.90	1.10	6
Augu			.25	30		0.0	16	0.06		0	26	0.48	0.92	1 10	4
Sept. Oct.		-	.29		1	T 177	_				28	0.51	0.95	1.10	2
Nov.	1		.33			I VI	v				30	0.56	0.97	1.10	0
Dec.	i		.40		1		+					X1 V	X IV	1X III	-
	_	1 0	-	DI		_	1 (-	-	-	111			_
-	Rel	lan T		BLE		N.1	alie-	-	1			CABLI	LI.		
		_	quatio	n or t			_			1		Equat		the	_
	on's		Equa	tion.		orres						Obliqui			
	Long		-		Day	s of t	ne I	lonth	[=9	.64		in Long		a's No	de. I
8		8	1 .	,			1		Long	1	1	- 1		7. 4	ong.
0	0	V	1		Mar	. 9	1 Sep	ot. 23	4.00		VI	IVII	[[V1]		on's
-	5		-	43	Jiai	2		28	Node.	1-	-	+-	+ -		ode.
	10			.41			1 Oc		0	-	,, ,	"		-	
	15				Apri			9	0	9	.65	8.34	4 82	1	
	20			33		10		14	1	9	.64	8.25	4 67	2	
1	25	377		29		1.		19	2		.63	8.16	4.53		
1	5	VI	1	22		20	- 1	24	3		.62	8.08	4 37		
	10		+0.		May				4		.60	7.94	4.22		
	15			.00			200	8	5 6		.58	7.89	3.92		
	20		-0	08		11		13	7		.56	7.69	3 76		
	25		0.	22		16	3	18	8		.54	7.59	3.61		20.
11	0	VIII		29		21		22	9		52	7.49	3.15	7.7	
	5			33		27		27	10	100	.50	7.38	3 39		
	10		1	7.50	June		1		11	1000	46	7.27	3.14		
	15		1.00	41 43		11		12	12		39	7.16	2.98		
	25	1		43		16	1	17	14		35	6.93	2.66		
III	0	IX		43		22	41	22	15		31	6.81	2.49		
	5			41		27		27	16		26	6.69	2.33	14	
	10			37	July	2			17		21	6.57	2.17	1	
	15			33		7		6	18		16	6.45	2.00		
	20			29		13		11	19		06	6.32	1.84		
īv	-	V		22	-	18		16	21		99	6.06	1.51		
. ,	5	X		15		28		20 25	22		93	5.93	1.34		
	10				Aug.			30	23	8.	87	5.80	1 17		
	15		+0.			8	Feb		21		80	5.66	1.01	6	
	20			15		13		9	25		73	5.53	0.84	5	
	25		0.	22		18		14	26		65	5.39	0.67	4	
V	0	XI		29		23		19	27		57	5.25	0.50	3	
	5			33		29		24	28		43	5.11 4.96	0.33	1	
	10			38 8	ept.	3	Ma		30		84	4.82	0.00	0	
4.	20			41	00	13		11	7	+	11	-	7 ==	4	190
	25			43		18		16	100	121			II ZI		- 7
VI		XII		13		23		21				4.7 Sept. 16			

104 Cha	TABLE LIL	1. Right Ascen	-			Stars for 1828	_
Cha- acters.	Constellations.	Pr. Name.	Mag.	Right Ascension.	Annual Var.	Declination.	Var.
199	a shallow		-	km s	5	0 / //	. 104
CE .	Ursæ Minoris		2	0 59 2.6		88 23 29 N 58 19 3 S	+ 19.45 -18.52
a	Eridani Arietis	Achernar	5	1 57 29.9		22 38 42 N	
æ	TAURI	Aldebaran	1	4 26 3.7			
a	Aurigæ	Capella	1	5 4 0.0		45 48 45 N	
β	Orionis	Rigel	1	5 6 16.6	+ 2.88		- 4.74
2	Orionis	Bellatrix	2	5 15 54.6		E. T. S. 1769 158	
OK.	Orionis	Betelguese	1	5 45 51.9		1 2 2 2 2 2 2	+ 1.36
CE	Navis Canis Majoris	Canopus	1	6 20 8.2			
-	Geminoru.n	Sirius	1	7 23 36.9		The second second	1
æ	Canis Minoris	Procyon	1	7 30 18.0		70 70 70 70	
B	GEMINORUM	Pollux	i	7 31 47.0			- 8.02
B	Navis	E - Chive	1	9 11 20.0			+ 14.85
æ	LEONIS	Regulus	1	9 59 12.4	Marie Control	12 48 18 N	
æ	Ursæ Majoris	Dubhe	2	10 53 2.5		62 40 40 N	A CONTRACTOR OF
æ	Crucis Vinginis	Cnice	1	12 17 7.7			+20.08 +18.94
B	Centauri	Spica	1	13 16 8.8 13 51 46.9			+ 17.85
2	Draconis	19 99. 10	2	13 59 44.2			_17.48
æ	Bootis	Arcturus	1	14 7 49.3	Carles and Carles	The second second	_18.97
æ	Centauri		Î	14 28 36.6	+ 4.45	60 8 8 8	+ 16.15
æ	2 Libræ	Zubenesch	2	14 41 22.9			+ 15.2
4	Scorpion is Draconis	Antares	1	16 18 52.5			+ 8.59
~	THE RESERVE	Rastaban	3	17 52 37.1	1	THE RESERVE OF THE PERSON NAMED IN	1000
æ	Lyræ	Vega	1	18 31 7.2 19 42 23.6	The Laboratory		+ 3.09
a	Aquarii	Altair	1 3	21 56 57.0			-17.2
B	Gruis	P PLOE	2	21 56 57.9	The Party of the P		_17.1
Œ	Pis. Austr.	Fomalhaut	1		+ 3.3	30 34 24 5	18.8
æ	PEGAST	Marcab	2	22 56 12.1		8 14 16 53 N	+ 19.3
	TABLE 1	IV.—Decimal	_	-	h Day in	the Year.	
1	A1 07. 400	AL I DA UR O		onths.	2.4	O N	100
-		April. May. 162 0.246 0.32				Oct. Nov. D	
- 1	20.003 0.088 0	.164 0.249 0.33	1 0.41	6 0.499 0.58	3 0.668 0	750 0.835 0.	917
	3 0.006 0.091 0	.167 0.252 0.33	4 0.41	9 0.502 0.58	6 6.671 0	.753 0.833 0.	920
	4 0.008 0.093 0	.170 0.255 0.33	7 0.42	22 0.504 0.58	9 0.673 0	.755 0.840 0.	922
		.173 0.258 0.34					
	6 0.014 0.099 0	.175 0.260 0.34	2 0.45	27 0.509 0.59	4 0.678 0	.760 0.845 0.	928
		0.178 0.263 0.34 0.181 0.266 0.34					
		.184 0.269 0.35					
-	10 0.025 0.109 0						
	11 0.028 0.112 0	.189 0.274 0.35	6 0.44	1 0.523 0.60	8 0.692 0	.775 0.859 0.	942
	12 0.030 0.115 0	.192 0.277 0.35	9 0.44	4 0.526 0.61	0 0.695 0	.777 0.862 0.	944
	13 0.033 0.118 0	0.195 0.280 0.36	2 0.44	17 0.529 0.61	3 0.698 0	.780 0.865 0.	947
	14 0.036 0.120 0 15 0.039 0.123 0						
	16 0.039 0.123 0						
	17 0.044 0.129 0						
	18 0.046 0.131 0	.208 0.293 0.37	5 0.4	50 0.542 0.69	7 0.711	.793 0.878 0.	961
	19 0.049 0.134 0	.211 0.296 0.37	8 0.46	63 0.545 0.63	0 0.714 0	.796 0.882 0.	964
	20 0.052 0.137	STREET, SQUARE, SQUARE,	-	THE RESERVE AND PERSONS ASSESSED.	Marie Street, or other Parkets and Parkets	CONTRACT THE REST LINE	
	21 0.056 0.140						
	22 0.057 0.142						
	23 0.060 0.145 0						
	24 0.063 0.148 0 25 0.066 0.151 0						
	26 0.068 0.151 0						
	27 0.071 0.156						
1	28 0.074 0.159						
1	29 0.077 0.162 0	.239 0.323 0.40	6 0.49	90 0.573 0.65	7 0.742 0	.824 0.909 0.	991
15	30 0.079	.241 0.326 0.40	18/0.4	93/0.575/0.6	0/447.0/08	.826 0.912 0.	994
		.244 0.4		0.578 0.6			700.

	1917	47	TABLE I	.VI.		108
	8		ension for ever	y Day in the Y	car 1828.	
Days.	January.	February.	Marcii	April.	May.	June.
1	h m s 1844 5	20 56 36	22 49 40	h m s	h m s	h m s
2	18 48 30	21 0 41	22 53 24	0 46 49	2 38 16	4 41 18
3	18 52 55	31 4 45	22 57 7	0 50 27	2 42 6	4 45 24
5	18 <i>57</i> 19 19 1 43	21 8 47 21 12 50	23 0 51 23 4 33	0 54 6	2 45 56 2 49 47	4 49 31 4 53 38
6	19 6 7	21 16 51	23 8 16	1 1 24	2 53 38	4 57 45
7	19 10 30	\$1 20 51	28 11 57	1 5 3	2 57 30	5 1 52
8	19 14 52 19 19 14	21 24 51 21 28 50	23 15 39 23 19 20	1 8 42	3 1 23 2 5 1;	5 6 0 5 10 8
, 10	19 23 36	21 32 44	28 23 1	1 16 2	3 9 10	5 14 17
11	19 27 57	21 36 45	23 26 41	1 19 42	3 13 4	5 18 25
12 13	19 38 17 19 36 37	21 40 42 21 44 38	23 30 22 23 31 1	1 23 23 1 27 3	3 16 59 3 20 55	5 22 34 5 26 43
14	19 40 57	21 4 , 33	23 37 41	1 30 45	3 24 51	5 30 52
15	19 45 15	21 52 27	23 41, 21	1 34 26	3 28 48	5 35 2
16 17	19 49 33 19 53 50	21 56 21 22 0 14	23 45 0 23 48 39	1 38 8 1 41 50	3 32 45 3 36 43	5 39 11
18	19 58 7	22 4 6	23 52 18	1 45 33	3 40 42	5 43 20 5 49 30
19	20 2 23	29 7 57	23 55 56	1 49 16	3 44 40	5 51 39
20	20 6 38	22 11 48 22 15 38	23 59 35	1 52 59	3 48 40	5 55 49
21 22	20 10 52 20 15 6	22 19 27	0 3 13 0 6 51	1 56 43 2 0 27	3 52 40 3 56 41	5 59 59 6 4 8
23	20 19 19	22 23 16	0 10 29	2 4 12	4 0 42	6 8 18
24	20 23 31	22 27 4	0 14 7	2 7 57	4 4 43	6 12 27
25	20 27 42 20 31 52	22 30 52 22 34 38	0 17 45 0 21 23	2 11 43 2 15 29	4 8 45 4 12 48	6 16 36 6 20 45
27	20 36 1	28 38 25	0 25 1	2 19 15	4 16 51	6 24 54
28	20 40 10	22 42 10	0 28 39	2 23 2	4 20 54	6 29 3
30	20 44 18 20 48 25	22 45 55	0 37 17 0 35 55	9 26 50 9 30 38	4 24 58 4 29 2	6 33 11
31	20 48 23		0 39 33	# 30 30	4 33 7	6 37 20
Days.	July.	August.	September.	October.	November.	December.
,	hm s	h mas	h m s 10 42 14	h m s 12 30 19	h m s	b m •
2	6 41 23 6 45 36	9 46 14 8 50 6	10 45 52	12 30 19 12 33 57	14 26 39 14 30 35	16 30 36 16 34 56
3	6 49 44	8 53 58	10 49 29	12 37 35	14 34 32	16 39 16
4	6 53 51	8 57 50 9 1 41	10 53 6 1 10 56 43	12 41 13 12 44 52	14 38 30	16 43 37
5 6	6 57 58	9 1 41	11 0 20	12 48 31	14 42 28 14 46 27	16 47 59 16 52 21
7	7 6 11	9 9 21	11 3 56	12 52 11	14 50 97	16 56 44
8	7 10 18	9 14 10 9 16 59	11 7 33	19 55 51	14 54 28	17 1 7
10	7 14 23 7 18 29	9 16 59 9 20 47	11 11 9 1	19, 59 31 13, 3 12	14 58 30 15 2 33	17 5 31 17 9 55
ii	7 22 34	9 24 34	11 18 91	13 3 53	15 6 36	17 14 20
12	7 26 38	9 28 21	11 21 56	13 10 35	15 10 41	. 17 18 44
13 14	7 30 42 2	9 32 7 9 35 53	11 25 32 11 29 8	13 14 17 13 18 0	15 14 46 15 18 52	17 23 10 17 27 35
15	7 88 49	9 49 38	11 32 43	13 21 44	15 22 59	17 38 1
16	7 48 61	9 43 23	11 36 19	13 24 28	15 27 6	17 36 27
17	7 46 53	9 47 7 9 50 51	11 39 54 11 43 29	13 29 12 13 32 57	15 31 15 15 35 24	17 40 53 17 45 19
19	7 54 55	9 54 34	11 47 5	13 36 43	15 39 34	17 49 45
20	7 58 56	9 58 16	11 50 40	13 40 29	15 49 45	17 64 18
21	8 9 56	10 1 58	11 54 16 11 57 51	13, 44, 16 13, 48, 3	15 47 57 15 52 9	17 58 38
22	8 6 55	10 5 40 10 9 21	12 1 27	13 51 52	15 56 22	18 3 5 18 7 31
24	8 14 51	10 13 2	12 5 3	13 55 41	16 0 36	18 11 58
25	8 18 49	10 16 48	12 8 39	13 59 30	16 4 51	18 16 25
26 27	8 22 45 8 26 42	10 20 22 10 24 2	12 12 15 12 15 51	14 9 21	16 9 7 16 13 23	18 20 51 18 25 17
28	8 30 37	10 27 41	12 19 28	14 11 4	16 17 40	18 29 44
29	8 34 38	10 31 20	12 23 4	14 14 56	16 21 58	16 34 10
30 31	8 42 20	10 34 58	12 26 42	14,18 50 14 22 44	16 26 17	18 \$8 35 18 43 1
21	0 74 40 1	10 00 00)		-2 -4 -23	H	

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106	TABLE	LVII.—Sun'	Declination fo	or every Day ir	the Year 182	BELLEVE
1	January.	February.	March.	April	May.	June
Days.	South.	South.	a South	North.	North.	North:
1	m° 4'm"	tal afort a	9 1 1	0 '1 "	9 1 11	0 / "
10	23 4 22	17 17 44	7 28 10	4 38 49	15 9 11	22 5 43
30	22 59 29	17 0 43 16 43 23	6 42 21	5 1 52 5 24 50	15 27 8	22 13 37
1112	22 48 20	16 25 46	6 19 18	5 47 48	15 44 50	22 21 7
5	22 42 5	16 7 53	5 56 9	6 10 29	16 19 27	22 34 57
6	22 35 23	15 49 42	5 32 56	6 33 9	16 36 22	22 41 17
70	22 28 14	15 31 15 15 12 32	5 9 38	6 55 43	16 53 0	22 47 12
8	22 20 38 22 12 36	14 53 34	4 22 50	7 18 10 7 40 30	17 9 22 17 25 26	22 52 44 22 57 52
10	22 4 8	14 34 21	3 59 21	8 2 42	17 41 13	23 2 36
11	21 55 14	14 14 53	3 35 48	8 24 46	17 56 43	23 6 55
12	21 45 54		3 12 13	8 46 42	18 11 54	23 10 50
13	21 36 9	13 35 14 13 15 5	2 48 36 2 34 57	9 8 29 9 30 6	18 26 48	25 14 20
15	21 25 59 21 15 24	12 54 43	2 1 16	9 51 35	18 55 38	23 17 26
16	21 4 24	12 34 8	1 37 35	10 12 54	19 9 35	23 22 24
17	20 53 0	12 13 21	1 13 52	10 34 2	19 23 12	23 24 16
180	20 41 13		0 50 10	0 55 1	19 36 29	23 25 431
19 20	20 29 2	11 31 13	0 26 27 0 2 45 S	11 15 48	19 49 27 20 2 4	23 26 45
21		10 48 22	0 20 56 N	P. Approved Prop. 1	20 14 20	23 27 221
22	19 50 11	10 26 41	0 44 36	12 17 1	20 26 16	23 27 22
23	19 36 29	10 4 51	1 8 11	12 37 2	20 37 51	22 26 452
21	19 22 26	9 42 52	1 31 50	22 56 50	20 49 5	23 25 44
25	19 8 1 18 53 16	9 20 44 8 58 28	1 55 24 2 18 56	13 16 25 13 35 48	20 59 57 21 10 28	23 24 17
27	18 38 10	8 36 5	2 42 21	13 54 56	21 20 36	23 22 26
28	18 22 43	8 13 33	3 5 49	14 13 51	21 30 28	23 17 30
29	18 6 57	7 50 55	3 29 10	14 32 32	21 39 47	23 14 25
30	17 50 52	THE RESERVE OF THE PERSON NAMED IN	3 52 27	14 50 59	21 48 49	28 20 56
31	17 34 27	12 00 W 10	4 15 10	October.	21 57 28	13 E 1
Days.	North.	North.	North.	South.	November.	December.
125	0 / "	0 / "	6 / //	9 / //	South.	South.
1	23 7 2	17 59 28	8 13 9	3 16 33	14 31 39	21 52 8
2	23 2 44	17 44 9	7 51 16	3 39 51	14 50 44	22 1 9
3	22 58 2	17 28 33	7 29 15	4 3 7	15 9 35	22 9 44
4	22 52 56	17 12 39	7 7 6	4 26 20	15 28 11	22 17 53
6	22 47 26 22 41 32	16 56 29 16 40 2	6 44 51 6 22 28	4 49 30 5 12 36	15 46 32 16 4 37	22 25 37
7	22 35 14	16 23 19	5 59 59	5 35 39	16 22 26	22 32 54 22 39 45
8	22 28 33	16 6 21	5 37 25	5 58 37	16 39 59	22 46 9
9	22 21 29	15 49 6	5 14 44	6 21 31	16 57 14	22 52 6
10	22 14 1	15 31 36	The state of the s	6 44 19	17 14 12	22 57 36
11	22 6 11	15 13 52 14 55 53	4 29 8	7 7 2 7 2 7 29 40	17 30 52 17 47 14	23 2 38
13	21 49 22	14 37 39	3 43 13	7 52 11	18 3 18	23 7 13 23 11 21
14	21 40 23	14 19 11	3 20 9	8 14 35	18 19 2	23 15 0
15	21 31 3	14 0 30	2 57 2	8 36 52	18 34 27	23 18 12
16	21 21 20	13 41 35	2 33 51 2 10 38	8 49 2	18 49 32	23 20 56
17 18	21 11 16 21 0 50	13 22 27	2 10 38 1 47 22	9 21 4 9 42 58	19 4 17 19 18 41	23 23 12 24 24 59
19	20 50 3	12 43 35	1 24 4	10 4 43	19 32 44	23 26 19
20	20 38 55	12 23 50	1 0 43	10 26 19	19 46 27	23 27 10
21	20 27 26	12 3 54	0 37 22	10 47 46	19 59 47	23 27 33
22	20 15 36	11 43 46	0 13 59 N 0 9 25 S	11 9 3	20 12 46	23 27 21
23 24	20 3 27 19 50 57	11 23 28 11 2 58	0 9 25 S 0 32 50	11 30 10	20 25 22 20 37 35	23 26 53 23 25 51
25	19 38 7	10 12 18	0 56 15	12 11 53	20 49 26	23 25 51 23 24 21
26	19 24 58	10 21 28	1 19 39	12 32 28	21 0 53	23 22 22
27	19 11 30	10 0 28	1 43 4	12 52 51	21 11 57	23 19 55
28	18 57 42	9 39 18 9 17 59		13 13 2	21 22 36	23 17 0
30	18 43 36 18 29 11	8 56 31	2 29 51 2 63 13	13 33 1 13 52 47	21 32 52 21 42 43	23 13 37 23 9 46
31	18 14 28	8 34 54	N. S. S.	14 12 20	21 42 43	23 9 46 23 5 27
	STREET, ST. ST. ST.	AND RESERVED ASSESSMENT OF THE PARTY NAMED IN		STATE OF THE PARTY	of the latest device the latest devices and t	2 61

	TAB	LE	L	VI	11.	-l	qu	ati	on	of '	Tin	ned	or	eve	ry	Da	y 11	n th	ne i	Yea	ar !	82	8.	10
(33	Ja	n.	F	·b.	HVE	ar.	AI	ril	M	ay.	Ju	ne	Ju	ly.	Au	g.	Se	pt.	O	ct.	No	v.	De	ec.
Day	SON	ld	A	del	=A	dd	A	let	Si	16.	Si	ıb.	A	det	A	ld	St	ıb.	S	b.	St	b.	Su	ıb.
7	m	8	m	N	m	8	m	8	m	8	m		m		m	8	m		m	8	m	s	m	8
1		35	13		12	35	3	54	3		2	33	3	25	•	57		15		0000		17	-	38
2	4	4	14	_	12	23	-	36	3	990		21	3		5	53		34		43	16	17	10	14
3	-	32	iola i	1000	12	10	3	18	3	_	2	14	3	48	•	49		53		шин	16	пом	9	50
4		59	ми	13	11	56	3	U	3	-	2	4	3	58		44		12	1000		Marie of the last	16	9	20
5		MAI.	14	1	11	42	2	42	3	-	1	54	4	9		38		32	000	Name of	16	14	9	
6	_	54	nam.	23	ioles	28	2	25	3		1	43	4	19		32	1 2	51	-	Control 1	16	11	8	3
7		30	n an	27	11	59	2	50	3	41	1	33	4	29		25		32		12	10001	8	8	O.
8	-	46 11	100	30	1000	43	1	33	3	48	1	10	ш	39		18		52		29	15	58	-	4:
10		35	200	31	2000	21	i	17	3	51	0	58	4	57	5	1		12			mona	52	-	4
11		30	980	35		12	1	1	3	53	-	46	5	5	4	52	3			15	10000	45	100	21
12	11 (11 27)	25	-	35	9	35	0	45	3	55	-	34	-	13	one o	43	_	5		30		Bear)	5	5
13	-	44	200	34	9	34	0	29	3		0	1	-	20	4	32		15	made of	44	-	-		2
14		10	20	33	9	22	0	11	3	The same	0	9		27	4	22				58				5
10	172	10	iii	20	m	-	-	10.	10	-	ш	id.	llo		В	-	1	-		00		-	86	-
15	9	39	14	30	9	5	0	1	3	56	0	4	5	34	4	10	4	57	14	11	15	9	4	2
16		54	14	25	8	47	0	16	3	55	0	17	5	40		58				24				5
17		15	14	24	8	30	0	30	3	51	0	30	-	45		46				36				2
18	10	: 5	14	19	8	12	0	44	3	52	0	43	5	50	3	33				47			2	5
19	10	54	14	11	7	54	0	58	3	19	0	56	5	51	3	20	6	2)	14	58	14	20	2	2
20	11	12	14	Dg	7	31	1	11	.3	46	1	9	5	35	3	6	6	4.5	15	8	14	6	1	5
21	11	30	14	2	7	18	1	21	3	43	1	2	6	-1		51	7	3	15	18	13	51	1	2
22		47		55	7	0	1	36	3	-	1	35	6	-	·	37				27				5
23		3	13	47	6	41	1	45	3	34	2	47	6	6	2	21	7	45	15	35	13	18		2
1			#10	死	60	100	m	IB	12	538	80	B	100	28	80	188	199	80		m		36	A	dd
21		18		39	6	23	1	59	3	29	3	0		_	•	5	-	-	-	43	1000	201	0	
25		33	9.00	29	6	4	2	10	3	24	2	13	6	-	1	49				50		42		3
26		47	-	20	5	46	2	20	3	18	2	25	6		1	33		46		1000	100000	23	-	
27		0	-	9	5	27	2	30		12	-	38	6	- 8		16	9	_	16		12	4	1	3
28	1000	12	0.00	59	5	8	5	40	3	5	2	50	6	7	0	58	9	26	-		mm.	43	2	
29	-	23	12	47	4	50	2	49	2	57	3	2	6	- 5		41	9	46		10		22	2	3
30		33	614	95	4	31	2	57	2		3	14		3			10			13		0	3	
31	13	-		1	4	13	12	150	2	41	4	1	6	0	0	4	1500	-	16	15	_	-	3	2

41 11	TABLE	LIXC	orrection of	the Longi	tude by Chro	nometers.	DESTRUCTION.	
Days.	Log.	Days.	Log.	Days.	Log.	Days,	Log.	ľ
211	0.00000	31	2.69549	61	3.27669	91	3.62180	ı
1420	0.47712	32	2.72263	62	3.29070	192	3.63124	ı
1374	0.77815	33	2.74896	63	3.30449	193	3.64058	ı
\$84 SE	1,00000	34	2.77452	64	3.31806	94	3.64982	ı
#25 SS	1.17609	35	2.79934	65	3.33143	95	3.65896	И
846 88	1.32222	36	2.82347	66	3.34459	96	3.66801	н
1,739	1,44716	37	2.84696	67	3.35755	97	3.67697	ä
0.823	1.55630	38	2.86982	68	3.37033	98	3.68583	B
11914	1.6532	39	2.89209	69	3.38292	99	3.69461	B
10	1,74036	40	2.91381	70	3.39533	100	3.70329	J
11	1.81954	41	2.93500	71	3.40756	101	3.71189	a
12	1.89209	42	2.95569	72	3.41963	102	3.72041	ı
13	1.95904	43	2.97589	73	3.43152	103	3.72884	
14	2.02119	44	2.99564	74	3.44326	104	3.73719	
15	2.07918	45	3.01494	75	3.45484	105	3.74547	ö
16	2,13354	46	3.03383	76	3.46627	106	3.75366	a
17	2.18469	47	3.05231	77	3.47756	107	3.76178	
18	2.23300	48	3.07041	78	3.48869	108	3.76982	
19	2.27875	49	3.08814	79	3.49969	109	3.77779	
20	2.32222	50	3.1055	80	3.51055	110	3.78569	
21	2.36361	51	3.12254	81	3.52127	111	3.79351	
22	2.10312	52	2.13925	82	3.53186	112	3.80127	
23 24	2.4 091	53	3.15564	83	3.54233	113	3.80895	
24	2.477 2	54	3.17173	84	3.55 67	114	3.81657	
25	2.51188	- 55	3.18752	85	3.56289	115	3.82413	
26	2.54531	56	3.20303	86	3,57299	116	3.83161	
27	2.57749	57	3.21827	87	3.58297	117	3.83904	
28	2.60853	58	3.23325	88	3.59284	118	3.84640	
29	2.63849	59	3.24797	89	3.60260	119	3.85870	
30	9.667.15	60	3.96945	00	9.61995	190	9.86094	

Aberdeen	108 TABLE I	X.—Latitudes an	nd Longitude	s of Places.	MANUAL DI
Aberdeen	Names of Places.	Latitude.		The second secon	THE RESERVE OF THE PARTY OF THE
Aberdeen	The latest of the latest	Maria Malatana de	ALC: NO PERSONAL PROPERTY AND ADDRESS OF THE PER	ALCOHOLD THE T	The second second
Amsterdam	A Market 100 100 100 100	A SHARE THE PARTY OF THE PARTY	Dr. Co. Block St.		
Archangel		B F C3 15 05 05 02 00 1	THE RESERVE AND ADDRESS OF THE PARTY OF THE		
Barbadoes (Bridgetown) 13 5 0 N 50 41 15 W 3 3.5 4 5 W 6 Barbaya 6 9 0 8 106 51 45 E 7 7 27 E Berlin 52 31 45 N 13 22 15 E 0 53 29 E 10 0 Berwick 55 54 62 1N 1 59 41 W 0 7 59 W 2 30 15 Berwick 53 3 4 38 N 8 48 0 E 0 35 12 E 6 0 Bremen 33 4 38 N 8 48 0 E 0 35 12 E 6 0 Bremen 33 4 38 N 8 48 0 E 0 35 12 E 6 0 Bremen 50 49 32 N 0 7 40 W 0 0 30 W 10 10 Brighton 50 49 32 N 0 7 40 W 0 0 30 W 10 10 Brighton 50 49 32 N 0 7 40 W 0 0 22 W 6 50 42 Calair 50 57 32 N 1 51 16 E 0 7 26 E 11 40 18 Calcutta 50 57 32 N 1 51 16 E 0 7 26 E 11 40 18 Calcutta 52 33 0 N 88 23 39 K 5 53 35 E 3 10 Cambridge 52 12 43 N 0 7 34 E 0 0 33 29 W 0 10 10 Canton 40 20 30 N 8 24 42 W 0 33 39 W 0 0 0 30 W 10 10 Canton 40 20 30 N 8 24 42 W 0 33 39 W 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0			DE 1 100 P. 1 Table 1 100 P.		Contract to the contract of th
Bertsin					D00-4-9-4-10
Berwick		# EQ. 1971 P. MIN.	70 150 12 164	411 THE R. P. LEWIS CO., LANSING, MICH.	500 to 10 10 10
Bombay (Church)	Berlin	52 31 45 N	13 22 15 E	0 53 29 E	
Bremen	Berwick	11 5 77 7 TV 36 36 8	F 122 00 103		TOURS OF THE PARTY
Brest					
Brighton			T 12 5 (6) 1025		ALL DO CO. O. O. O.
Bristol		10 2020 - 7 EST-CAL CO. A.	T 170 0 190		
Calcig		10 Page 1 Apr 1 Page 1 Page 1	17 1000 100 1201	THE RESERVE THE PARTY OF THE PA	7 40 2 2
Calcutta			TT. INVENTORISE VISION	THE PARTY NAMED IN COLUMN	
Cambridge		50 57 32 N		0 7 25 E	11 40 18
Canton	Calcutta	22 33 0 N	88 23 39 E	THE RESERVE OF THE PARTY OF THE	3 10
Coimbra		111 AND 1610 GEVOR	AN OWN PROPERTY	1 1 2 2 3 1 3 1 3 1 D D	THE AN RES
Constantinople	Canton		THE WEST NOTICE		A PER WALLES
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Rdinburgh (Observatory) 55 57 21 N 3 10 21 W 0 12 41 E 2 20 16	Dublin	53 23 13 N	6 20 30 W		
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Heligoland	Gottingen		THE RESERVE OF THE PARTY OF THE PARTY.		Time At 1
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Madras . 13 4 9 N 80 17 21 E 5 21 9 E Madrid . 40 24 57 N 3 42 15 W 0 14 49 W Malta . 35 53 0 N 14 30 35 E 0 58 2 E May (Light) . 56 11 22 N 2 32 47 W 0 10 11 W 1 50 Montpelier . 43 36 16 N 3 52 40 B 0 15 31 E Moscow . 55 45 45 N 37 33 0 E 2 30 12 E Naples . 40 50 15 N 14 15 45 E 0 57 3 E Oxford . 51 45 39 N 1 35 22 W 0 5 1 W Palermo . 38 6 44 N 13 22 0 E 0 53 28 E Paris . 48 50 14 N 2 20 15 E 0 9 21 E Pekin . 39 54 13 N 116 26 45 E 7 45 51 E Petersburgh . 59 56 28 N 30 18 45 E 2 1 15 E Philadelphia . 39 56 55 N 75 11 30 W 5 0 46 W 2 30 Plymouth . 50 22 20 N 4 7 16 W 0 16 29 W 6 0 18 Portsmouth . 50 48 3 N 1 5 59 W 0 4 24 W 11 20 18 Rome . 41 53 54 N 12 29 47 E 0 49 59 E Rotterdam . 51 55 22 N 4 29 11 E 0 17 56 E Slough . 51 30 20 N 0 36 0 W 0 2 24 W Stockholm . 59 20 31 N 18 3 30 E 1 12 14 E Toulon . 43 7 9 N 5 55 11 E 0 23 43 E Upsal . 59 51 50 N 17 39 0 E 1 10 36 E Venice . 45 25 32 N 12 20 59 E 0 49 24 E		49 57 44 N	5 11 5 W	0 20 44 W	5 0
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Pairis	Oxford	UNITED TO STATE OF THE STATE OF	ALTONOMORPO LA	THE RESERVE OF THE PARTY OF THE	W. B. LEWIS
Pekin . . 39 54 13 N 116 26 45 E 7 45 51 E Petersburgh .	raiermo .		TOURS OF U.S.		NO. S. LEWIS CO.
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Plymouth	Philadelphia	90 FP FF 37	CONTRACTOR AND ADDRESS AND ADD	5 0 46 W	2 30
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	7 man 5 1 007 5 10	100 P	VAC NO. T.	NE 1988	400 1000
the state of the s			170		

			E LXL			TABLE LXII. 109										
m			to Time.		**	Time into Space.										
To con	into	ees at Sider	eal Time	of the	Equator	To convert Sidereal Time into Degrees and Parts of the Equator.										
1	h m	1	m s	1	8	h	4.5	m	0 1	8	, ,,					
2	0 8	2	0 8	2	0.066	1 2	15 30	1 2	0 15	1 2	0 15					
3	0 12	3	0 12	3	0.200	3	45	3	0 45	3	0 45					
4	0 16	4	0 16	4	0.266	4	60	4	1 0	4	1 0					
5	0 20	5	0 20	5	0.333	5	75	5	1 15	5	1 15					
6	0 24	6	0 24	6	0.100	6	90	6	1 30	6	1 30					
8	0 28	8	0 28	8	0.466	7	105	7	1 45	7	1 45					
9	0 36	9	0 36	9	0.533	8 9	120 135	8	2 0	8	2 0 2 15					
10	0 40	10	0 40	10	0.666	10	150	10	2 30	10	2 30					
11	0 44	11	0 44	11	0.733	11	165	11	2 45	11	2 45					
12	0 48	12	0 48	12	0.799	12	180	12	3 0	12	3 0					
13	0 52	13	0 52	13	0.866	13	195	13	3 15	13	3 15					
14	0 56	14	0 56	14	0.933	14	210	14	3 30	14	3 30					
15 16	1 0	15 16	1 0	15	1.000	15	225	15	3 45	15	3 45					
17	1 8	17	1 8	16 17	1.066	16 17	240 255	16 17	4 0	16 17	4 0					
18	1 12	18	1 12	18	1.200	18	270	18	4 30	18	4 30					
19	1 16	19	1 16	19	1.266	19	285	19	4 45	19	4 45					
20	1 20	20	1 20	20	1.333	20	300	20	5 0	20	5 0					
25	1 40	21	1 24	21	1.400	21	315	21	5 15	21	5 15					
30	2 0	22	1 28	22	1.466	22	330	55	5 30	22	5 30					
35 40	2 20 2 40	23	1 32	23	1.533	23	345	23	5 45	23	5 45					
45	3 0	25	1 40	24	1.600	24	360	24	6 0 6 15	24 25	6 0 6 15					
50	3 20	26	1 44	26	1.733	Ten	ths.	26	6 30	26	6 30					
55	3 40	27	1 48	27	1.799	0.1	1.5	27	6 45	27	6 45					
60	4 0	28	1 52	28	1.866	0.1	3.0	28	7 0	28	7 0					
65	4 20	29	1 56	29	1.933	0.3	4.5	29	7 15	29	7 15					
70	4 40	30	2 0	30	2.000	0.4	6.0	30	7 30	30	7 30					
75 80	5 0 5 20	31	2 4 2 8	31	2.066	0.5	7.5	31	7 45	31	7 45					
90	6 0	33	2 12	32	2.133	0.6	9.0	32	8 0 8 15	32	8 0 8 15					
100	6 40	31	2 16	34	2.266	0.7	10.5	31	8 30	34	8 30					
110	7 20	35	2 20	35	2.333	0.9	13.5	35	8 45	35	8 45					
120	8 0	36	2 24	36	2.400	1.0	15.0	36	9 0	36	9 0					
130	8 40 9 20	37 38	2 28	37	2.466	Hundi	edths.	37	9 15	37	9 15					
140 150	9 20	39	2 32 2 36	38	2.533	s	1 "	38	9 30 9 45	39	9 30 9 45					
160	10 40	40	2 40	40	2.666	0.01	0.15	40	10 0	40	10 0					
170	11 20	41	2 44	41	2.733	0.02	0.30	41	10 15	41	10 15					
180	12 0	42	2 48	42	2.799	0.03	0.45	42	10 30	42	10 30					
190	12 40	43	2 52	43	2.866	0.05	0.75	43	10 45	43	10 45					
200	13 20	44	2 56	44	2.933	0.06	0.90	41	11 0	44	11 0					
210 220	14 0 14 40	45	3 0 3 4	45	3.000	0.07	1.05	45	11 15	4.5	11 15					
230	15 20	47	3 8	46	3.066	0.08	1.20	46	11 30 11 45	46 47	11 30					
240	16 0	48	3 12	48	3.200	0.09	1.35	48	12 0	48	12 0					
250	16 40	49	3 16	49	3.266	0.10		49	12 15	49	12 15					
260	17 20	50	3 20	50	3.333	Thous	andths.	50	12 30	50	12 30					
270	18 0	51	3 24	51	3.400	0.001	0.015	51	12 45	51	12 45					
280	18 40	58	3 28	52	3.466	0.002	0.030	52	13 0	52	13 0					
290 300	19 20 20 0	53	3 32	53	3.533	0.003	0.045	53	13 15	53	13 15					
310	20 0	51	3 36	55	3.600	0.004	0.060	54	13 30	54 55	13 30 13 45					
320	21 20	56	3 44	56	3.666	0.005	0.075	55 56	13 45 14 0	56	14 0					
330	22 0	57	3 48	57	3.799	0.007	0.105	57	14 15	57	14 15					
340	22 40	58	3 52	58	3.866	0.008	0.120	58	14 30	58	14 30					
350	23 20	59	3 56	59	3.933	0.009	0.135	59	14 45	59	14 45					
360	24 0	60	4 0	60	4.000	0.010	0.150		15 0	60	15 0					
Or to	convert I	Degre	es and p	arts (of Ter-	Or to c			into Degr		d Parts					
- 1	estrial Lo	ngitu	ue into	Time			of Ter	restri	d Longit	ude.						
						or a comment and product										

1110	TABLE LXIII.—U	seful Numbers.	SCENAT.
Char.	Numbers.	Logarithms.	Arith. Com. Log.
Line hall	3 .14159265	0.4971499	9.5028501
92	9 .86960440	0.9942998	9.0057002
10	0 .78539816 .	9.8950899	0.1049101
100	0 .52359878	9.7189986 1.7581226	0.2810014
A=R°	57°.29577951	5.3144251	8.2418774 4.6855749
A=R"	206264".8	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	A CHARLEST TO SECOND
A=1°	0 .01745329	2.2418773	1.7581227
A=1'	0 .0002908882 +	4.4637262	2.5362738
A=1"	0 .0000048481368	6.6855749	5.3144251
N. 80.1	0.0795775=area of a circle to cir-	2.9007904	1.0992096
2555	1296000=seconds in a circle	6.1126050	3.8873940
CHARLE	86400=seconds in 24 hours	4.9365137	5.0634863
1000	86164.0908 seconds of time the)	(B) 大阪 (B) 177	The second
10000	earth takes to perform a rota-	4.9353264	5.0646736
1 307	tion about its axis	1.0010001	+ dereson
5 11	Half 43082.0454 (43082.0454)2	4.6342964 9.2685928	5.3657036 0.7314072
10. 850	Length of the tropical year	0.2000320	0.1314012
P.S. L. 875	=365d 5h 48m 50s= .	AND THE PARTY.	No. of Concession, Name of Street, or other Publisher, or other Pu
1100	31556930s	7.4990948	2.5009052
191	Metre 39.37079 inches .	1.5951741	8.4048259
7 13	3.2808992 feet .	0.5159929	9.4840071
1	1 French toise= 1.065777 fath.	0.0276664	9.9723336
1	1 Myriametre = 6.213856 miles	0.7933608	9.2066392
-	1 Hectare = 2.47117 acres	0.3929026 1.5479850	9.6070974
Stere	1 Cubic metre =35.31716 feet 1 Cu. Decimetre=61.0286 inches	1.7855291	8.4520150 8.2144709
Litre	1 Kilogramme =121.33 lb. Troy	1.0839682	8.9160318
ME BULL	1 Gramme =15.444 grains T.	1.1887598	8.8112402
W-15	Mean circumference of the earth 24856 miles	4.3954312	5.6045688
1	Diameter 7912 miles	3.8982863	6.1017137
100	Radius of Equator 3962.349 miles	3.5979528	6.4020372
100	Semipolar axis 3949.669	3.5965608	6.4034392
Mr. mar	Difference 12.680	1.1031193	8.8968807
HOUSE.	Geographical mile=6075.6 feet	3.7835892	6.2164108
Q to the	Circumference of the equator = 24896 miles	4.3961296	5.6038704
110	Radius of Eq. = 20920000 ft. from 1	7.3205617	2.6794383
100	a Mean of Playfair and Lambton J Mean Velocity of sound 1140 feet	SALES COL	VLOS SILVERS
THE PARTY NAMED IN	per second	3.0569049	6.9430951
ALC:	Modulus of Tabular logs.	Section 1	STATE OF THE PARTY
Sec. 200	=0.4342944819 .	BERT M 1 20-2002	
See Mr.	Double 0.8685889638 .	100 To 10	MACS STATE OF THE PARTY OF THE
1	Reciprocal or hyper. log. 10	2.3025851	7.6974149
62 11 4	Log. of this	0.3622149	9.6377851
NE WE	Number of which 1 is the hyp. log. 1	0.4342945	9.5657055
18-55	its recip. 0.36787944 .	新年4分分元6 位	SHARING
THE REAL PROPERTY.	Length of seconds pendulum	Was the same	PROPERTY AND ADDRESS.
	at London 39.1393 inches .	1.5926130	8.4073870
1	at Edinburgh 39.1555 in.	1.5927928	8.4071072
SECTION 1	Force of gravity or g at.	1 5077999	9 40000000
5	London 32.19084 . Edinburgh 32.20415 .	1.5077222	8.4922778 8.4920891
1g	London 16.09542	1.2066922	8.7933078
25	Edinburgh 16.102075	1.2068809	8.7911191
	THE RESERVE THE PARTY OF THE PA	10 40 50	CALL STREET, SQUARE, S

 $h = \begin{cases} 251.5 + \frac{3}{2}(n-1) \end{cases} n \text{ in which } h \text{ is the height in feet, and } n \text{ the change of temperature.}$ $n = \frac{h}{251.5 + 0.005h} \text{ very nearly, } n \text{ being the change of temp. in degrees of Fah.}$ $t = 97^{\circ}.08 \text{ cos.}^{\frac{3}{2}} \lambda - \left(10^{\circ}.53 + \frac{h}{251.5 + 0.005h}\right) \text{ in which } t \text{ is the temp. and } \lambda \text{ the latitude.}$

Moor			1	AB	LE	LX	1V.				Ioriz	ont	al Par		ot H	igh \	Vater		_	_	m'i
ran	sit	54'	55	56'	57'	58'	59'	60'	Trut	0'5	Maan	9 1	64	55'	56'	57'	58'	59	60		nsi
	m	m	m	m _2	m _0	m L 9	m + 4	m +6	h	m	h 6	m O	_56		_60	62	65			h 18	m
0	0	6	5	4	3		+1		1.0	10	1.00	10	52	54	56	59	62	65	68	10	10
2	50	8	7	6	5	-0	0	-1		20		20	49	51	53	55	58	60	63		20
	30	10	10	9	10	10	9	5	113	30		30 40	46	44	50 45	51 41	54	56	58		30
	50	15	14	13	13	12	12	11		50		50	38	39	40	41	43	44	45		50
1	0	17	17	16	16	16	15	15	13	0	7	0	32	33	33	31	35	36	37	19	0
	10	20	20	19	19	19	19	18		10		10	27	27	28	28	29	30	30		10
	30	22	22	22 25	22 25	22	22	22		20 30	1.5	30	22 18	22 18	22 17	16	22 16	22	22		30
	10	27	27	28	28	28	29	29		40	. 4	40	11	11	10	10	8	7	- 6		40
-	50	29	30	31	31	31	32	33	-	50	-	50	6	- 6	_ 5	<u> </u>	- 2	0	+ 1		50
2	0	31 34	32 35	33 36	33	34	35	36	14	10		0	- 1 + 2	+ 1	+ 2	+ 3	5 9	7 12	14	20	10
	01	36	37	38	39	39	41	43	1	20		20	5	7	5 9	11	14	16	19		20
5	30	35	39	40	41	42	44	46		30	:	30	8	10	12	15	18	21	24		30
	10	40	41	43 50	44	46	48 50	50		40 50		40 50	11	13	16	18	21	25	28		50
3	0	44	45	47	49	51	53	-	15	0	9	0	14	17	18	21	23	27	30	-	0
	10	46	47	49	51	54	56	58	-	10	100	10	15	18	20	23	26	30	34	-1	10
2	90	48	49	51	53	56	58	61		20		20	17	19	22	25	28	32	36		20
	10	50	52	56	56 48	58 61	61	64		30		$\frac{30}{40}$	16	18	21	24	27	31	35		30
	50	53	55	57	60	63	66	69		50		50	16	18	21	23	27	30	34		50
4	0	55	57	59	62	65	69	72	16	U	10	0	15	17	20	23	27	30	34	22	(
	10	56	58	61	63		70	73		10		10	14	17	20	22	25	29			10
	30	57 58	60	63 64	65 66	63 69	72	75		30		20 30	13	16 15	18	20	23	27	31		30
	10	59	62	65	67	70	74	78		40		40	11	13	16	18	21	25			40
-	50	60	62	65	67	70	75	79	-	50	-	50	9	11	14	16		22	-	-	50
5	0	60	63 63	66	68	71	75 76	79 80	17	10	11	0	7	9	12	14	17	20	-	23	1
	10 20	60	63		68	71	75	80		20		20	4	6	7	9	11	14	20		20
	30	59	62	65	67	70	74	78		30		30	+ 2	4	6	7	9	12	14	4	30
	10 50	58	61	63 62	65	68	72 71	76		50		40 50	_ 2	_ 1	+ 1	5	7	6		1	40
6	0	56	58	_	64	-	69	_	18	-	12	0	_ 1	0	0	+ 0		+ 4	_	24	-
~	-	-	-	-	TA	BL					find	mg	the	Heigi	nt of t		ide.	-		140	_
٦,	T:	me.	1		n's	Hor RO'	1	Moo	n's		-		pon's Par.		Tin	100	Mult.	Ti		NT	1.
	1.11	ne.	-	_	_	liers.	-	Mu	_		-	_	ultipl		- 111	ue.	M LILL.	111	ine.	Mu	It.
1	m	h	m												h	m		h	m	_	
0	0	12											50+0				1.000		10	0.5	
													4a+(0.998 0.993	3		0.4	
2	0	14											4a+0		0 3	30	0.985	3	40	0.3	
_	22												54+0				0.974		50	0.3	
3 :		15 16											6a+0			000	0.959 0.941	4	4.2	0.3	
		16	400	460	a+(0.74	960.	413	a+0	.58	760	.37	24+0	.412	1 1	0	0.921	4	20	0.2	
		-0.4											5a+(0.597	4		0.2	
6		18	-										7a+0			-	0.871 0.843	4	_	0.1	-
7	20	19	20.0	,000)a+	1.27	760.	000	a+1	.00	060	.00	0a+0	0.703	6 1 2		0.812	5		0.1	
B	3	20	00	.084	4+	1.13	36 0.	030	a+0	.97	06.0.	.02	71+0	0.682	6 2	0	0.779	5	10	0.0	91
													5a+(0.774 0.708	5		0.0	
9		22											2a+(0.670	5		0.0	
10	40	22	400	.66:	a+	0.52	760.	587	a+().41	36 0.	.52	9a+	.290	6 2	10	0.631	5	50	0.0	90
-													6a+0				0.591 0.551	6		0.0	
12	0	24	Olo	.99	na+	5-1 T	JO U.	003	4+(.11	100	. 19	5a+(1.085	3	0	1.001	6	20	0.00	JU.

** • • •

TABLE LXVI.—Equations of Third Differences for Twelve Hours. Time Third Difference.																
Tin after N		90000	1	2000												
Midn		1'	2'	3'	4	5'	6'	7'	8'	9'	10'	10"	20"	30'	40"	50"
+	1	"	"	"	"	"	"	"	"	"	n	"	"	11	"	"
h m	h m	1001	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	1000	300	0.0	1 2 4	0.0
0 0 0 0 30	12 0 11 30	0.0	0.4	0.5	0.7	0.9	1.1	1.3	1.5	1.6	1.8		0.1	0.1	10000	0.0
1 0	11 0	0.3	0.6	1.0	1.3	1.6	1.9	2.2	2.5	2.9	3.9		0.1	0.5		0.3
1 30	10 30	0.4	0.8	1.2	1.6	2.1	2.5	2.9	3.3	3.7	4.1		0.1	0.5		0.3
2 0	10 0	0.5	0.9	1.4	1.9	2.3	2.8	3.2	3.7	4.2	4.6	0.1	0.2	0.	0.3	0.4
2 30	9 30	0.5	1.0	1.4	1.9	2.4	2.9	3.4	3.8	4.3	4.8	0.1	0.2	0.5	0.3	0.4
3 0	9 0	0.5	0.9	1.4	1.9	2.3	2.8	3.3	3.7	4.2	4.7	I BOSSIC	0.2	0.5		0.4
3 30	8 30	0.4	0.9	1.3	1.7	2.2	2.6	3.0	3.4	3.9	4.5	1 100000	100000	0.:	9 100000	0.4
4 0	8 0	0.4	0.7	0.9	1.5	1.9	2.2	2.6	3.0	3.3	1000		H 200	0.	2000	0.3
4 30 5 0	7 30	0.3	0.4	0.6	0.8	1.0	1.2	1.4	1.6	1.8	10000		400200	0.		0.2
5 30	6 30	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	17 37 0	1 1000	100000	1000		0.1
6 0	6 0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.	0.0	DESCRIPTION OF THE PERSON OF T
+	-		12.47				100	100		20		123	16.60		1	6
THE REAL PROPERTY.	TABL	EL	XVI	1.—	Equa	tions	of F	_			_	_	welve	e He	ours.	
Time Fourth Difference.											03		0 38			
	dnight.	-	1'		2	3′	4'	-	5'	10		20"	30	"	40"	50"
h m	h	n	"	"	1	11	"		"	10		"	1	,	"	"
0 0	12		0.0	0.0)	0.0	.0.0	0	0.0	1000	0	0.0	0	.0	0.0	0.0
0 30	1000		0.2	0.4		0.6	0.9	8	1.0		0	0.1		1	0.1	0.2
1 0	11	0	0.4	0.8	3	2.2	1.0	_	2.0	0.	1	0.1	0	.2	0.3	0.3
1 30			0.6	1.5		1.7	2.		2.9	0.	201	0.2		.3	0.4	0.5
2 0			0.7	1.	_	2.2	3.	200	3.7	1000	1	0.2	1000		0.5	0.6
2 30			0.9	1.8		2.7	3.6		4.5	0	-	0.3	0.4		0.6	0.7
3 0		0	1.0	2.		3.1	4.1		5,1	1000					0.7	0.9
3 30	1 2 5	80	1.1	2.	_	3.4	4.		5.7		2	0.4		.6	0.8	0.9
4 30	100000	30	1.3	2.		3.9	5.	_	6.5	100	2	0.4		7	0.8	1.0
5 0	1000	0	1.4	2.	E111	4.1	5.		6.8		.2	0.5		.7	0.9	1.1
5 30		30	1.4	2.		4.2	5.	6	7.0	0	.2	0.5		.7	0.9	1.2
6 0	6	0	1.4 2.8		-	N. SCHOOL SECTION		6	7.0	-	.2	0.5	0.7		0.9	1.2
100	m	6.3		A			BLE				100	0			(1)	100
-	To	nna	tne	4	1 6		e Al	tituc	le of	the 1	ole	Star		_	100	
Merid	ian Dis	tance		orrec	-	n.	Log.	M	eridia	n D	istar	100	Corr		An.	1
NAC.	aut Dis	built		tion.	SUI MOOS		f A"		- I I CLE		Lotte	ice.	tion	-	varia-	Log.
-1	+ +		30	LIUIII	-	-	1000		- 10-	-	+1		1,00		tion.	of A"
h mh			m°	1	,	11		h	_	_	m	m	7	11	"	-
0 01				37 4	8 19	.45		3	09	0 18			1 9	-	13.74	1.6205
10	12001	200	501		90 60	2000	.2009		22 100	50	10	50	1 6	5	13.15	1.6569
20	254	200, 10 114	401				.8021			40	20	40	1 2	52	12.51	1.6899
30	BOOK IN THE PERSON NAMED IN	200	301	1223			.152			30	30		0 59	32	11.84	1.7205
40	10000	50	201				.592		202	20	50	100	0 56			1.7483
1 0	CONTRACTOR OF THE PARTY OF	0 23	-		100 202	2000 F	1.747		08	100	2000		0 52 0 48	33		1.7735
10	THE RESERVE AND ADDRESS.	10					.877		1 1 1	50	10		0 45		8.99	1.7965
20	40	20	401	41	54 18	3.30	.989	7	200	40	20	40	0 41	19	8.99	1 9961
30		30	301	30	21 17	7.99	.087	1		30	30	30	0 37	26	7.45	1.8527
40		40		28	38 17	1.62	.173	3		20	40	20	0 33	27	6.66	1.8675
	10 10 0 14	50 29	101				1.250		50 7	10	50	10	0 29	25	5.85	1.8803
10	50	10 22	50 1				1.381		07	50	10		0 25 0 21			1.8715
20	40	20	401				1.438		20	40	20		0 16			1.9007
30	30	30	30 1	17	36 18	5.42	1.490	3	30	30	30	30	0 12	46		1.9081
40	20	40	201	14	55 14	1.90	1.537	4	40	20	40	20				1.9139
50	10	50	101	12			2.580	9	50	10	50	10	0 4	16	0.85	1.9207
	N 10 10	-		-	1	18	100	6	06	01	8 0	18 0	0 0	0	0.00	1.9215
			17.5				250	200	OUTO	207	100	-	THE O	-	100/00	-







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